

Benoît BRAÏDA

**Is qualitative VB theory useful for
current chemical problems ?**

**Laboratoire de Chimie Théorique
Université Pierre et Marie Curie - Paris6**

Purpose

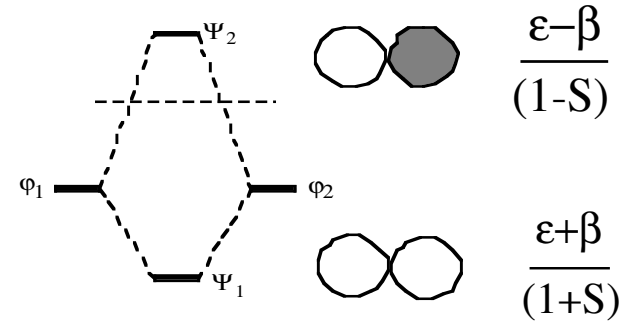
Models (VB theory here) can bring useful insight on non-trivial system

- Basics of qualitative VB theory
- MO & VB analysis of «pancake bonding» DTCNE
- Verification by correlated VB calculations

Qualitative VB

Effective Hamiltonian : $H^{\text{eff}} = (\mathbf{h}(1) + \mathbf{h}(2) + \mathbf{h}(3) + \dots)$

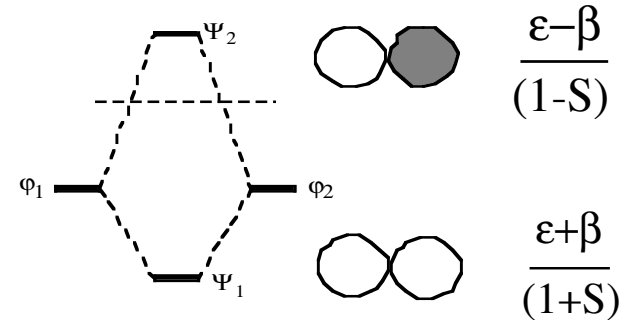
Parameters: β , S , ϵ (same as in the MO framework)



Qualitative VB

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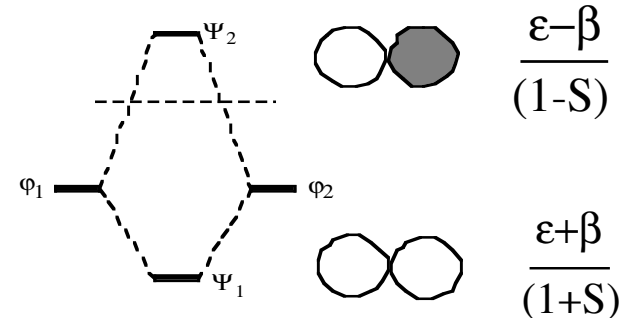
1) Energy of a determinant :

$$\langle D_i | H | D_i \rangle = \frac{-2n\beta S}{1 - S^2} \quad n = \text{N}^\# \text{ of neighboring } (\uparrow\uparrow) \text{ pairs}$$

Qualitative VB

Effective Hamiltonian : $H^{\text{eff}} = (\mathbf{h}(1) + \mathbf{h}(2) + \mathbf{h}(3) + \dots)$

Parameters: β , S , ϵ (same as in the MO framework)



1) Energy of a determinant :

$$\langle D_i | H | D_i \rangle = \frac{-2n\beta S}{1 - S^2} \quad n = \text{N}^\# \text{ of neighboring } (\uparrow\uparrow) \text{ pairs}$$

2) Off diagonal terms :

- Determinants differ by 2 spinorbitals:

$$\left\langle \left(\left| a \bar{b} \right| \right) \left| H \right| \left(\left| b \bar{a} \right| \right) \right\rangle = 2\beta_{ab} S_{ab}$$

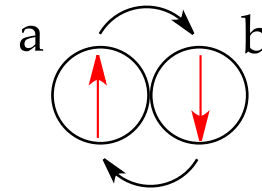
- Determinants differ by + than 2 spinorbitals :

$$\langle D_i | H | D_j \rangle = 0$$

Qualitative VB

- 2e-bond :

$$\psi_{VB} = \frac{|a\bar{b}| + |b\bar{a}|}{\sqrt{2(1+S^2)}}$$

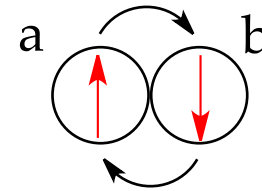


$$\Rightarrow E = \langle \psi_{VB} | H | \psi_{VB} \rangle = \dots = \frac{2\beta S}{(1+S^2)} = D_e(2e-bond)$$

Qualitative VB

- **2e-bond :**

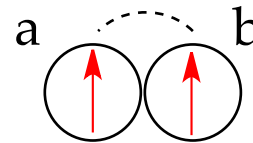
$$\psi_{VB} = \frac{|a\bar{b}| + |b\bar{a}|}{\sqrt{2(1+S^2)}}$$



$$\Rightarrow E = \langle \psi_{VB} | H | \psi_{VB} \rangle = \dots = \frac{2\beta S}{(1+S^2)} = D_e(2e-bond)$$

- **Triplet repulsion :**

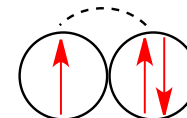
$$\psi_{VB} = \frac{|a\bar{b}| \ominus |b\bar{a}|}{\sqrt{2(1+S^2)}}$$



$$\Rightarrow E = \langle \psi_{VB} | H | \psi_{VB} \rangle = \frac{\ominus 2\beta S}{(1\ominus S^2)}$$

Same as **3e-repulsion :**

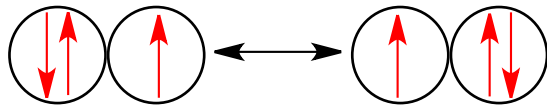
$$\psi_{VB} = |a\bar{a}b|$$



Qualitative VB

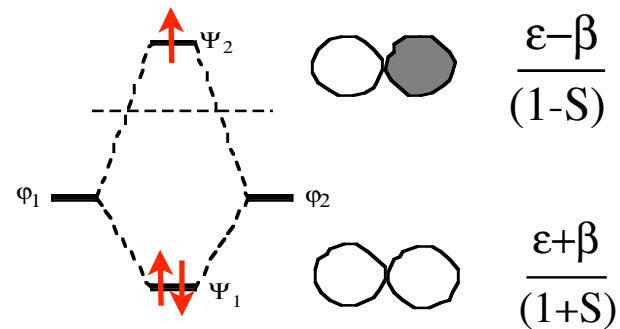
- **3-e bond** : Examples : the He_2^+ dimer cation , $\text{RS} \overset{\ominus}{\cdot\cdot} \text{SR}'$, π bonds in O_2 G.S

VB description :



$$\Psi_{VB} = |a\bar{a}b| + |b\bar{b}a|$$

MO description :

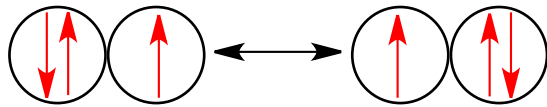


$$\Psi_{MO} = |\sigma\bar{\sigma}\sigma^*|$$

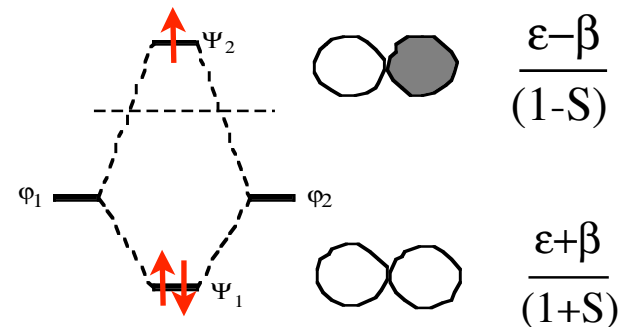
Qualitative VB

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VB description :



MO description :



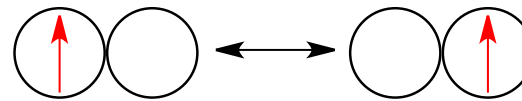
$$\Psi_{MO} = |\sigma\bar{\sigma}\sigma^*| = |(a+b)\overline{(a+b)}(a-b)^*| = \dots = -|a\bar{a}b| - |b\bar{b}a| = -\Psi_{VB}$$

$$\Rightarrow D_e = \frac{\beta(1-3S)}{(1-S^2)} \quad \Rightarrow S_{opt} \approx 0.17$$

Qualitative VB

- Elementary interactions :

1-e bond ($A\uparrow B$) =



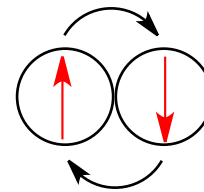
VB

$$\frac{\beta}{1+S}$$

MO

$$\frac{\beta}{1+S}$$

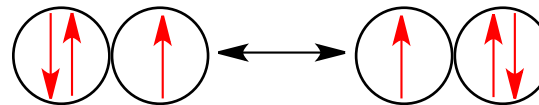
2-e bond ($A-B$) =



$$\frac{2\beta S}{1+S^2}$$

$$\frac{2\beta}{1+S}$$

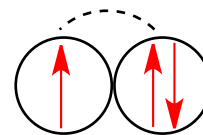
3-e bond ($A\cdot\cdot B$) =



$$\frac{\beta(1-3S)}{1-S^2}$$

$$\frac{\beta(1-3S)}{1-S^2}$$

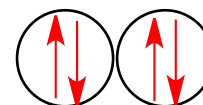
Triplet / 3-e repulsion ($A\downarrow\uparrow \uparrow B$) =



$$\frac{-2\beta S}{1-S^2}$$

$$\frac{-2\beta S}{1-S^2}$$

4-e repulsion ($A\uparrow\downarrow \downarrow\uparrow B$) =

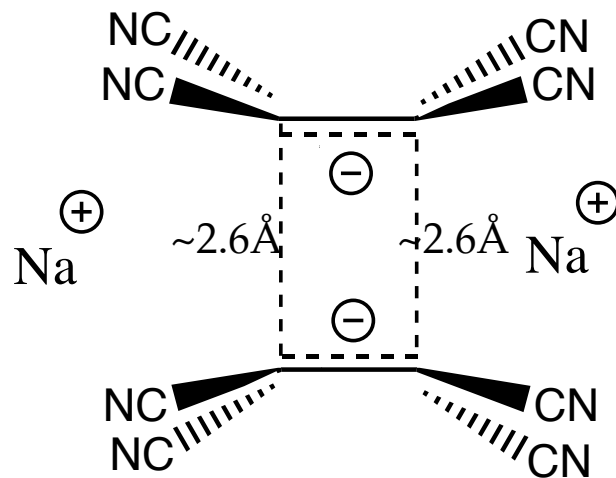


$$\frac{-4\beta S}{1-S^2}$$

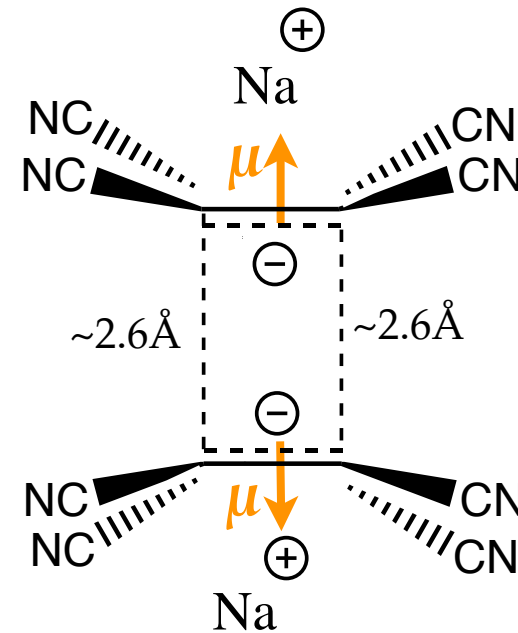
$$\frac{-4\beta S}{1-S^2}$$

«Pancake bonding»

- What kind of bonding in DTCNE_2^{2-} ?



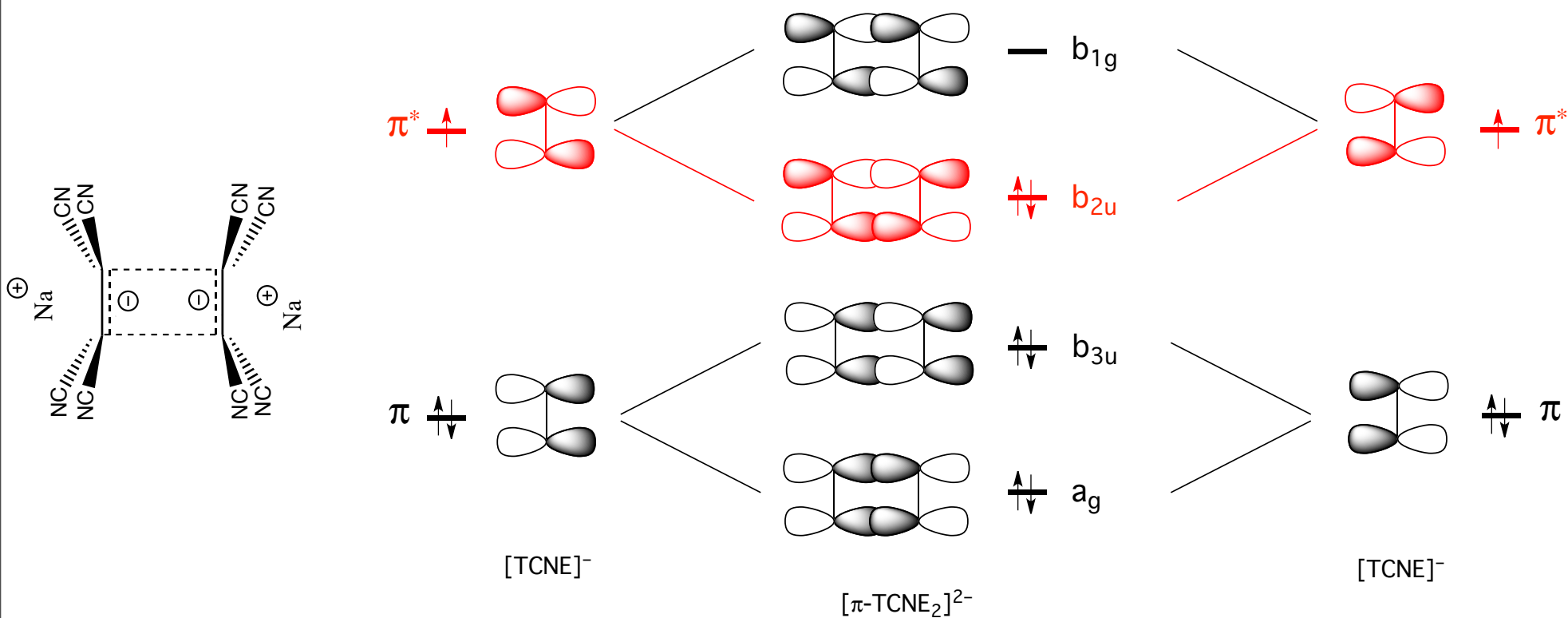
$$D_e \approx 80. \text{ kcal/mol}$$



$$D_e \approx 11. \text{ kcal/mol}$$

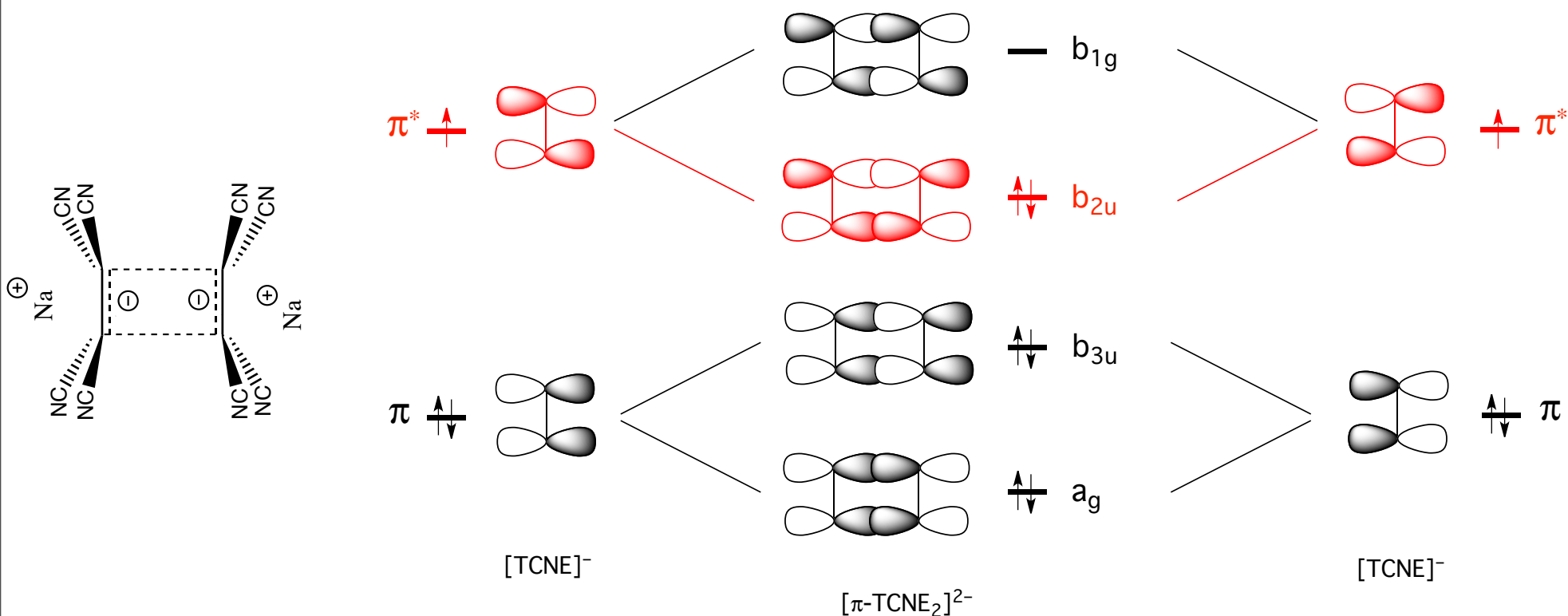
- Right geom : significant bonding force overcome repulsive electrostatics...
- $d_{\text{C} \cdots \text{C}} < \text{sum of vdW radii } (3.4 \text{ \AA})$, but much longer than C-C 2e bonds

«First sight» MO analysis

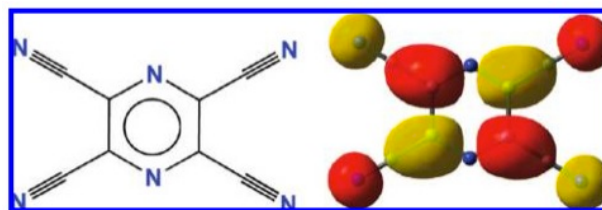


\Rightarrow a $4c/2e^-$ bond ?

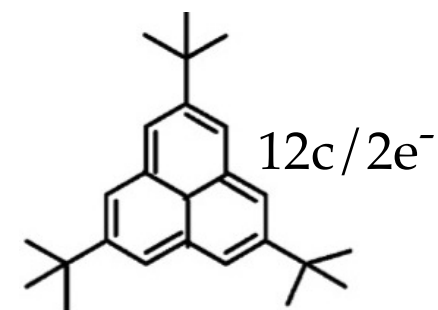
«First sight» MO analysis



⇒ a **4c/2e⁻** bond ?



8c/2e⁻

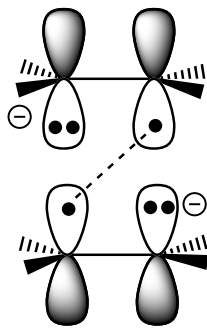
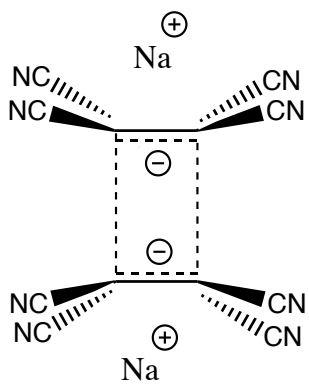


12c/2e⁻

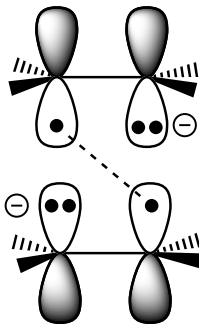
Others «pancacke bondings» : **nc/2e⁻** bond

VB analysis

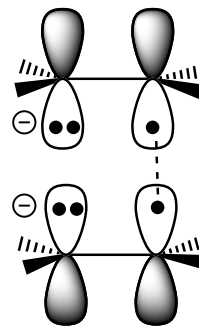
- VB set of structures :



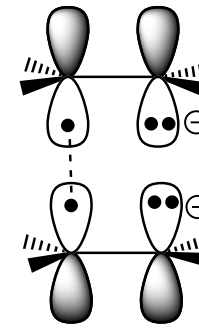
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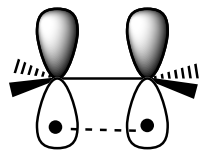
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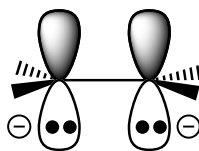
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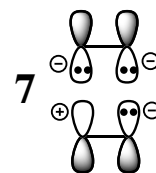
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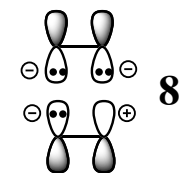
5



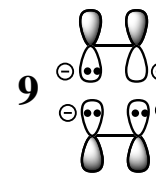
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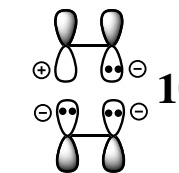
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8



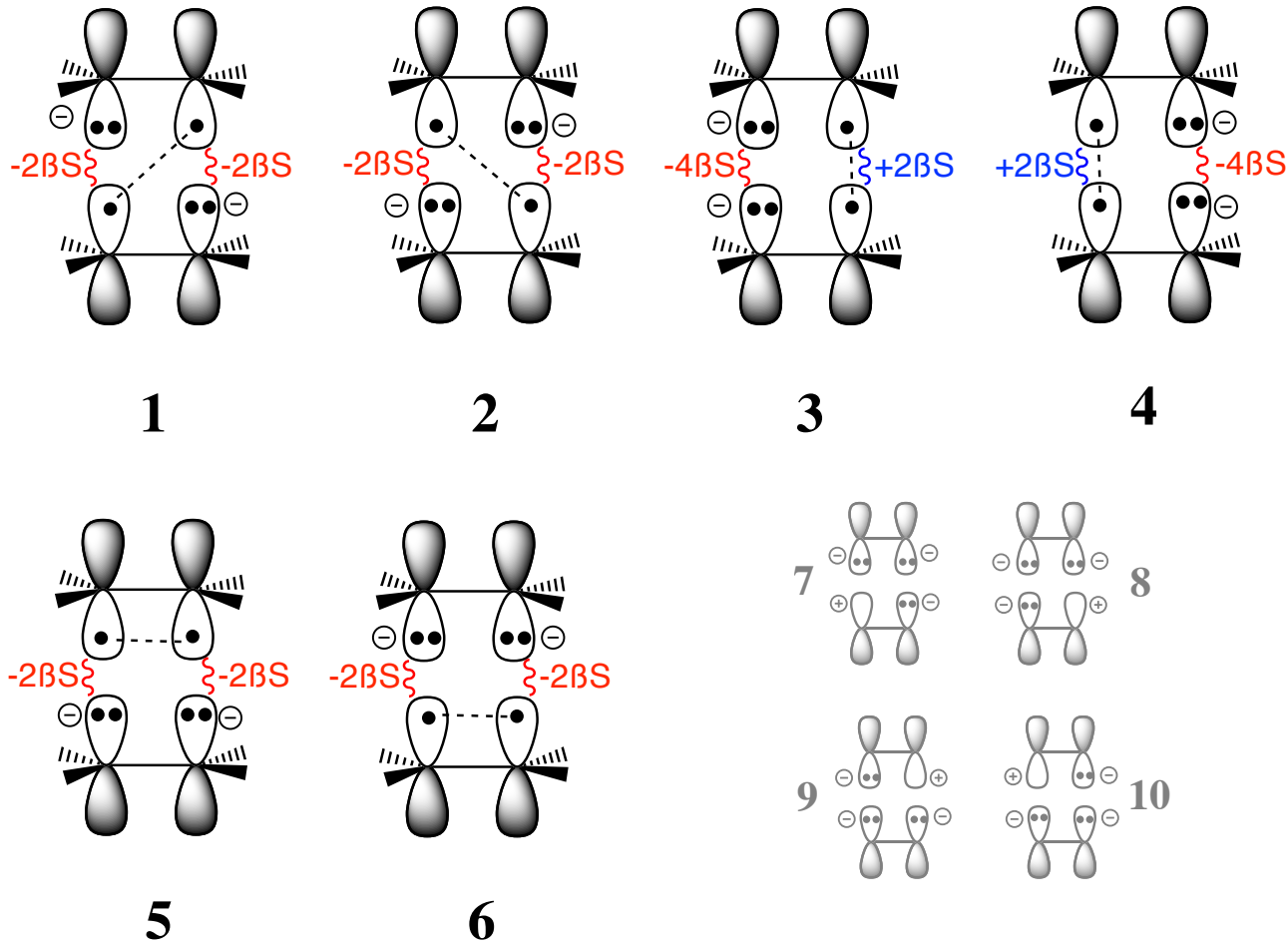
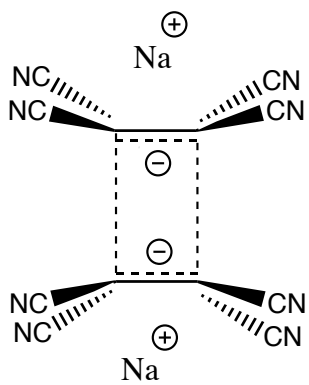
9



10

VB analysis

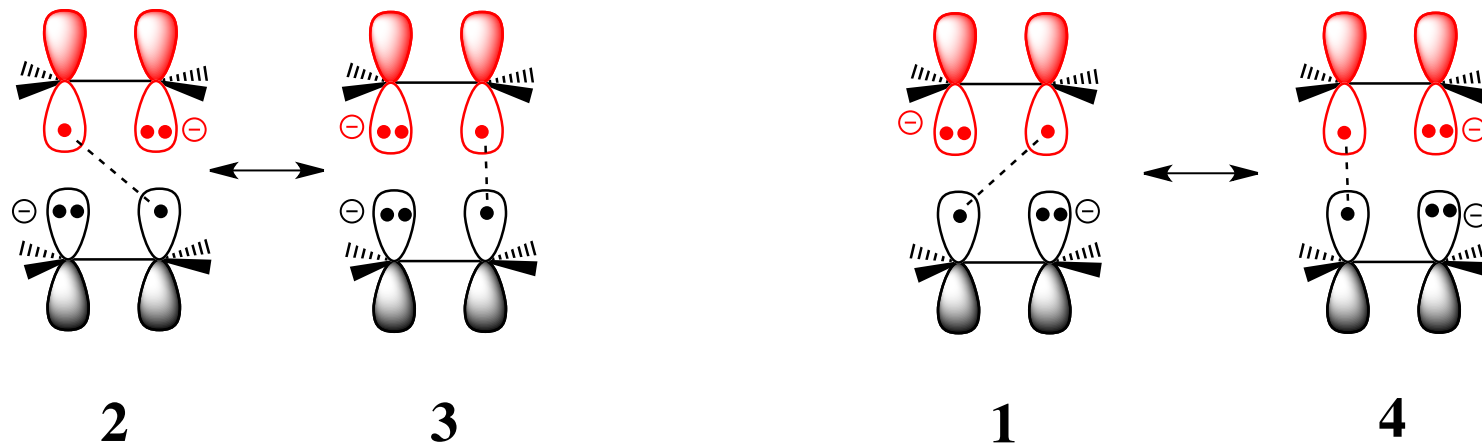
- VB set of structures :



⇒ No structure is bonding by itself, **all the bonding comes from the resonance**

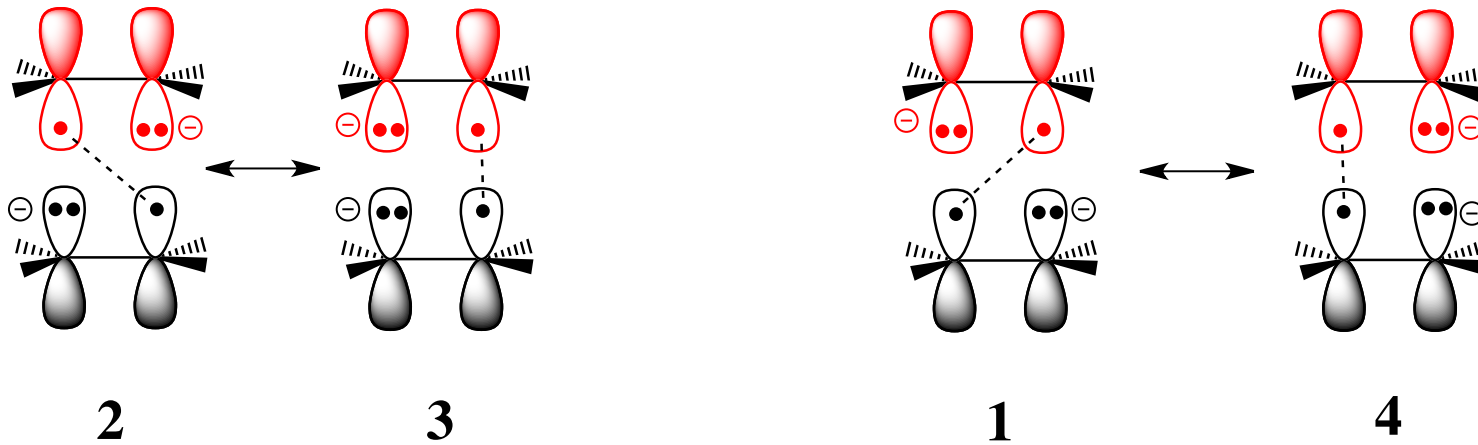
VB analysis

- $2 \leftrightarrow 3$ and $1 \leftrightarrow 4$: **intra-fragment $3e^- \pi$ bond** (upper fragment) :

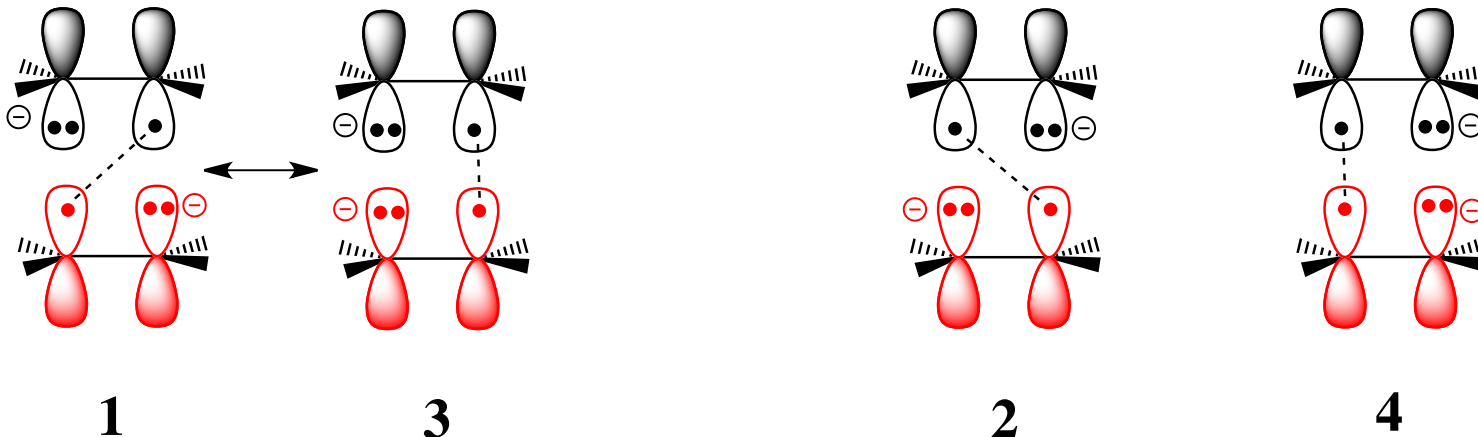


VB analysis

- $2 \leftrightarrow 3$ and $1 \leftrightarrow 4$: **intra-fragment $3e^- \pi$ bond** (upper fragment) :

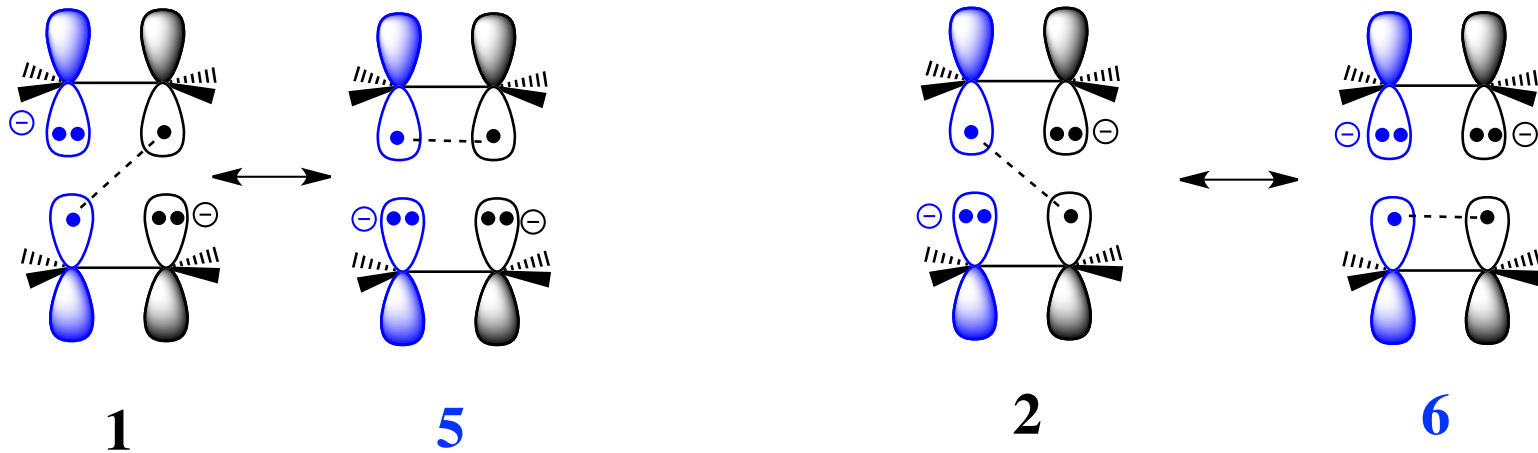


- $1 \leftrightarrow 3$ and $2 \leftrightarrow 4$: **intra-fragment $3e^- \pi$ bond** (lower fragment) :

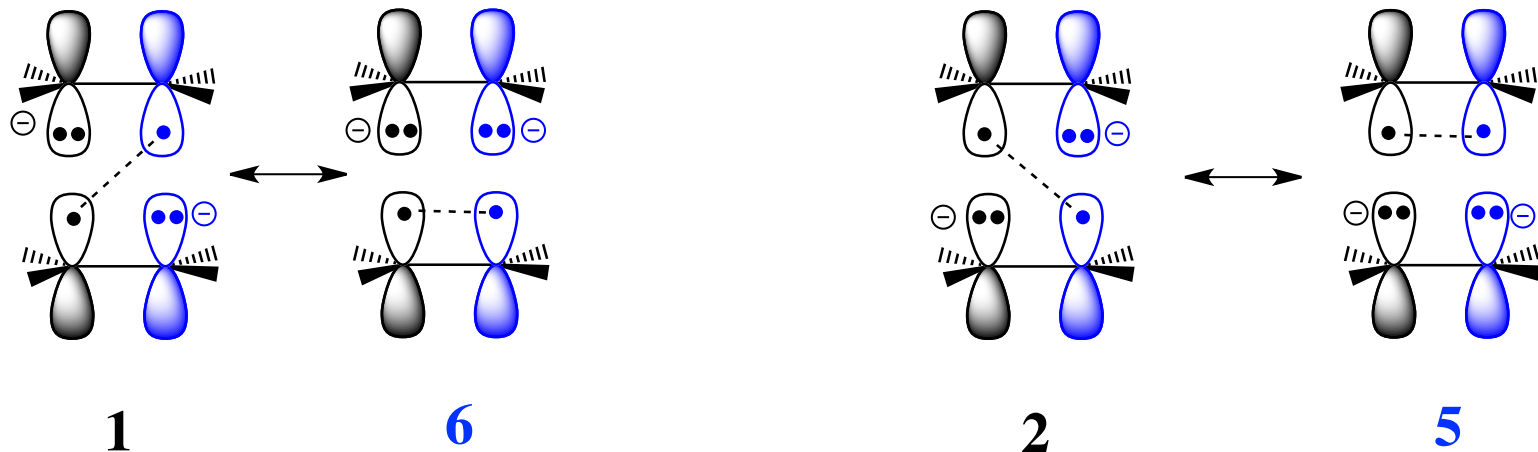


VB analysis

- $1 \leftrightarrow 5$ and $2 \leftrightarrow 6$: **inter-fragment $3e^- \pi$ bond** (left-hand side) :

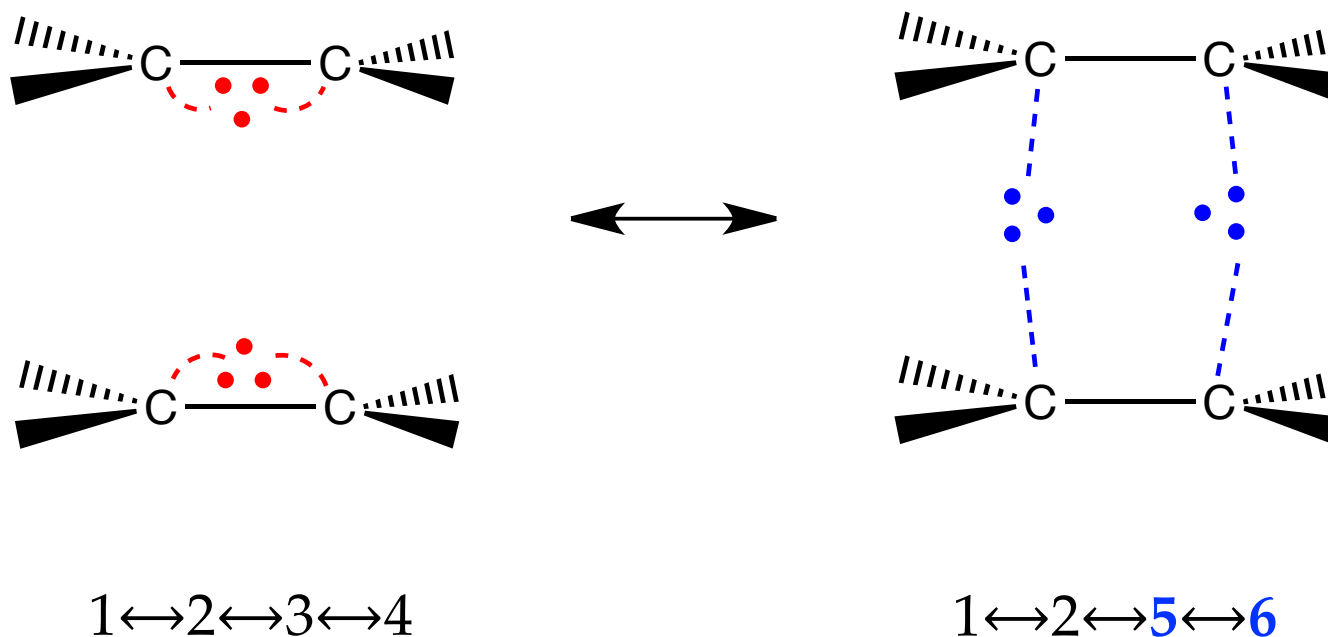


- $2 \leftrightarrow 5$ and $1 \leftrightarrow 6$: **inter-fragment $3e^- \pi$ bond** (right-hand side) :



VB analysis

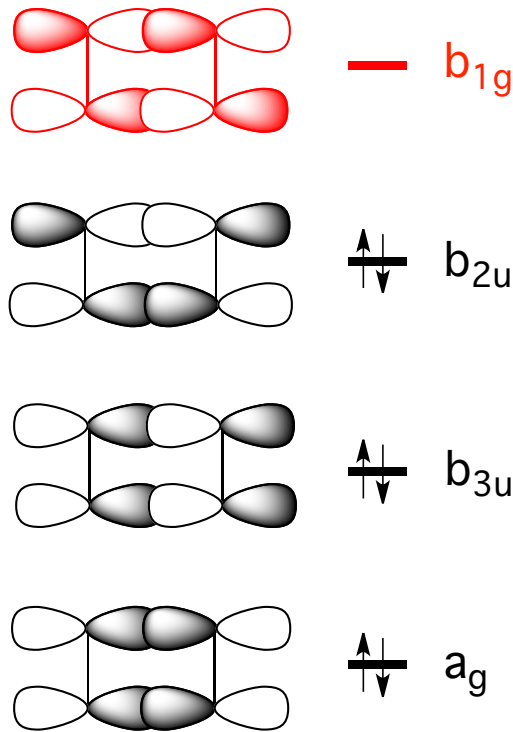
- Conclusion of the qualitative VB analysis :



⇒ bonding in DTCNE : two inter-frag. 3e bonds !

MO/VB mapping

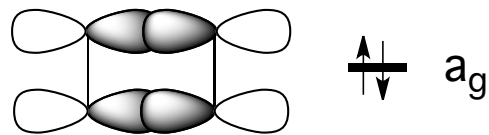
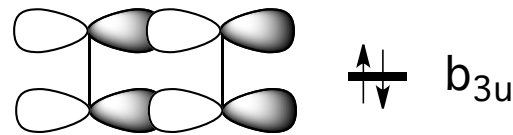
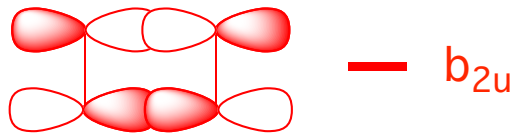
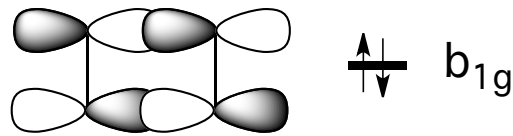
- HF determinant - development in VB basis of structures :



$$\Psi_{HF} = |a_g \bar{a}_g b_{3u} \bar{b}_{3u} b_{2u} \bar{b}_{2u}| = \dots = \ominus \Psi_1^{VB} \ominus \Psi_2^{VB} + \Psi_3^{VB} + \Psi_4^{VB} \ominus \Psi_5^{VB} \ominus \Psi_6^{VB}$$

MO/VB mapping

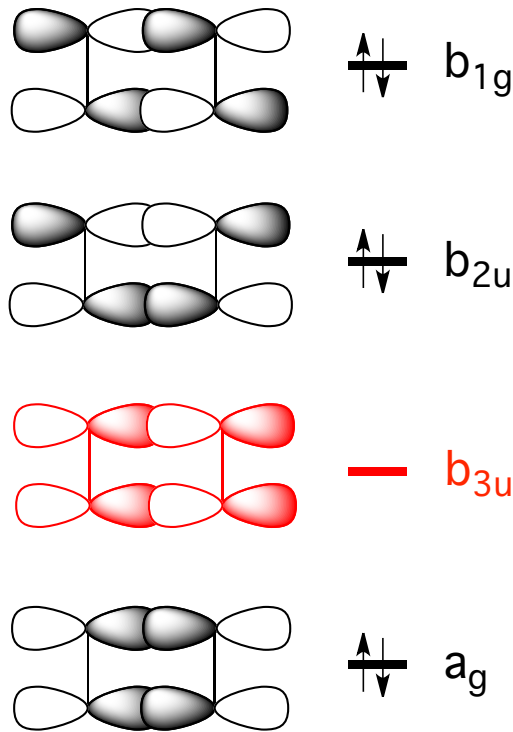
- 1st excited det. - development in VB basis of structures :



$$\Psi_{1-ext} = |a_g \bar{a}_g b_{3u} \bar{b}_{3u} b_{1g} \bar{b}_{1g}| = \dots = +\Psi_1^{VB} + \Psi_2^{VB} \ominus \Psi_3^{VB} \ominus \Psi_4^{VB} \ominus \Psi_5^{VB} \ominus \Psi_6^{VB}$$

MO/VB mapping

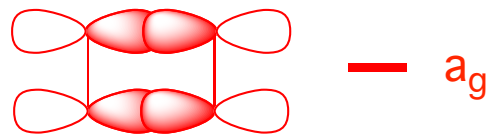
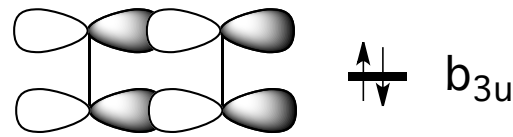
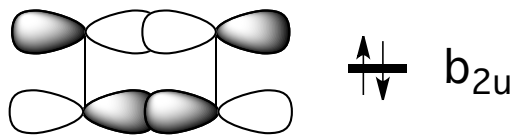
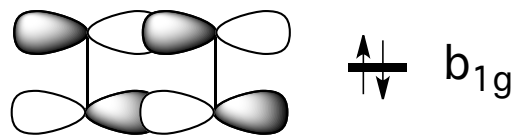
- 2nd excited det. - development in VB basis of structures :



$$\Psi_{2-ext} = |a_g \bar{a}_g b_{2u} \bar{b}_{2u} b_{1g} \bar{b}_{1g}| = \dots = +\Psi_1^{VB} + \Psi_2^{VB} + \Psi_3^{VB} + \Psi_4^{VB} + \Psi_5^{VB} + \Psi_6^{VB}$$

MO/VB mapping

- 3rd excited det. - development in VB basis of structures :



$$\Psi_{3-ext} = |b_{3u} \bar{b}_{3u} b_{2u} \bar{b}_{2u} b_{1g} \bar{b}_{1g}| = \dots = -\Psi_1^{VB} - \Psi_2^{VB} - \Psi_3^{VB} - \Psi_4^{VB} + \Psi_5^{VB} + \Psi_6^{VB}$$

MO/VB mapping

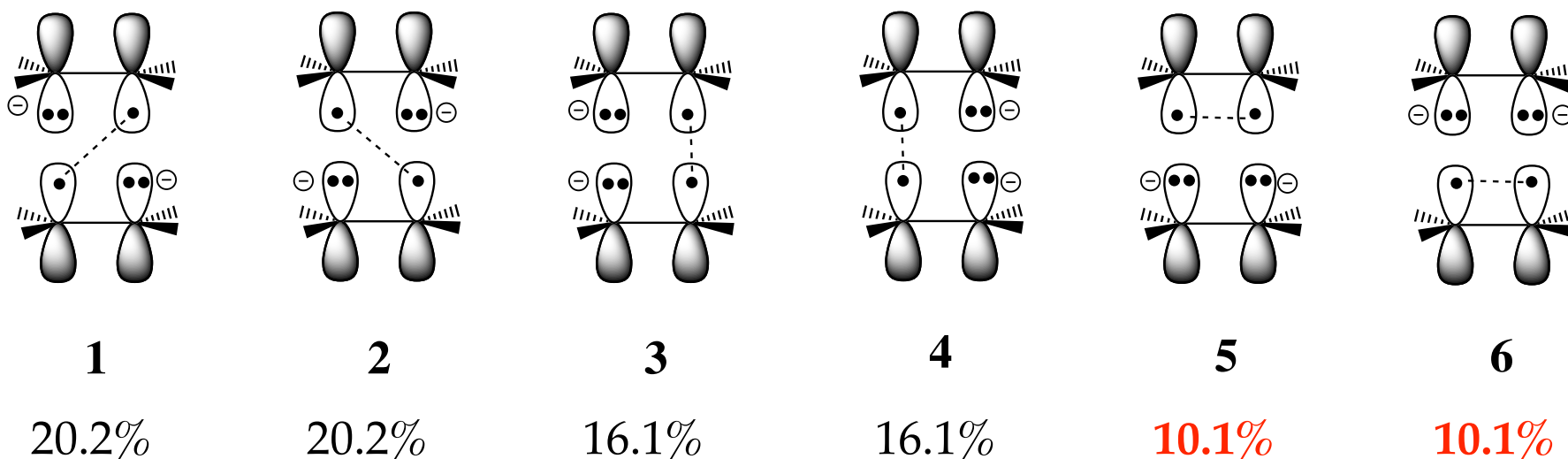
- CAS(4,4) \Leftrightarrow 6 VB structures mixing :

$$\left\{ \begin{array}{l} \Psi_{HF} = |a_g \bar{a}_g b_{3u} \bar{b}_{3u} b_{2u} \bar{b}_{2u}| = \dots = +\Psi_1^{VB} + \Psi_2^{VB} - \Psi_3^{VB} - \Psi_4^{VB} - \Psi_5^{VB} - \Psi_6^{VB} \\ \Psi_{1-ext} = |a_g \bar{a}_g b_{3u} \bar{b}_{3u} b_{1g} \bar{b}_{1g}| = \dots = +\Psi_1^{VB} + \Psi_2^{VB} - \Psi_3^{VB} - \Psi_4^{VB} + \Psi_5^{VB} + \Psi_6^{VB} \\ \Psi_{2-ext} = |a_g \bar{a}_g b_{2u} \bar{b}_{2u} b_{1g} \bar{b}_{1g}| = \dots = +\Psi_1^{VB} + \Psi_2^{VB} + \Psi_3^{VB} + \Psi_4^{VB} - \Psi_5^{VB} - \Psi_6^{VB} \\ \Psi_{3-ext} = |b_{3u} \bar{b}_{3u} b_{2u} \bar{b}_{2u} b_{1g} \bar{b}_{1g}| = \dots = +\Psi_1^{VB} + \Psi_2^{VB} + \Psi_3^{VB} + \Psi_4^{VB} + \Psi_5^{VB} + \Psi_6^{VB} \end{array} \right.$$

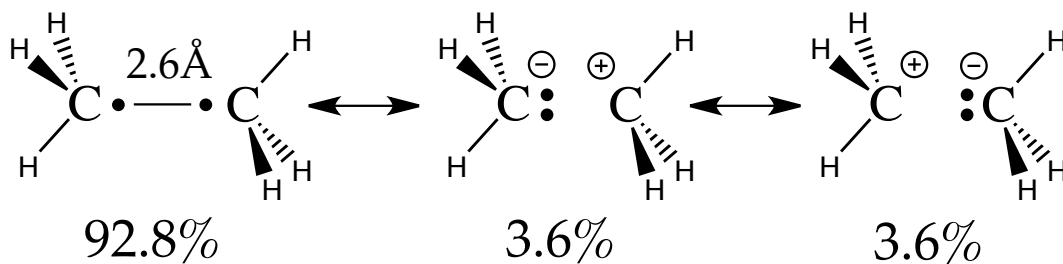
- MO (4x4) description = VB description
- VB analysis reveals the 3e-bond nature

Quantitative VB (1)

- DTCNE computed weights :



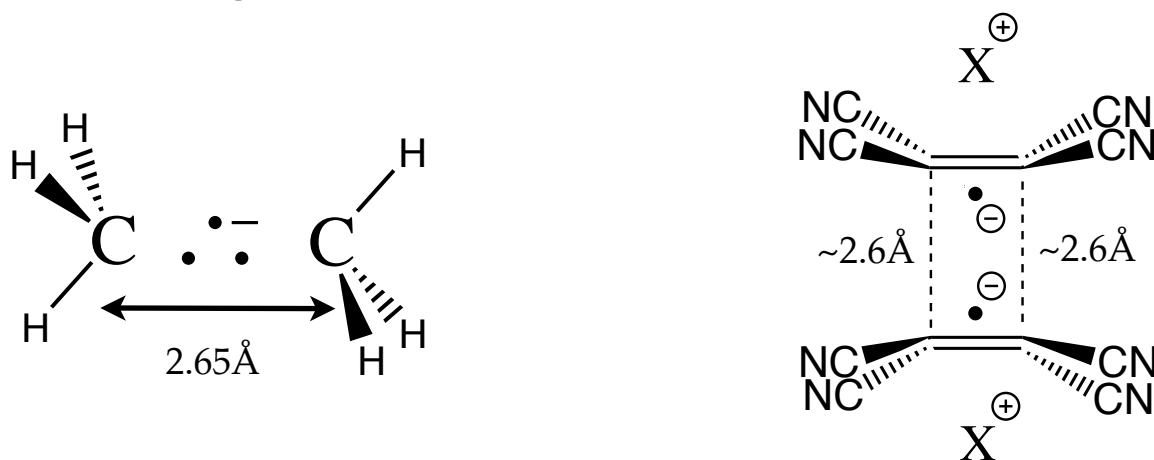
- Stretched ethane :



⇒ Str. 5-6 weights are not compatible with a 2c2e bond

Quantitative VB (2)

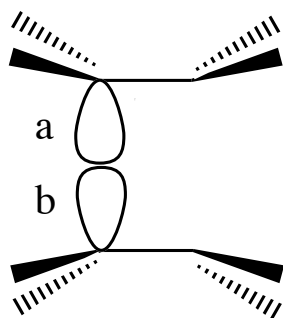
1) DTCNE bond length close to $3e^-$ bonded ethane anion :



2) DTCNE active orb. overlaps close to optimal $3e^-$ bond value :

$$S_{ab} = 0.15$$

(computed)

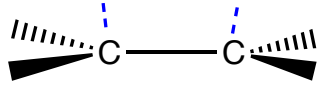
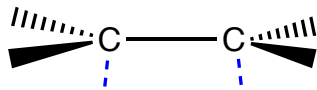
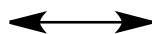
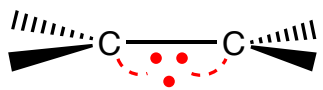


$$S_{opt} \approx 0.17$$

(from qualitative VB and Hückel)

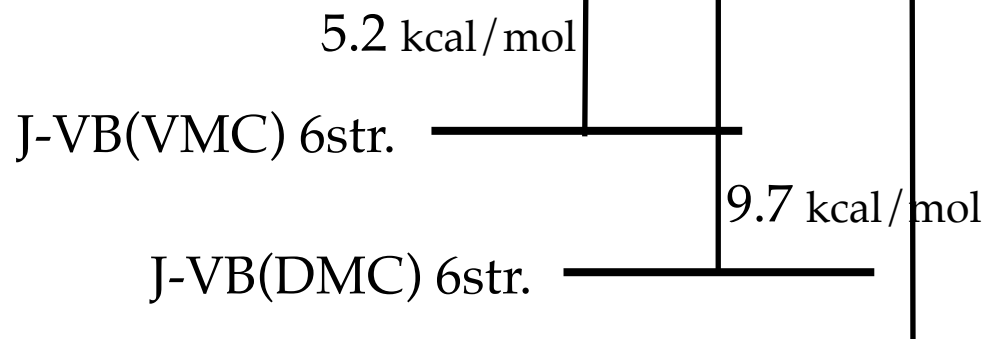
3) Dynamical Correlation Energy important for DTCNE

Quantitative proof (3)



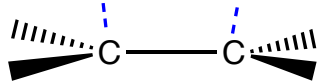
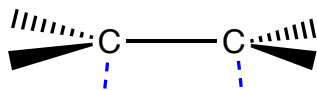
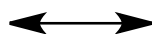
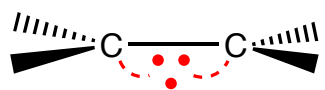
1 ↔ 2 ↔ 3 ↔ 4

1 ↔ 2 ↔ 5 ↔ 6



$\Delta E(\llcorner\text{reference}\llcorner) \approx 11. \text{ kcal/mol}$

Quantitative proof (3)



1 ↔ 2 ↔ 3 ↔ 4

1 ↔ 2 ↔ 5 ↔ 6



J-VB(VMC)

1 ↔ 2 ↔ 3 ↔ 4

10.6 kcal/mol

5.2 kcal/mol

J-VB(VMC) 6str.

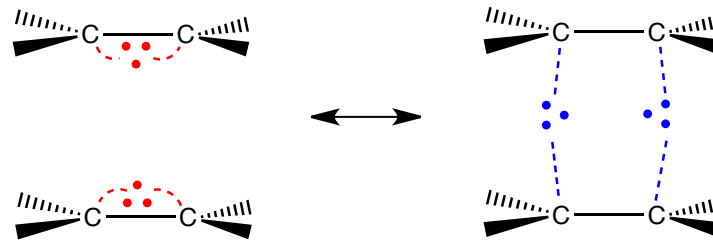
J-VB(DMC) 6str.

9.7 kcal/mol

ΔE

⇒ Without str. 5-6, DTCNE becomes repulsive !

Conclusion



- Qualitative VB analysis reveals the 3e-bonding nature in DTCNE multicenter «pancake» bonding system
- Confirmed by correlated VB calculations
- Models still important nowadays to «**understand**» :

*«I know that the computer has understood,
but I would like to understand too !» (E. Wigner)*

Conclusion

- VB allows to see things from a different perspective
(Prof. Keating, Dead Poets Society)

- Combining different models can lead to deeper understanding



Conclusion

- VB allows to see things from a different perspective
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- Combining different models can lead to deeper understanding

Thanks to :

Philippe HIBERTY, Kévin HENDRICKS



VB workshop in Paris !

Paris, July 2012

- ➔ plenary lectures on Valence Bond theory, methods, and related models,
- ➔ short talks given by participants on a topic relevant to VB theory,
- ➔ space dedicated to free discussions,
- ➔ "hands-on" lab : basic initiation to the XMVB and BLW programs (limited to 30 participants)

The logo for XMVB, featuring a stylized blue 'X' followed by 'MVB' in a bold, sans-serif font.

An Ab Initio Non-orthogonal Valence Bond Program

➔ <http://wiki.lct.jussieu.fr/workshop>



The name is Bond, Valence Bond !

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