



Enlighten Chemical Interactions Using Real Space Theories of Chemical Bond

Current Topics in Theoretical Chemistry School – Trujillo, Peru
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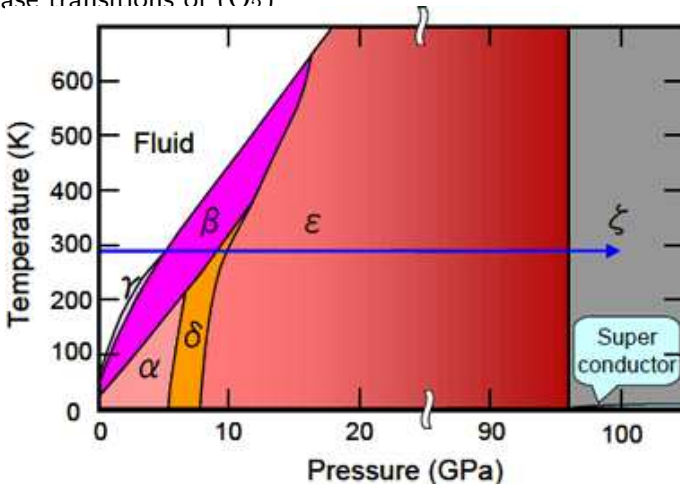


Outline

- 1 O₂ under pressure
 - The solid, (O₂)₄ unit
 - Model of solid: multireferential embedding of (O₂)₄
 - Interacting Quantum Atoms
 - Electron Distribution Functions
 - The (O₂)₄ in \mathfrak{R}^3
 - Chemical interactions: IQA and EDF
 - Spin structure and magnetic behavior: EDF
 - Conclusions (O₂)₄
- 2 Drawing Bonds with IQA
 - Conclusions (O₂)₄

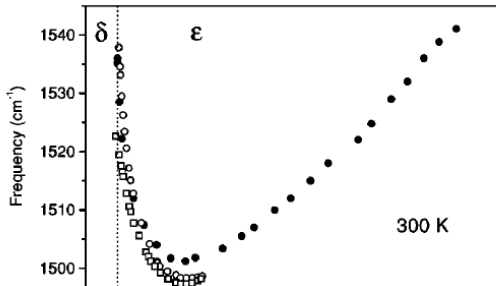
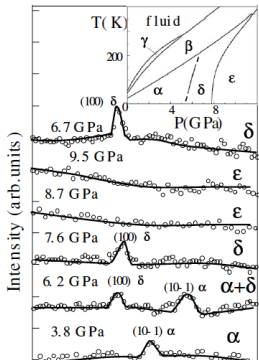
The solid, (O₂)₄ unit

Phase transitions of (O₂)



The solid, (O₂)₄ unit

- Changes in physical properties along the compression process
 - Magnetic and volume collapse (*Goncharenko, Phys. Rev. Lett. 2005, 94, 1*)
 - Peculiar spectroscopic behavior (*Gorelli, et al., H. Phys. Rev. B. 2001. 63, 104110*)



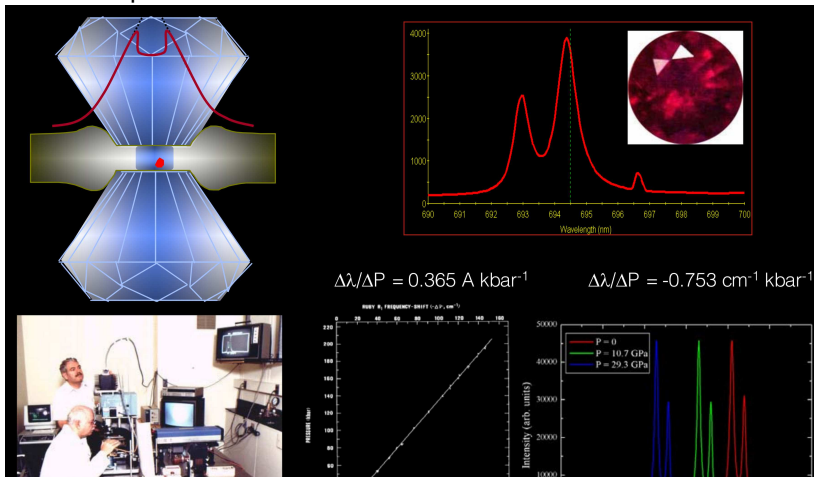


The solid, (O₂)₄ unit

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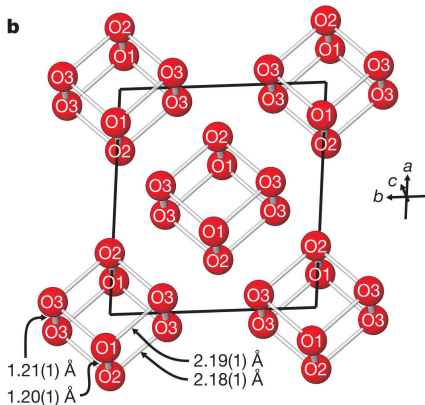
The solid, (O₂)₄ unit

Escala de presión-luminiscencia del Rubí



The solid, (O₂)₄ unit

- The structure for the ϵ -(O₂) was solved in 2006



Lundegaard, et al. *Nature*
2006 **443**, 201.

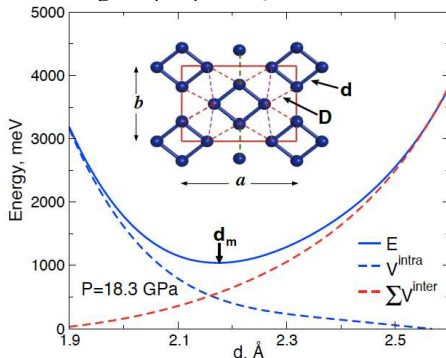
Fujihisa, et al. *Phys. Rev.*
Lett. 2006 **97**, 085503.



Model of solid: multireferential embedding of (O₂)₄

- The experimental geometry of ϵ phase was reproduced using high correlated methodologies. RCCSD(T)/CASPT2 for (O₂)₄ plus a pair potential for neighbor O₂ molecules

$$E(d) = V^{intra}(d) + \frac{1}{2} \sum_{ij} V_{ij}^{inter}(r_{ij})$$





Model of solid: multireferential embedding of (O₂)₄

Can we extract information about chemical bonding directly from Quantum Mechanics?



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- Wavefunction $\Psi(\vec{\chi}, t)$.
- **Operators**, $\hat{\mathcal{H}} = \hat{T} + \hat{V}$
- **Observables**, E .
- Electron density, $\rho(\vec{r}) = |\Psi|^2$
- Pair Density, $\rho_2(\vec{r}_1, \vec{r}_2)$
- La ecuación estacionaria de Schrodinger.

$$\hat{\mathcal{H}}\psi(\vec{\chi}) = E\psi(\vec{\chi}) \quad (1)$$

- There are not \hat{O} related with chemical bond, delocalisation, aromaticity, reactivity, etc.



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- Writing $\rho_2(\mathbf{r}_1, \mathbf{r}_2) = \rho(\mathbf{r}_1)\rho(\mathbf{r}_2) + \rho_2^{\text{xc}}(\mathbf{r})$,
 $E_{\text{int}}^{AB} = V_{\text{cl}}^{AB} + V_{\text{xc}}^{AB}$, interaction between atoms, where

$$V_{\text{cl}}^{AB} = \int_A \int_B \frac{\rho(\mathbf{r}_1)\rho(\mathbf{r}_2)}{r_{12}} + V_{en}^{AB} + V_{ne}^{AB} + V_{nn}^{AB}$$

$$\text{y } V_{\text{xc}}^{AB} = \int_A \int_B \frac{\rho_2^{\text{xc}}(\mathbf{r})}{r_{12}}$$

Blanco, et al., *J. Chem. Theory Comput.*, 2005 **1**,1096.



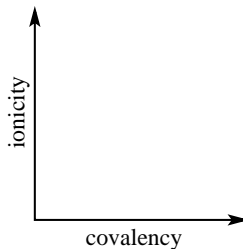
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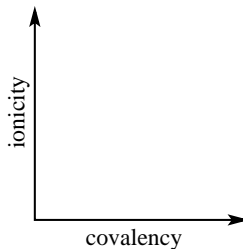


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Electron Distribution Functions

- A \mathcal{R}^3 partition defined by the $3N$ -dimensional domain D
- $\Omega_k (\cup_{k=1}^m \Omega_k = R^3)$



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- A \mathcal{R}^3 partition defined by the $3N$ -dimensional domain D
- $\Omega_k (\cup_{k=1}^m \Omega_k = R^3)$
- In a integer distribution of electrons, $(S) = n_1, n_2, \dots, n_m$, the probability to find n_1 electrons in Ω_1 , n_2 in Ω_2, \dots y n_m in Ω_m is defined by:

$$p(S) = \frac{N!}{n_1! \dots n_m!} \int_D |\psi|^2 dr_1 \dots dr_N,$$

$$\sum_s p(S) = 1$$

- S is named as a real space resonance structure (RSRS)

Francisco et al. J. Chem. Phys. 2007, 126, 094102.



The (O₂)₄ in \mathbb{R}^3

Computational details:

(O₂)₄ singlet state, CAS[8,8]//aug-cc-pVQZ

The reaction coordinate is the d_m defined by Bartolomei et al.

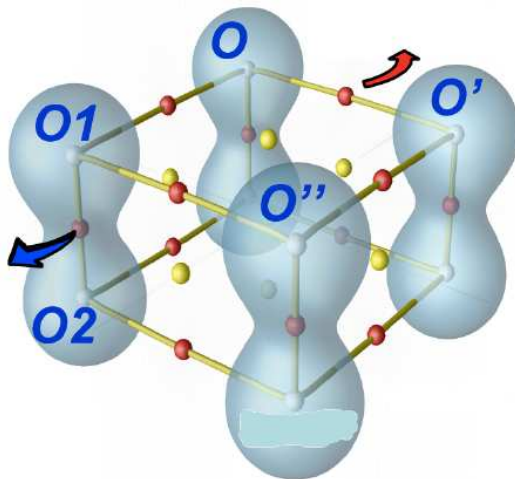
IQA partition was done using the PROMOLDEN code

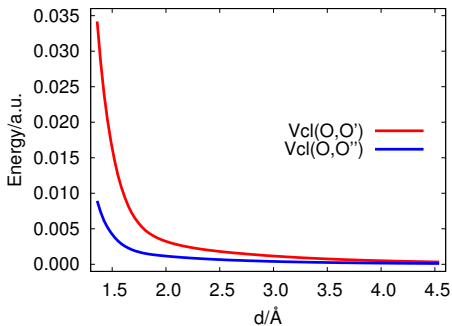
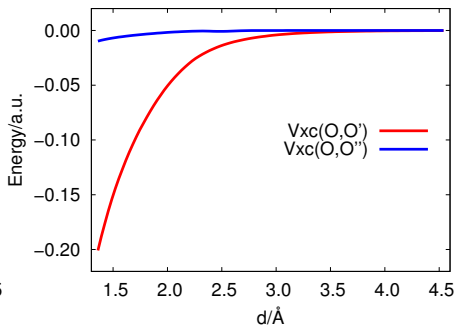
EDF calculations were done with the EDF code

AIM partition of \mathbb{R}^3 .

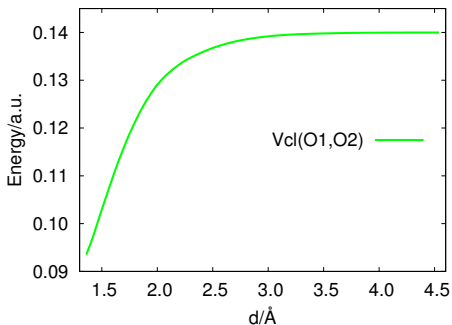
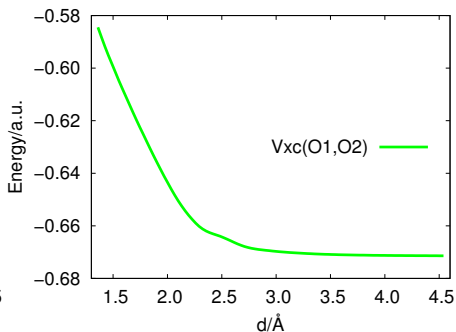


Chemical interactions: IQA and EDF



 V_{cl} inter-monomer V_{xc} inter-monomer

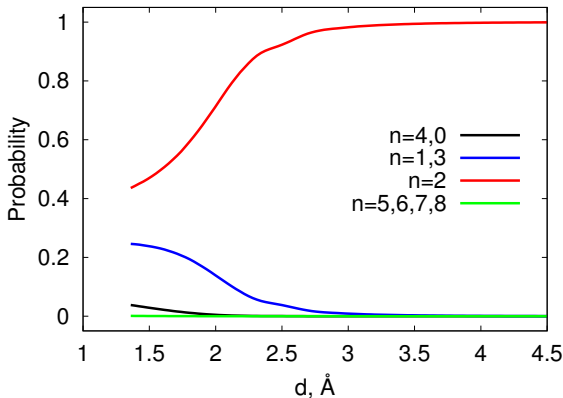
García-Revilla, et al., *J. Chem. Theory Comput.* 2013, 9, 2179-2188

 V_{cl} intra-monomer V_{xc} intra-monomer

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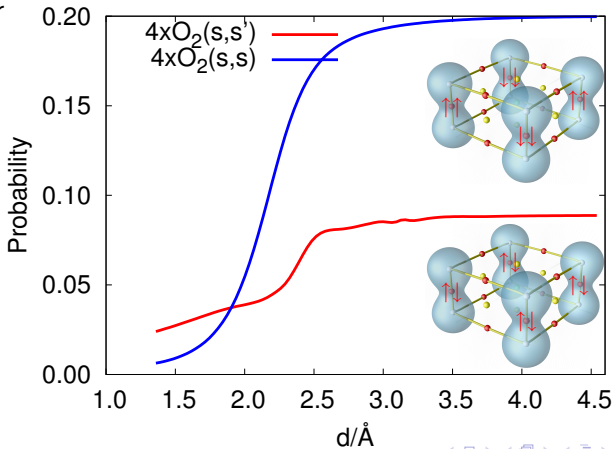


Spinless EDFs for the probability of finding a number n of active electrons in one oxygen molecule





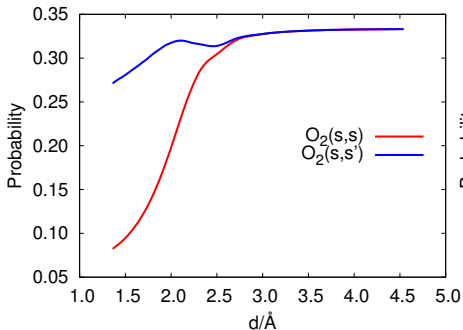
EDF probabilities for a spin arrangement in the molecular oxygen tetramer



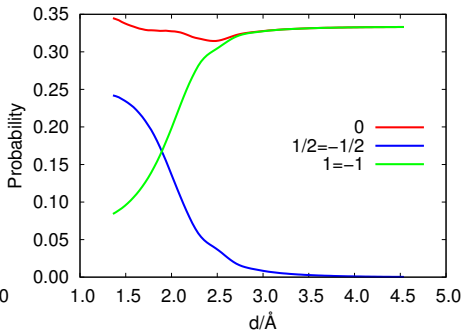


EDF probabilities for a given oxygen molecule within the molecular oxygen tetramer

S, single molecule



Ms, single molecule



García-Revilla, et al., *J. Chem. Theory Comput.* 2013, 9, 2179-2188



Conclusions (O₂)₄

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- Along the compression process the intermolecular bonding is built up from a simultaneous weakening of the intramolecular bond.
- EDF reveals the changes in spin structure along the compression process of (O₂)₄.
- EDF evidences a pairing of the electron spins at short distances in (O₂)₄ in agreement with the experimental behavior.



- Molecular models have been extremely useful to understand Chemistry
- Can we arrive to such molecular models from the Quantum Mechanics somehow?

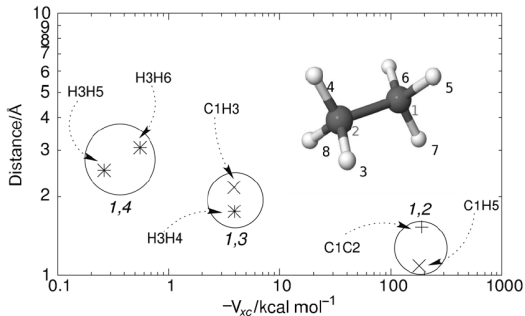


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Beyond the topology of $\rho(r)$ of QTAIM, IQA can be used to draw molecular graphs from energy partitioning.



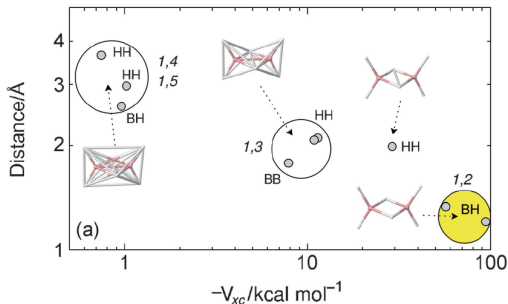
- A simple example, V_{xc} can be used to differentiate between different chemical interactions in ethane.



3 clusters can be found: (C-C, vicinal C-H), non vicinal C-H, and non vicinal H-H



Diborane interactions:

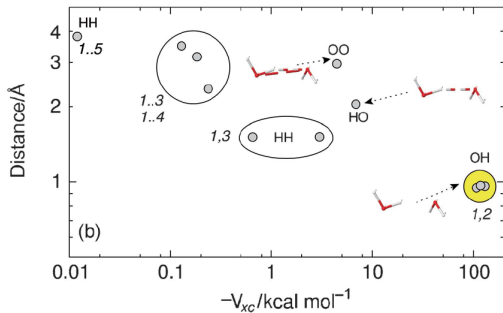


clusters differentiate interactions, observe molecular graphs

level of theory HF//6-311G(d,p)



Water dimer interactions:



clusters differentiate interactions, observe molecular graphs

level of theory CAS[6, 5]//6-311G(d,p)



Conclusions(O₂)₄

- Vxc is useful to draw molecular graphs with physical and chemical insight



Conclusions(O₂)₄



Conclusions(O₂)₄

Thank you!