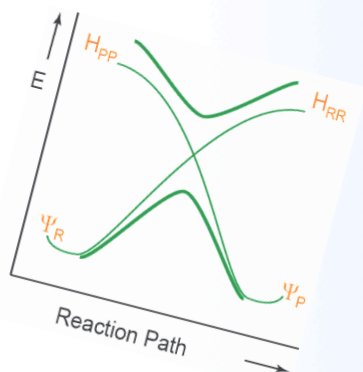




VB/MM Insights into Enzyme catalysis



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The Lise-Meitner Minerva Center for
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The Hebrew University of Jerusalem*

Acknowledgement

Hadar Crown
Avital Sharir-Ivry
Dr. Tamar Shnerb
Dr. Rajapandian Varatharaj
Moshe Amitay
Tamar Ansbacher
Dr. Hemant Kumar Srivastava

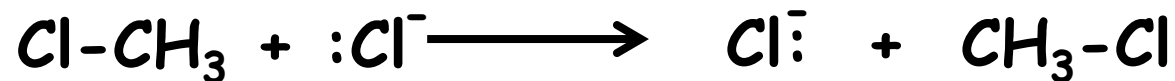


Collaborations:
Prof. Wei Wu

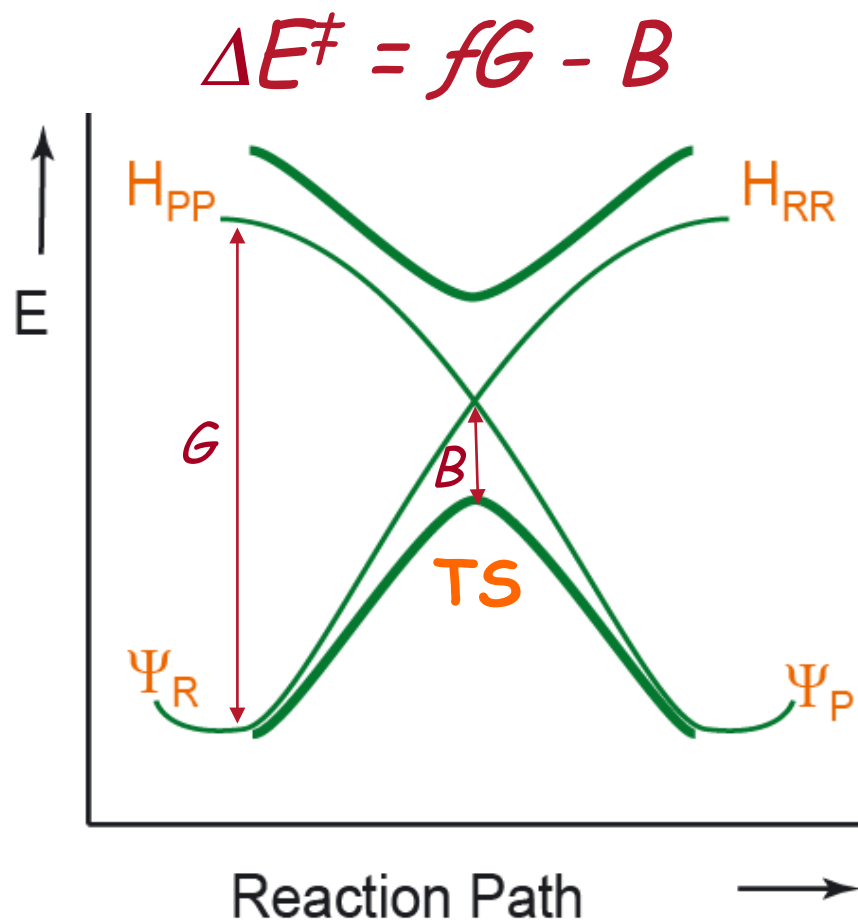
*Interested post-docs are most welcome to the group
to continue with this and other interesting projects*

\$\$\$ Israel Science Foundation (ISF)
Human Frontiers of Science Program (HFSP)
Alex Grass Center for Drug Design and Synthesis of Novel Therapeutics

VB - Reactivity Tool



VB Structures



Empirical VB (EVB)

Advantages

- ✱ Simple picture of reactivity
- ✱ Relatively fast
- ✱ Comparative - reduces mistakes
- ✱ Calibration - reliable results
- ✱ Good & easy description of Reaction Coordinate

Disadvantages / Problems

- ✱ QM region - parameterization
- ✱ Difficult to handle more than two states
- ✱ Strong assumptions

ab initio VB/MM

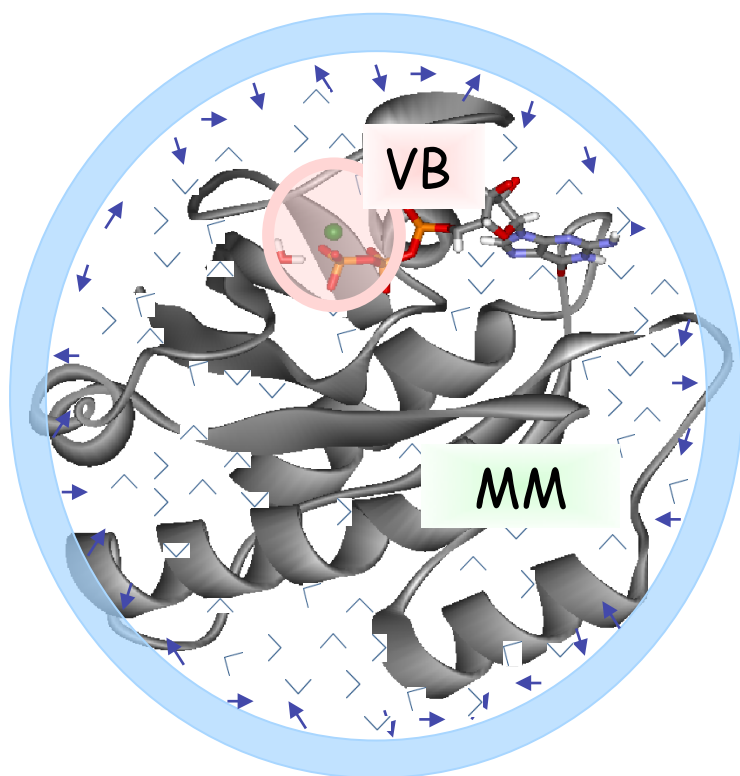
Ab-initio VB/MM

$$H_{VB/MM} = H(VB) + H(MM) + H(VB/MM)$$

Bonding

Electrostatic

✓ VdW



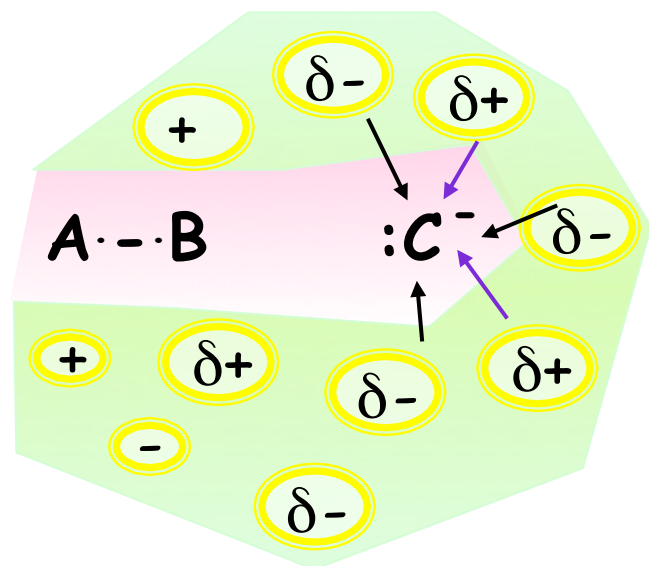
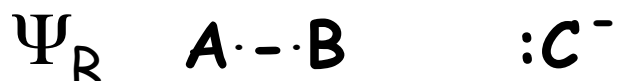
HOW?

- ✚ VdW - classically
- ✚ **Electrostatic:**
Mechanical embedding each VB structure
→ Wavefunction polarization (electrostatic embedding)

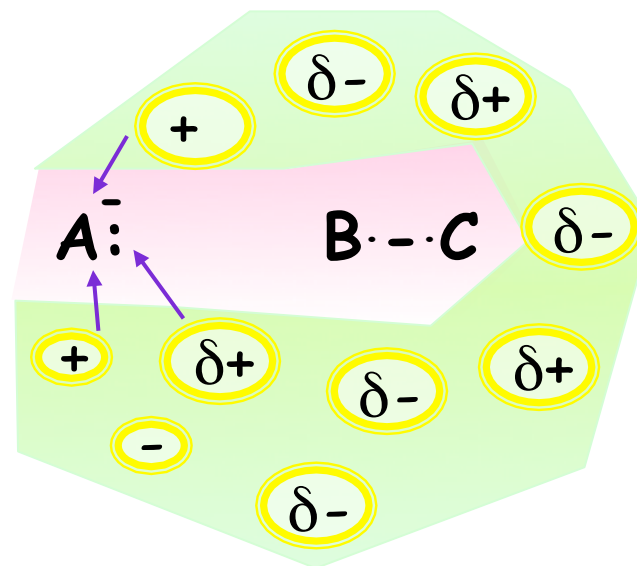


ab initio VB/MM

VB structures - Electron localization



Less



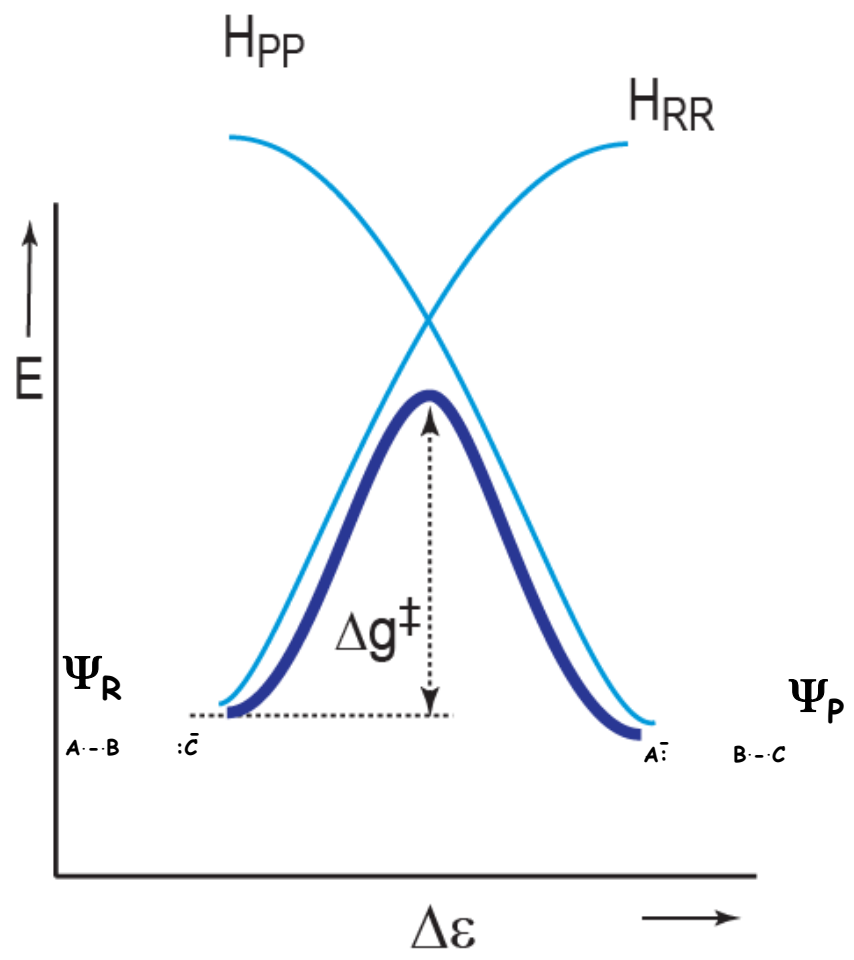
More

Stabilization

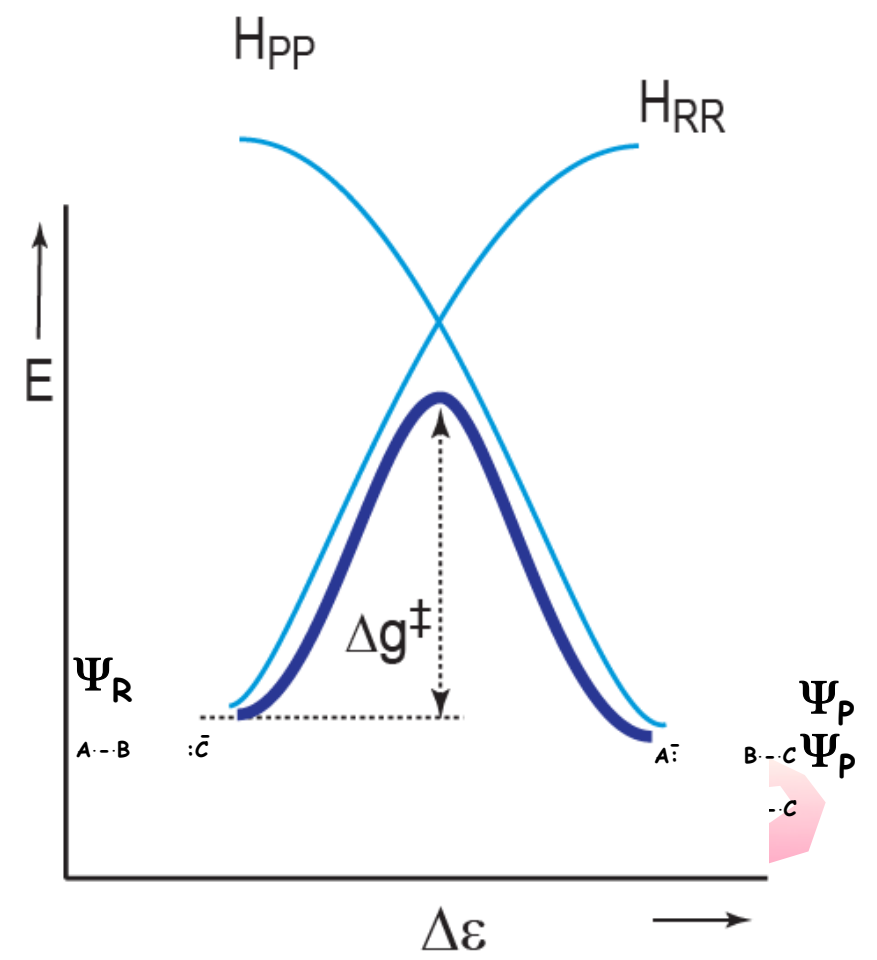
$$\Psi_{\text{Total}} = c_R \Psi_R + c_P \Psi_P$$

Mechanical Embedding with each VB structure separately should include most of the wavefunction polarization.

Gas



Protein



ab initio VB/MM

$$H_{VB/MM} = H(VB) + H(MM) + H(VB/MM)$$

H_{ii} is the diabatic state energy:

$$H_{ii} = H_{ii}(VB) + H_{ii}^{\text{int}} + \left[H(MM) \right]$$

H_{ii}^{int} is calculated classically

How to calculate H_{ij} ?

Assumption: Both overlap S_{ij} and reduced resonance integral, β_{ij} , are invariant to the environment.

$$\beta_{ij}^{\text{gas}} = \beta_{ij}^{\text{env}} \quad S_{ij}^{\text{gas}} = S_{ij}^{\text{env}}$$

$$\beta_{ij} = H_{ij} - \frac{1}{2}(H_{ii} + H_{jj})S_{ij}$$

$$H_{ij} = H_{ij}^0(VB) + \frac{1}{2}(H_{ii}^{\text{int}} + H_{jj}^{\text{int}})S_{ij}$$

*Solve new matrix,
Get new wavefunction*

This formula will serve also in the general case

ab initio VB/MM

New matrix is solved:

$$\begin{pmatrix} H_{11}^0 + H_{11}^{\text{int}} & H_{12}^0 + \frac{1}{2} (H_{11}^{\text{int}} + H_{22}^{\text{int}}) S_{12} \\ H_{21}^0 + \frac{1}{2} (H_{11}^{\text{int}} + H_{22}^{\text{int}}) S_{21} & H_{22}^0 + H_{22}^{\text{int}} \end{pmatrix}$$

New wavefunction, and energy are obtained:

$$E_{\text{total}} = E + H^0(\text{MM})$$

Relax the environment accordingly and repeat

Finally, for the reaction profile:

use potential of mean force (PMF) combined with FEP/US

ab initio VB/MM

Finally ...

The *ab initio* VB calculations of the reactive fragments utilized the program **XMVB**:

Lingchun Song, Wei Wu, Yirong Mo, Qianer Zhang, **XMVB** - an *ab initio* Non-orthogonal Valence Bond Program, Center of Theoretical Chemistry, Department of Chemistry, and State Key Laboratory for Physical Chemistry of Solid Surfaces, Xiamen University, Xiamen Fujian 36005, China.

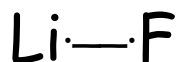
The MM calculations as well as dynamics utilized the **MOLARIS** program with the **ENZYMIX** force-field:

Microscopic and Semimicroscopic Calculations of Electrostatic Energies in Proteins by the POLARIS and ENZYMIX Programs, F. S. Lee, Z. T. Chu, and A. Warshel, *J. Comp. Chem.* 14, 161 (1993).

Results: Li-F

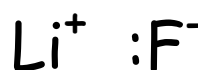
VB Structures:

Φ_{COV}



;

Φ_{ION}



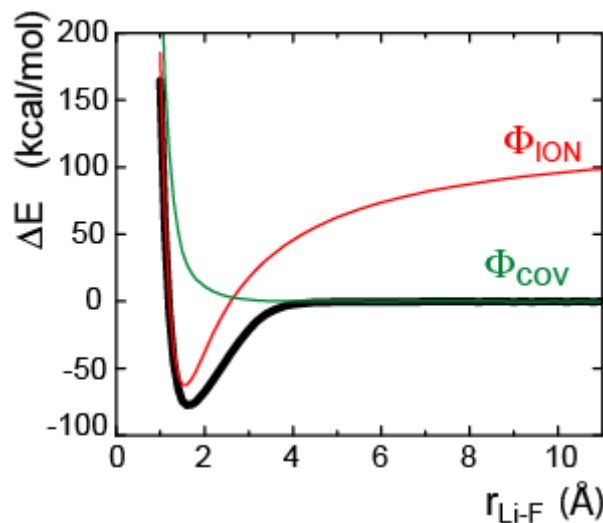
;

~~Φ_{ION}~~

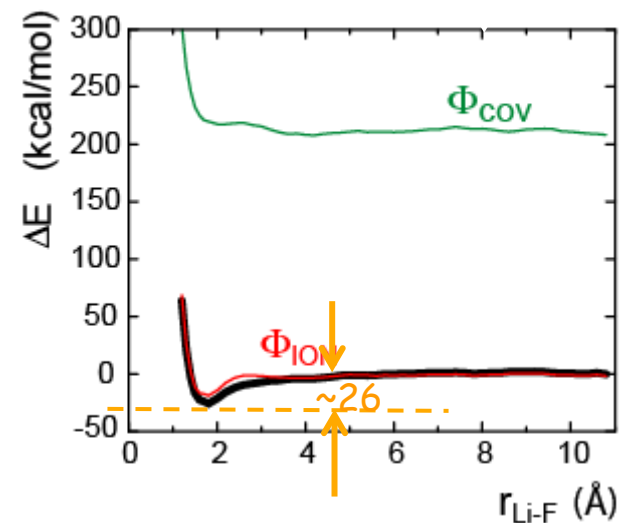


Energy Curves

Gas Phase



Solution



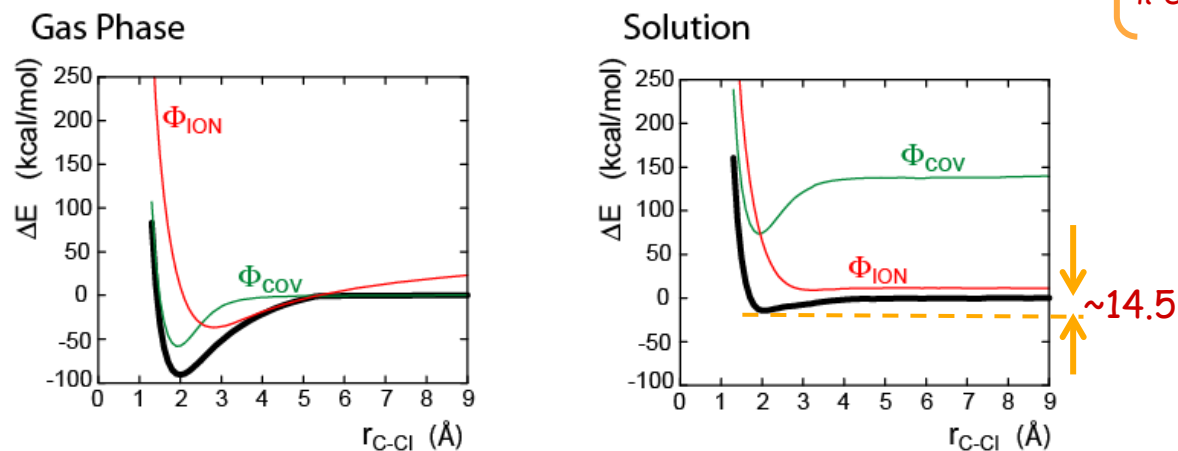
(6-31G* basis set
1S electrons frozen)

- ✚ correct description of dissociation into ions in solution
- ✚ Predicted dissociation of barrier ~26 kcal/mol (exp. ~5 kcal/mol)

Results: Tertiary-Butyl Chloride (*t*-BuCl)

6-31G basis set
 π electrons frozen

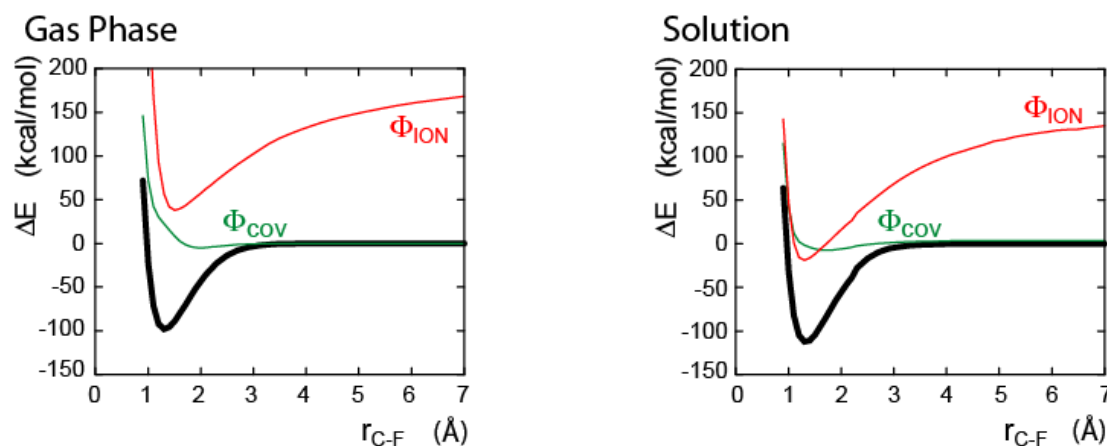
Energy Curves



- ⚡ Dissociation into: radicals - vacuum vs ions - solution
- ⚡ Predicted dissociation barrier of ~ 14.5 kcal/mol (Exp. ~ 19.5 kcal/mol)

Results: CH_3-F

Energy Curves



- ⚡ Homolytic dissociation in both vacuum and solution
- ⚡ Most of the bond energy comes from resonance

6-31G* basis set
Core electrons frozen

ab initio DE-VB/MM

Environment partial charges are included in the quantum Hamiltonian:

No need for the assumption regarding the overlap and the reduced resonance in case of an electrostatic environment:

$$\beta_{ij}^{gas} = \beta_{ij}^{env} = S_{ij}^{gas} = S_{ij}^{env}$$

New matrix is solved:

$$\begin{pmatrix} (H_{11}^0)' & (H_{12}^0)' \\ (H_{21}^0)' & (H_{22}^0)' \end{pmatrix}$$

New wavefunction, and energy are obtained:

$$E_{total} = E + H^O(MM)$$

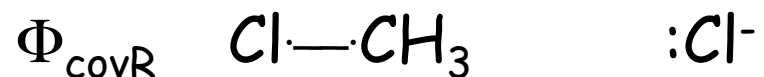
Relax the environment accordingly and repeat

Use of potential of mean force PMF

Results: Identity S_N2 Reaction

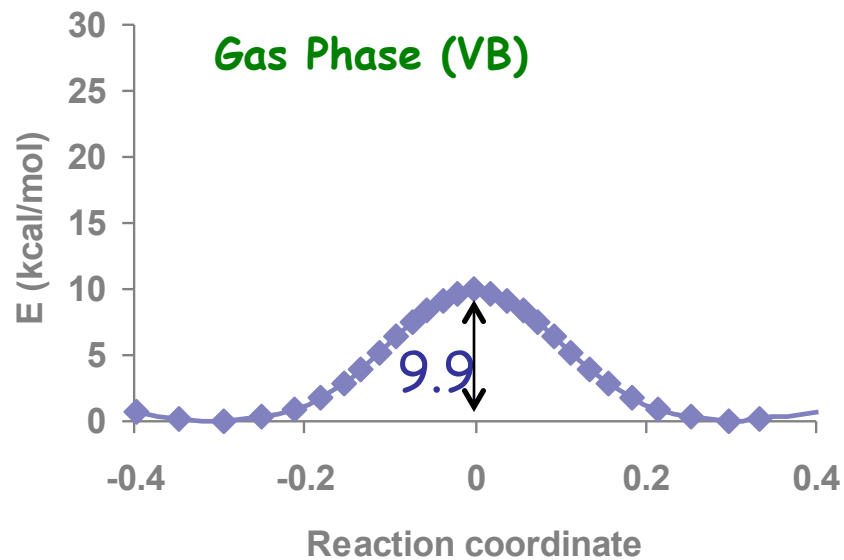


Important VB Structures:



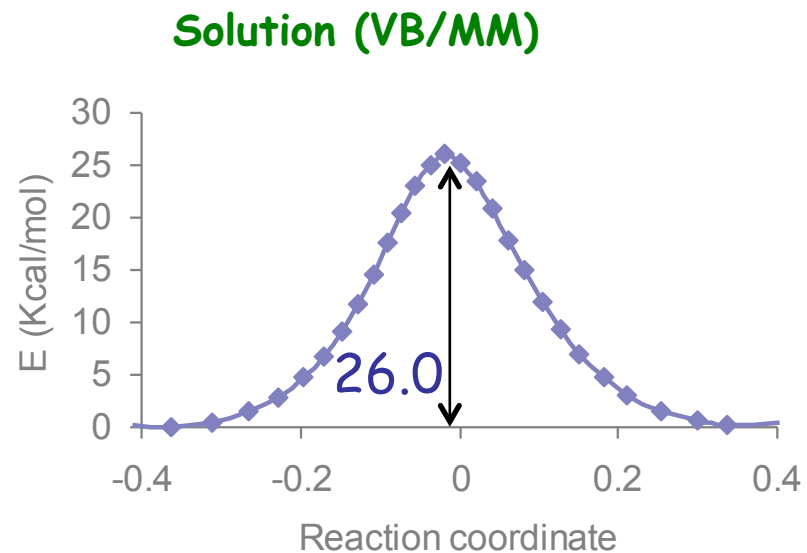
Use both VB/MM and DE-VB/MM

BOVB
6-31G* basis set
Core+ π electrons frozen



Experimental
Gas ~10.2
Solution ~26.6

*VB/MM predicts correctly
the energetics*



ab initio VB/MM

Mechanical Embedding

H_{ii}^{int} is calculated classically

$$\begin{pmatrix} H_{11}^0 + H_{11}^{\text{int}} & H_{12}^0 + \frac{1}{2} (H_{11}^{\text{int}} + H_{22}^{\text{int}}) S_{12} \\ H_{21}^0 + \frac{1}{2} (H_{11}^{\text{int}} + H_{22}^{\text{int}}) S_{21} & H_{22}^0 + H_{22}^{\text{int}} \end{pmatrix}$$

Requires the approximations: $\beta_{ij}^{\text{gas}} = \beta_{ij}^{\text{env}}$ $S_{ij}^{\text{gas}} = S_{ij}^{\text{env}}$

ab initio DE-VB/MM

Wavefunction Polarization

Environment partial charges are included in the quantum Hamiltonian:

H_{ii}^{int} is included in the quantum Hamiltonian

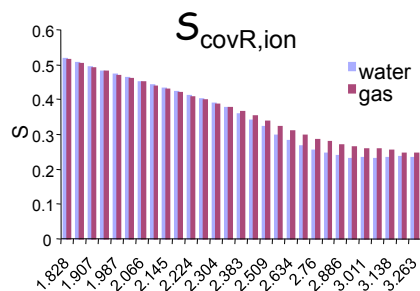
$$\begin{pmatrix} (H_{11}^0)' & (H_{12}^0)' \\ (H_{21}^0)' & (H_{22}^0)' \end{pmatrix}$$

in case of an electrostatic environment:

$$\beta_{ij}^{\text{gas}} = \beta_{ij}^{\text{env}} \quad S_{ij}^{\text{gas}} = S_{ij}^{\text{env}}$$

No Need!

Examination of approximations regarding S_{ij} and β_{ij}



TS geometry (2.38Å)

| | Gas | VB/MM | DE-VB/MM |
|-----------------|---------|-------------|----------|
| | overlap | | |
| $S_{covR,covP}$ | 0.124 | Same as gas | 0.118 |
| $S_{covR,ion}$ | 0.376 | | 0.359 |
| $S_{covP,ion}$ | 0.349 | | 0.359 |

Sharir-Ivry, Shurki, JPC B
2008, 112, 12491

- Changes in overlap and reduced resonance are negligible
- The trends in the weights are kept, VB/MM sufficient for wavefunction polarization

The approximations in VB/MM seem reasonable

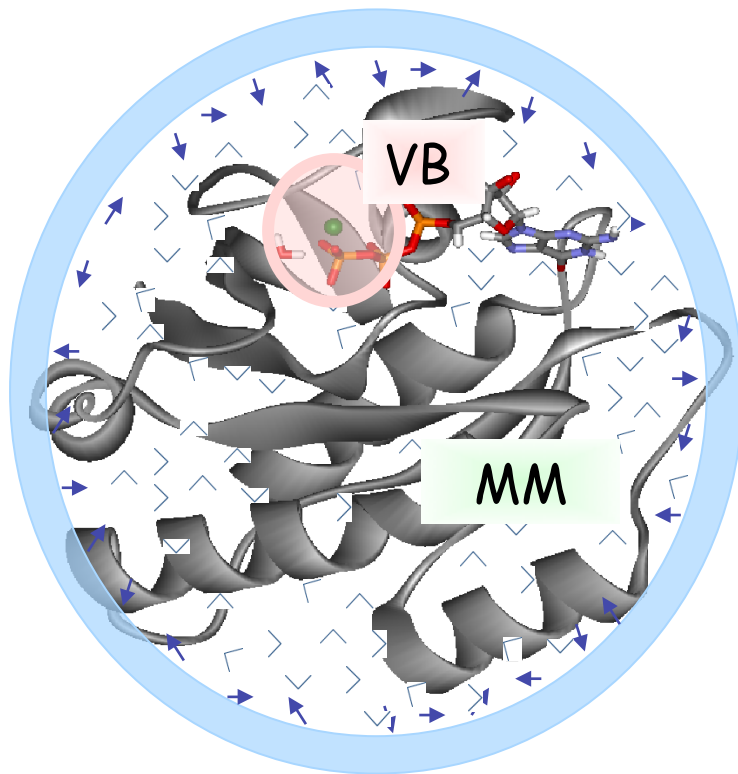
ab initio VB/MM

$$H_{VB/MM} = H(VB) + H(MM) + H(VB/MM)$$

Bonding

✓ Electrostatic

✓ VdW

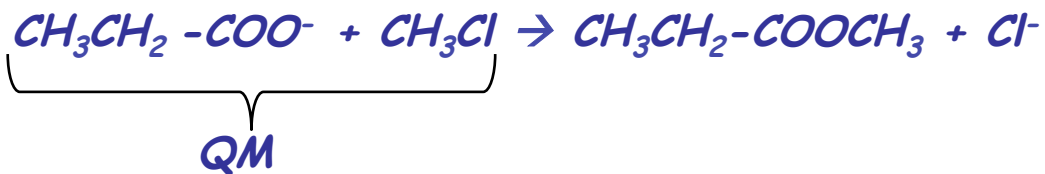


HOW?

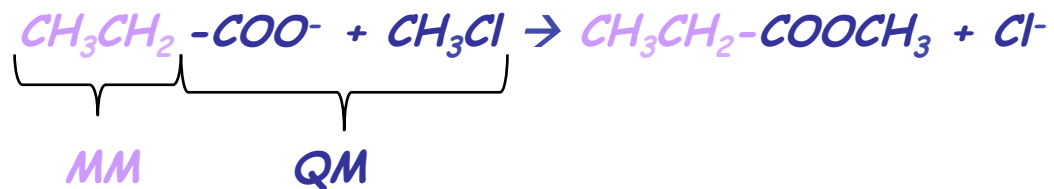
- ✚ VdW - classically
- ✚ Electrostatic:
 - Mechanical embedding each VB structure
 - Wavefunction polarization (electrostatic embedding)
- ✚ Bonding - link atom scheme

Link Atom Scheme

Full treatment



Link atom treatment



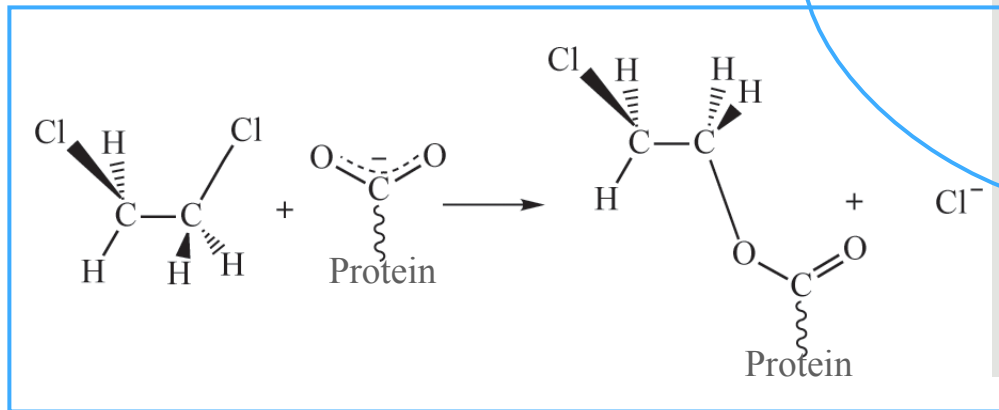
Reaction barriers (kcal/mol)

| | ΔG_g^\ddagger | ΔG_w^\ddagger |
|---------------------|-----------------------|-----------------------|
| Full treatment | 11.9 | 18.2 |
| Link atom treatment | 11.5 | 18.7 |

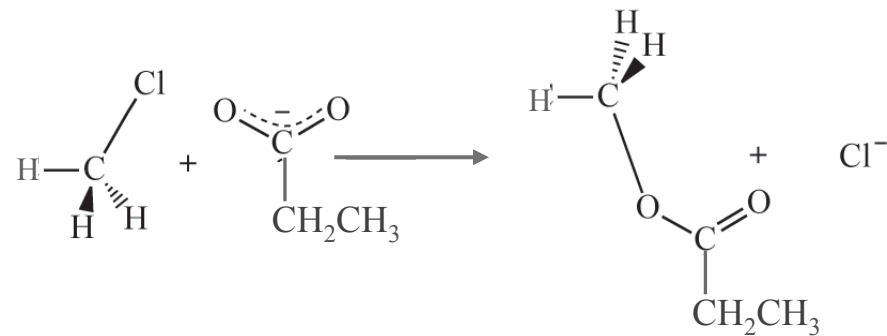
Barriers are similar for the two treatments
Link atom treatment is suitable

Link Atom Scheme

haloalkane dehalogenase (DhIA)



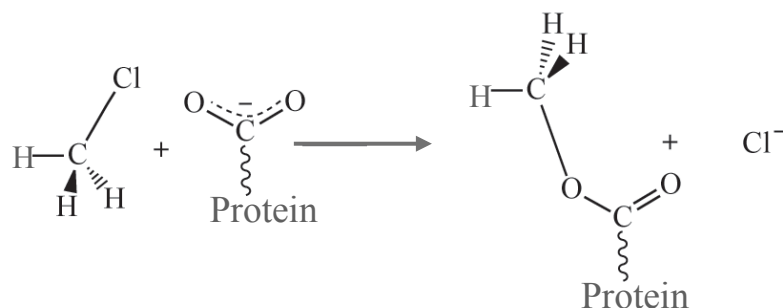
Our Model System



haloalkane dehalogenase (Dh1A)



Our Model System of the Reactive Part



L-VBSCF
6-31G* basis set
Core+ π electrons frozen

| | Gas | Water | Protein | |
|-------|---------|----------|------------------|-------|
| Exp | (18-28) | ~ 7 | (<26) ~ -12 | (<15) |
| VBSCF | 13 | 7.1 | 20.1 | -8.9 |

Low barriers (different experimental system and insufficient description of gas phase), yet the overall trend is correct

Solvation Energies (weighted)

| | | Reactants | TS | $\Delta_{(TS-R)}$ | $\Delta\Delta_{(P-W)}$ |
|---------|------|-----------|-----|-------------------|------------------------|
| water | CovR | -54 | -17 | 37 | |
| | Ion | -26 | -49 | -23 | |
| protein | CovR | -54 | -23 | 31 | -6 |
| | Ion | -37 | -61 | -24 | -1 |
| | Tot | | | | -8 |

* Results based on one run and include VdW and intra electrostatic interaction.

- The stabilization in the protein is consistently larger than in water
- Water stabilize CovR in the reactants geometry much more than in the TS - leading to the increased barrier
- This differential stabilization considerably decreases in the protein

Understand mutations

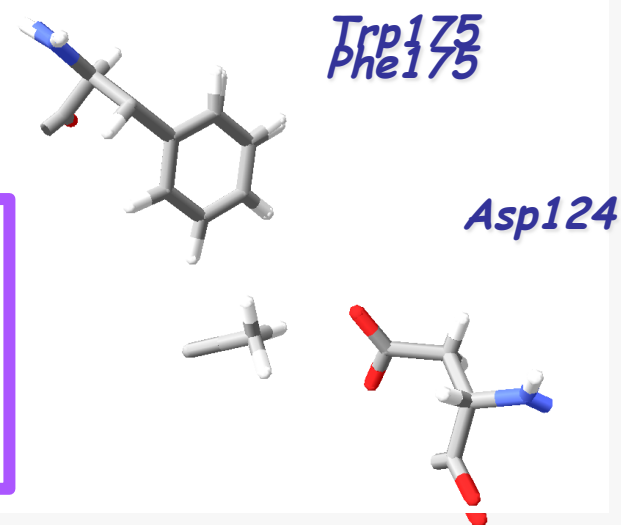
W175F as a case study

Exp

| <u>wt</u> | <u>W175P</u> | |
|-----------|--------------|------|
| Units/mg | 2.9 | 0.28 |

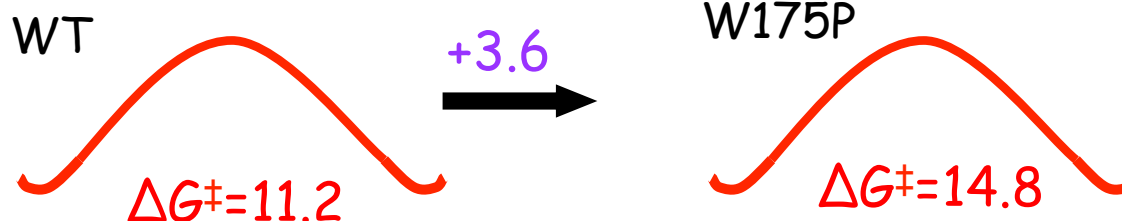
(Data corresponds to di-chloroethane as substrate)

Observed anti-catalytic effect ≥ 3 kcal/mol!

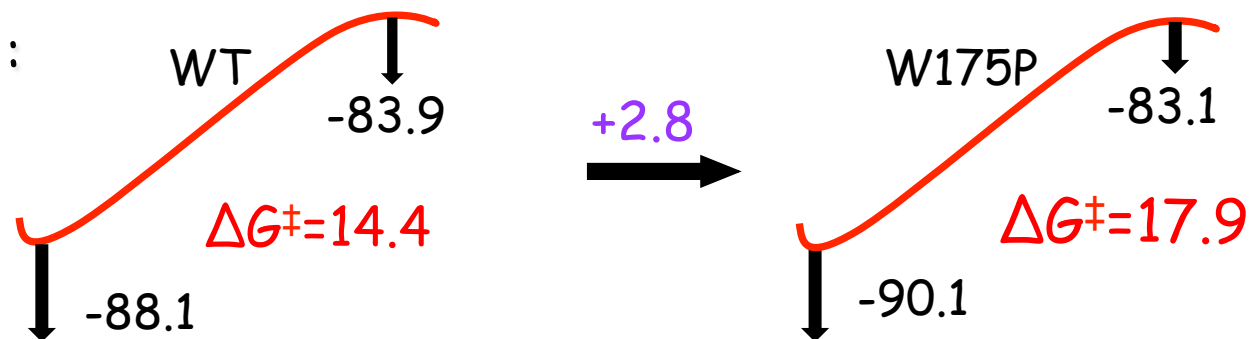


Our calculations:

VB/MM-FEP:



LRA, solvation:



Understand mutations

| <u>Trp175</u> | Φ_{covR} | Φ_{covP} | Φ_{ion} | Φ_{lb} | Tot |
|------------------|---------------|---------------|--------------|-------------|------|
| RS | -0.9 | 0.0 | -2.1 | 0.0 | -3.0 |
| TS | -0.4 | -1.3 | -5.2 | 0.0 | -6.9 |
| catalytic effect | +0.5 | -1.3 | -3.1 | 0.0 | -3.9 |

Trp 175 is catalytic due to better solvation in the TS

The main contribution to this effect comes from the higher TS stabilization of both Φ_{ion} and Φ_{covP}

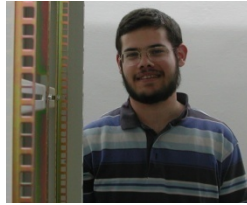
Phe is not polar thus, ionic stabilization is decreased leading to decrease of catalytic effect.

Conclusions

- ✱ Two methods were presented: VB/MM and DE-VB/MM
- ✱ The approximations made for VB/MM were shown to be reasonable
- ✱ Mechanical embedding of each VB structure separately captures most of the environmental effect of wave-function polarization
- ✱ The method allows studies of reactions in solvents as well as enzymes and enables understanding of the effect of mutations on the reaction.

Acknowledgement

Hadar Crown
Avital Sharir-Ivry
Dr. Tamar Shnerb
Dr. Rajapandian V
Moshe Amitay
Tamar Ansbacher
Dr. Hemant Kumar Srivastava



Collaborations:
Prof. Wei Wu

*Interested post-docs are most welcome to the group
to continue with this and other interesting projects*

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Alex Grass Center for Drug Design and Synthesis of Novel Therapeutics

Understand mutations

Anti-catalytic effect of known mutants

| | Calculated $\Delta\Delta g_{wt \rightarrow mut}^{\ddagger(\text{calc})}$ | Observed $\Delta\Delta g_{wt \rightarrow mut}^{\ddagger(\text{obs})}$ |
|-------|---|--|
| wt | 0.0 | 0.0 |
| W125F | 2.3 | ≤ 2.3 |
| V226A | -2.2 | 0.7 |
| W175Y | 5.2 | ≤ 3.0 |
| W175F | 2.8 | ≤ 3.0 |
| N148D | 1.9 | > 2.7 |
| D-Mut | 1.5 | > 2.7 |

Calculated values from LRA using electrostatic

Agreement suggests that electrostatic indeed has a major role in catalysis.

| residue | $\Delta\Delta g_{sol}^{TS-RS}(\psi)$ | $\Delta\Delta g_{sol}^{TS-RS}(\phi_{cov}^R)$ | $\Delta\Delta g_{sol}^{TS-RS}(\phi_{cov}^P)$ | $\Delta\Delta g_{sol}^{TS-RS}(\phi_{ion})$ | $\Delta\Delta g_{sol}^{TS-RS}(\phi_{LB})$ | $\Delta g_{sol}^{RS}(\psi)$ |
|---------|--------------------------------------|--|--|--|---|-----------------------------|
| | Tot-cat | $\bar{\Phi}_{covR}$ | $\bar{\Phi}_{covP}$ | $\bar{\Phi}_{ion}$ | $\bar{\Phi}_{lb}$ | RSsolv |
| W175 | -3.85 | 0.53 | -1.26 | -3.09 | -0.04 | -2.97 |
| W125 | -3.40 | 0.28 | -1.28 | -2.36 | -0.05 | -2.36 |
| V226 | -1.02 | -2.38 | -3.40 | 0.58 | -0.48 | -1.00 |
| H54 | 0.25 | 1.07 | -0.22 | -0.57 | -0.02 | -2.77 |

- VB analysis provides better understanding of the effects.
- without structural interference, dominant VB contribution remains also in the mutant.

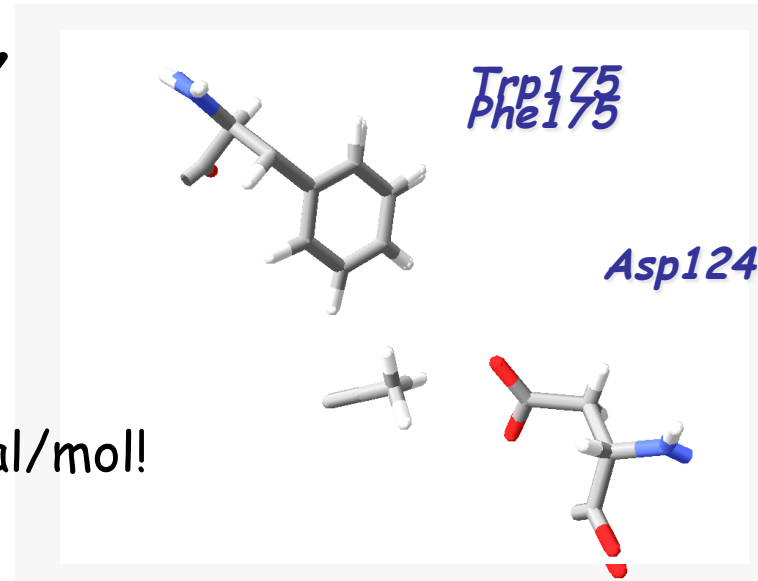
Understand mutations

W175F as a case study

| Units/mg | <u>WT</u> | <u>W175P</u> |
|----------|-----------|--------------|
| | 2.9 | 0.28 |

(The data refers to the case of di-chloroethane as substrate)

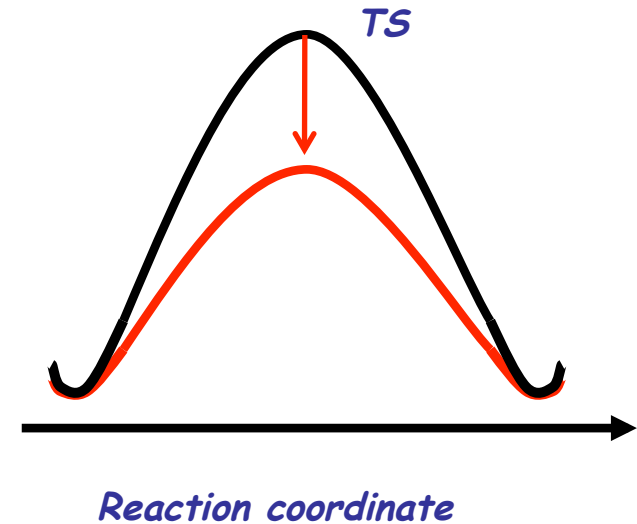
Observed anti-catalytic effect ≤ 2.3 kcal/mol!



Reverse direction: W175F \rightarrow wt

We can now turn to study the specific contributions of residue 175!

Enzyme Design



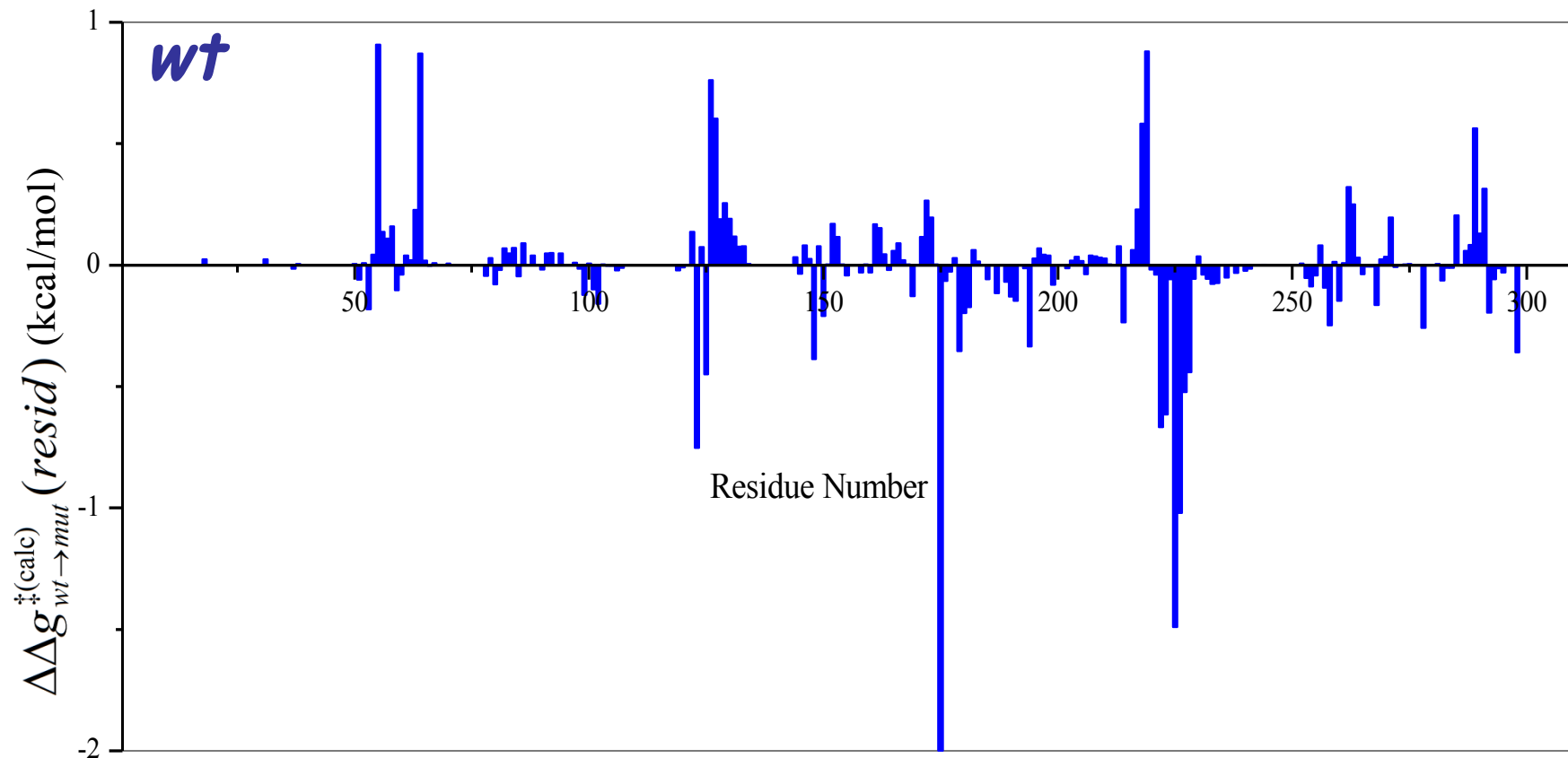
*The challenge:
computational based enzyme design!*

*If electrostatics is important for catalysis
→ Identification of hot spots*

Valence bond provides added insights

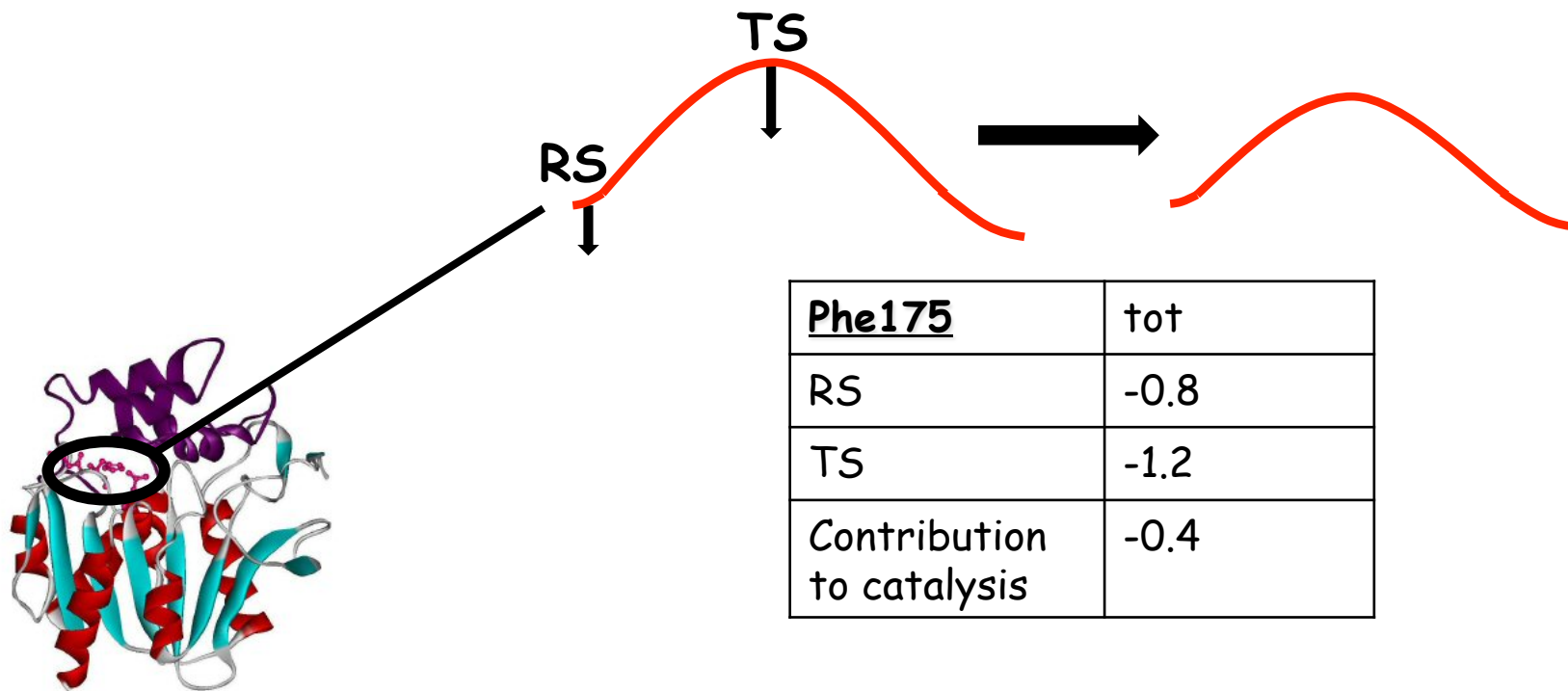
Scheme Validation

Contribution to differential solvation of particular residues



1. Classify the residue as catalytic, anti-catalytic or non-catalytic

Identify the residue's contribution to the solvation of the substrate in both RS and TS using LRA

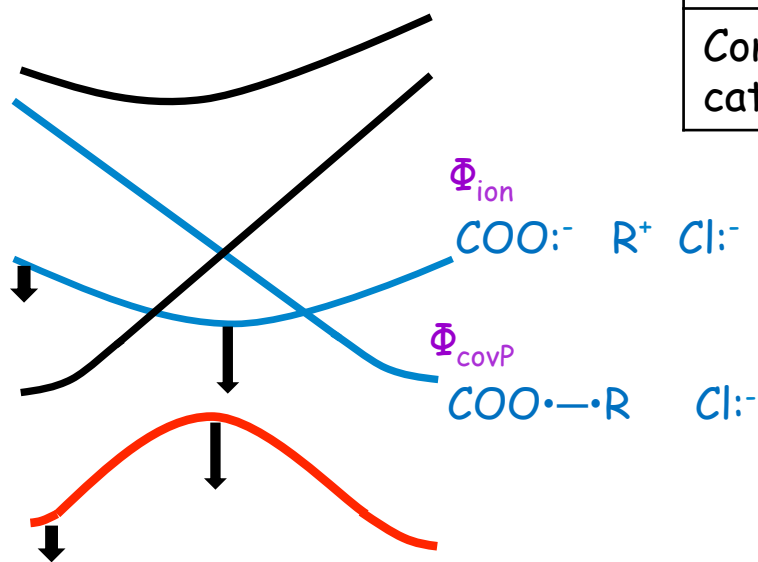


Phe 175 is slightly catalytic due to better solvation in the TS

2. Understand the origin of this catalytic effect

- i. By decomposing the effect into the contributions from the various VB structures!
- ii. Identify the VB structures that govern the overall effect.

| <u>Phe175</u> | Φ_{covR} | Φ_{covP} | Φ_{ion} | Φ_{lb} | Tot |
|---------------------------|---------------|---------------|--------------|-------------|-------------|
| RS | -0.3 | 0.0 | -0.5 | 0.0 | -0.8 |
| TS | -0.1 | -0.2 | -0.9 | 0.0 | -1.2 |
| Contribution to catalysis | +0.2 | -0.2 | -0.4 | 0.0 | -0.4 |



The main contribution to this effect comes from the higher TS stabilization of both Φ_{ion} and Φ_{covP}

Understand mutations

enhance ionic stabilization by increasing the residue polarity in the right direction - wt (W175)

| <u>Trp175</u> | Φ_{covR} | Φ_{covP} | Φ_{ion} | Φ_{lb} | Tot |
|------------------|----------------------|----------------------|---------------------|--------------------|------|
| RS | -0.9 | 0.0 | -1.6 | 0.0 | -2.5 |
| TS | -0.3 | -1.1 | -4.3 | 0.0 | -5.7 |
| catalytic effect | +0.6 | -1.1 | -2.7 | 0.0 | -3.2 |

Effect of Φ_{ion} and Φ_{covP} increased and is still dominant

The main contribution to this effect comes from the higher TS stabilization of both Φ_{ion} and Φ_{covP}

3. *Understand/suggest mutations:*

- a. enhance the effects of the leading VB structures if these are catalytic
- b. decrease/change if it is anti-catalytic!

enhance ionic stabilization by increasing the residue polarity in the right direction - wt (W175)

| <u>Trp175</u> | Φ_{covR} | Φ_{covP} | Φ_{ion} | Φ_{lb} | Tot |
|------------------|---------------|---------------|--------------|-------------|------|
| RS | -0.9 | 0.0 | -1.6 | 0.0 | -2.5 |
| TS | -0.3 | -1.1 | -4.3 | 0.0 | -5.7 |
| catalytic effect | +0.6 | -1.1 | -2.7 | 0.0 | -3.2 |

Effect of Φ_{ion} and Φ_{covP} increased and is still dominant

| residue | $\Delta\Delta g_{sol}^{TS-RS}(\psi)$ | $\Delta\Delta g_{sol}^{TS-RS}(\phi_{cov}^R)$ | $\Delta\Delta g_{sol}^{TS-RS}(\phi_{cov}^P)$ | $\Delta\Delta g_{sol}^{TS-RS}(\phi_{ion})$ | $\Delta\Delta g_{sol}^{TS-RS}(\phi_{LB})$ | $\Delta g_{sol}^{RS}(\psi)$ |
|---------|--------------------------------------|--|--|--|---|-----------------------------|
| | Tot-cat | Φ_{covR} | Φ_{covP} | Φ_{ion} | Φ_{lb} | RSsolv |
| W175 | -3.85 | 0.53 | -1.26 | -3.09 | -0.04 | -2.97 |
| F175 | -0.47 | 0.06 | -0.14 | -0.38 | 0.00 | -0.50 |
| Y175 | -3.05 | -0.26 | -0.71 | -2.03 | -0.06 | -0.99 |
| W125 | -3.40 | 0.28 | -1.28 | -2.36 | -0.05 | -2.36 |
| F125 | -0.43 | 0.34 | -0.23 | -0.53 | -0.01 | -1.03 |
| | | | | | | |
| V226 | -1.02 | -2.38 | -3.40 | 0.58 | -0.48 | -1.00 |
| A226 | -1.04 | -2.39 | -3.43 | 0.56 | -0.60 | -0.98 |
| H54 | 0.25 | 1.07 | -0.22 | -0.57 | -0.02 | -2.77 |
| N54 | -1.01 | -2.76 | 0.02 | 1.72 | 0.00 | 7.36 |

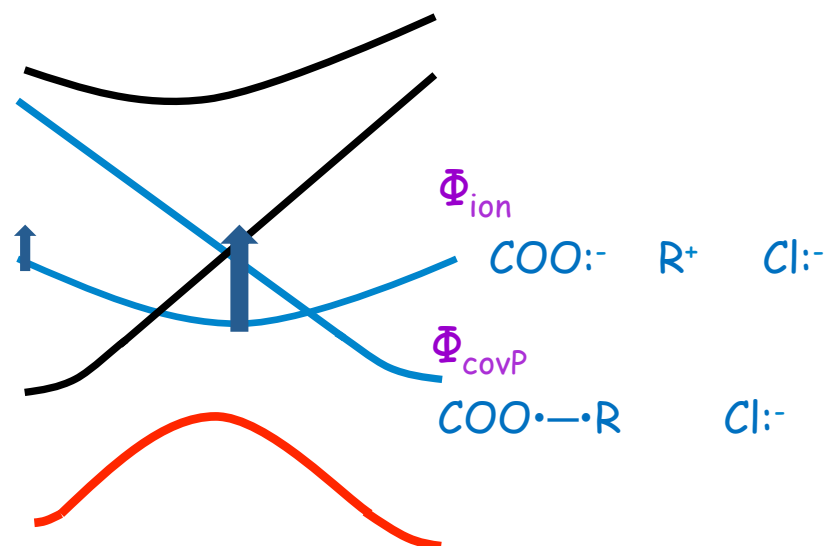
- VB analysis provides better understanding of the effects.
- without structural interference, dominant VB contribution remains also in the mutant.

Prediction Glu56

1. classify

| | |
|------------------|-------|
| | Glu56 |
| RS | +2.3 |
| TS | +2.5 |
| catalytic effect | +0.2 |

Glu56 is slightly anti-catalytic



2. analyze, understand

| <u>Glu56</u> | Φ_{covR} | Φ_{covP} | Φ_{ion} | Φ_{Ib} | Tot |
|------------------|----------------------|----------------------|---------------------|--------------------|-------------|
| RS | +1.3 | 0.0 | +1.0 | 0.0 | +2.3 |
| TS | +0.5 | +0.3 | +1.7 | 0.0 | +2.5 |
| catalytic effect | -0.8 | +0.3 | +0.7 | 0.0 | +0.2 |

The main contribution to this effect is higher destabilization of Φ_{covP} and Φ_{ion} in the TS

Prediction Glu56Gln

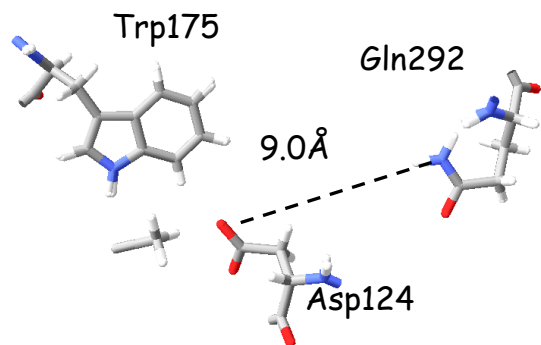
4. Suggest a mutation that will reduce and maybe even turn this destabilization interaction into stabilization, by e.g., removing the negative charge

| <u>Gln56</u> | Φ_{covR} | Φ_{covP} | Φ_{ion} | Φ_{lb} | Tot |
|------------------|----------------------|----------------------|---------------------|--------------------|-------------|
| RS | -1.7 | -0.1 | -2.5 | 0.0 | -4.3 |
| TS | -0.6 | -1.2 | -4.0 | 0.0 | -5.8 |
| catalytic effect | +1.1 | -1.1 | -1.5 | -0.0 | -1.5 |

LRA calculations indeed predict catalytic trend,

with $\Delta\Delta g_{wt \rightarrow mut}^{\ddagger(\text{calc})} = -6.5$

Prediction Gln292



1. classify

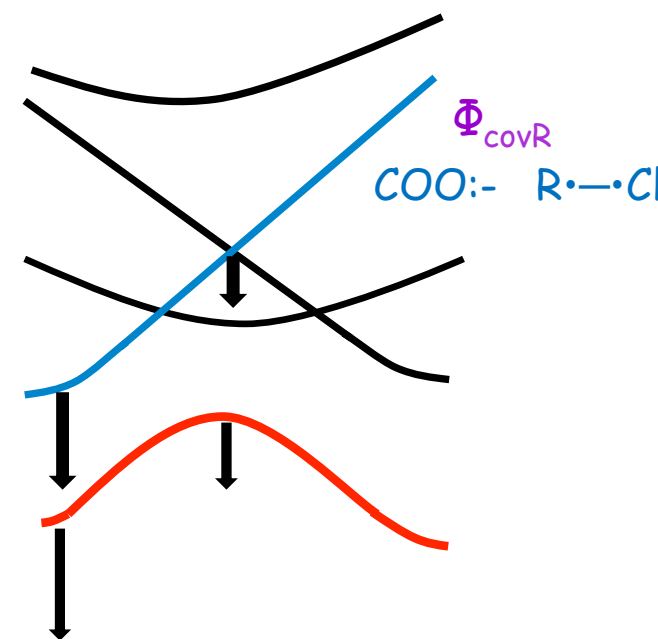
| | |
|------------------|--------|
| | Gln292 |
| RS | -1.9 |
| TS | -1.2 |
| catalytic effect | +0.7 |

Gln 292 is slightly anti-catalytic

2. analyze, understand

| <u>Gln292</u> | Φ_{covR} | Φ_{covP} | Φ_{ion} | Φ_{lb} | Tot |
|------------------|---------------|---------------|--------------|-------------|-------------|
| RS | -1.2 | 0.0 | -0.7 | 0.0 | -1.9 |
| TS | -0.3 | -0.1 | -0.8 | 0.0 | -1.2 |
| catalytic effect | +0.9 | -0.1 | -0.1 | 0.0 | +0.7 |

The main contribution to this effect is higher stabilization of Φ_{covR} in the RS

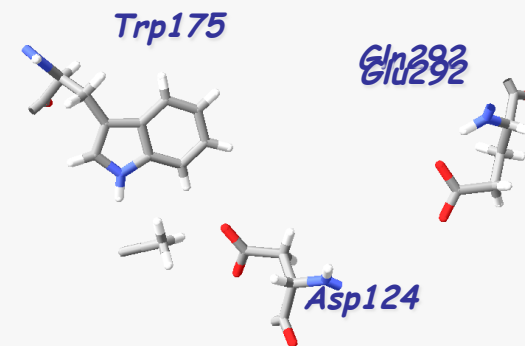


Prediction Gln292

4. Suggest a mutation that will destabilize Φ_{covR} by e.g., introducing negative charge



| <u>Glu292</u> | Φ_{covR} | Φ_{covP} | Φ_{ion} | Φ_{lb} | Tot |
|------------------|---------------|---------------|--------------|-------------|-------|
| RS | +12.7 | 0.0 | +8.0 | 0.0 | +20.7 |
| TS | +4.4 | +1.9 | +4.0 | 0.2 | +18.5 |
| catalytic effect | -8.3 | +1.9 | +4.0 | 0.2 | -2.2 |

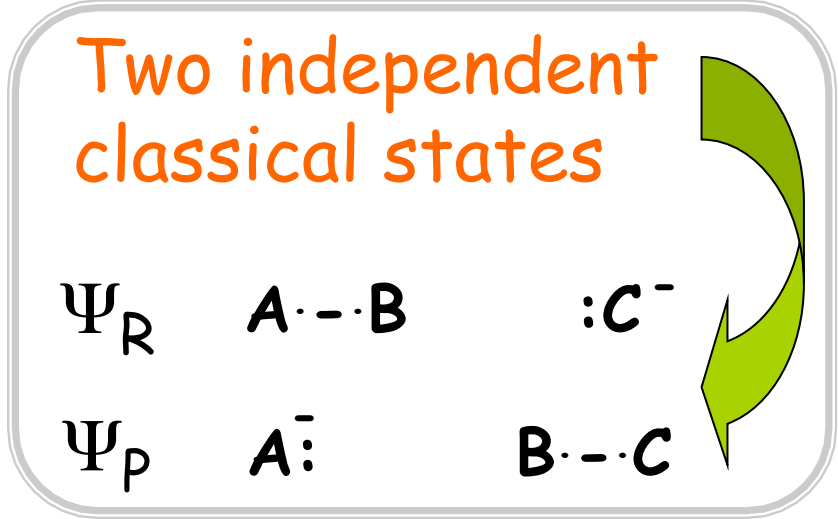
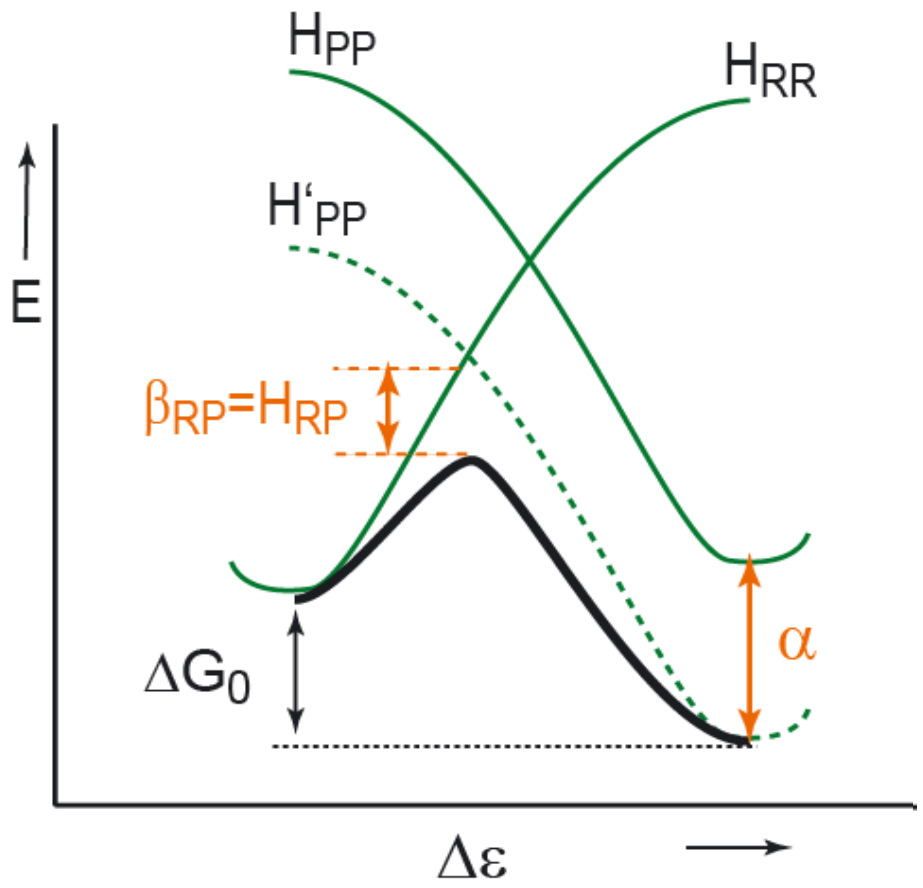


LRA calculations indeed predict catalytic trend,

with $\Delta\Delta g_{wt \rightarrow mut}^{\ddagger(\text{calc})} = -1.0$

| | Calculated | Observed |
|---------------------------|---|--|
| | $\Delta\Delta g_{wt \rightarrow mut}^{\ddagger(\text{calc})}$ | $\Delta\Delta g_{wt \rightarrow mut}^{\ddagger(\text{obs})}$ |
| <i>wt</i> | 0.0 | 0.0 |
| W125F | 2.3 | ≤ 2.3 |
| V226A | -2.2 | 0.7 |
| W175Y | 5.2 | ≤ 3.0 |
| W175F | 2.8 | ≤ 3.0 |
| N148D | 1.9 | > 2.7 |
| D-Mut | 1.5 | > 2.7 |
| <i>predictions</i> | | |
| H54N | 0.2 | |
| E56Q | -4.4 | |
| Q292E | -1.1 | |

Empirical VB (EVB)



Parameterize

- ☀ QM interactions

Assume

- ☀ Overlap $S_{RP} = \delta_{RP}$

Calibrate

- ☀ Gas phase shift - α
- ☀ Resonance energy

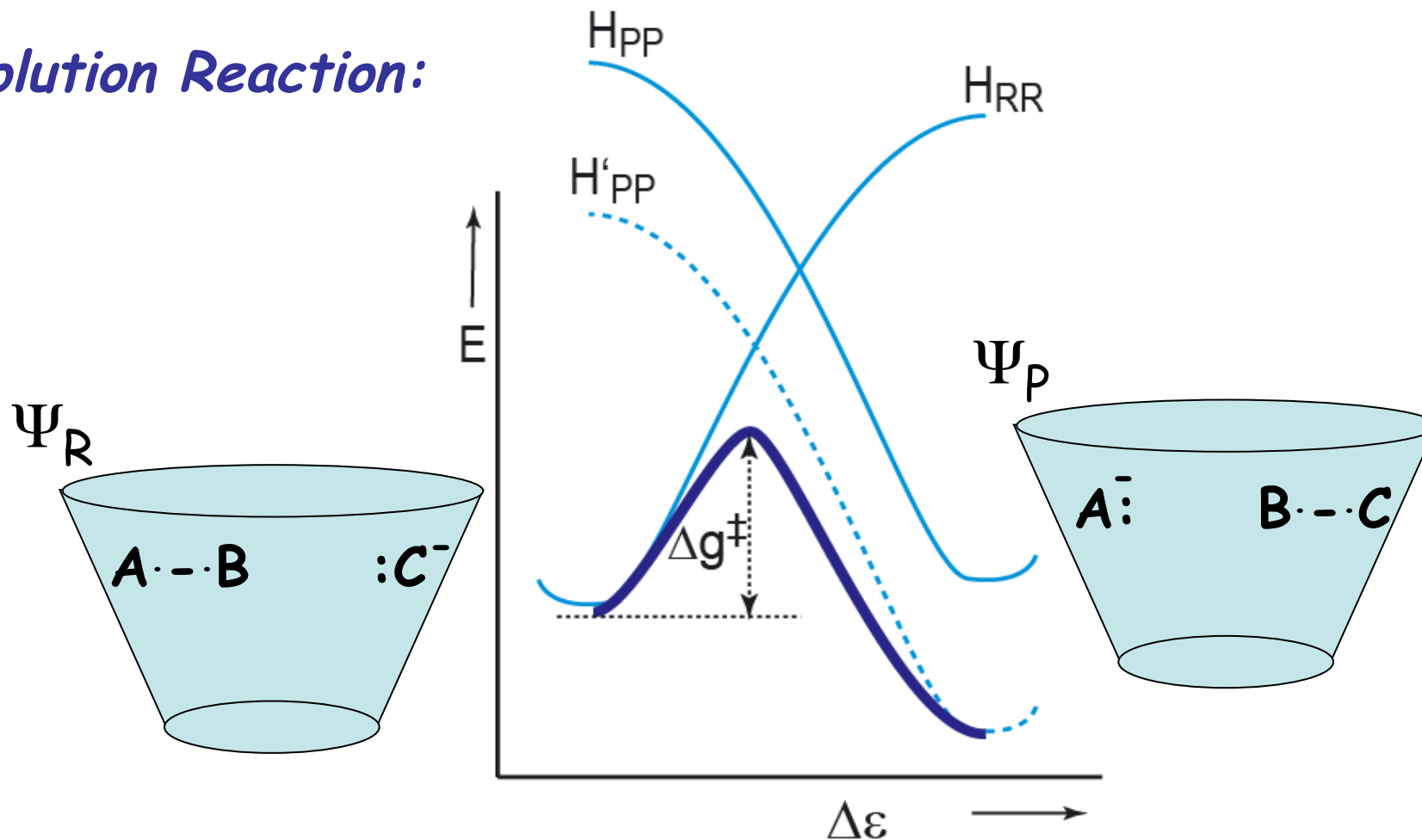
$$H_{RP} = \beta_{RP}$$

What can be studied ?

Empirical VB (EVB) - Comparative Studies

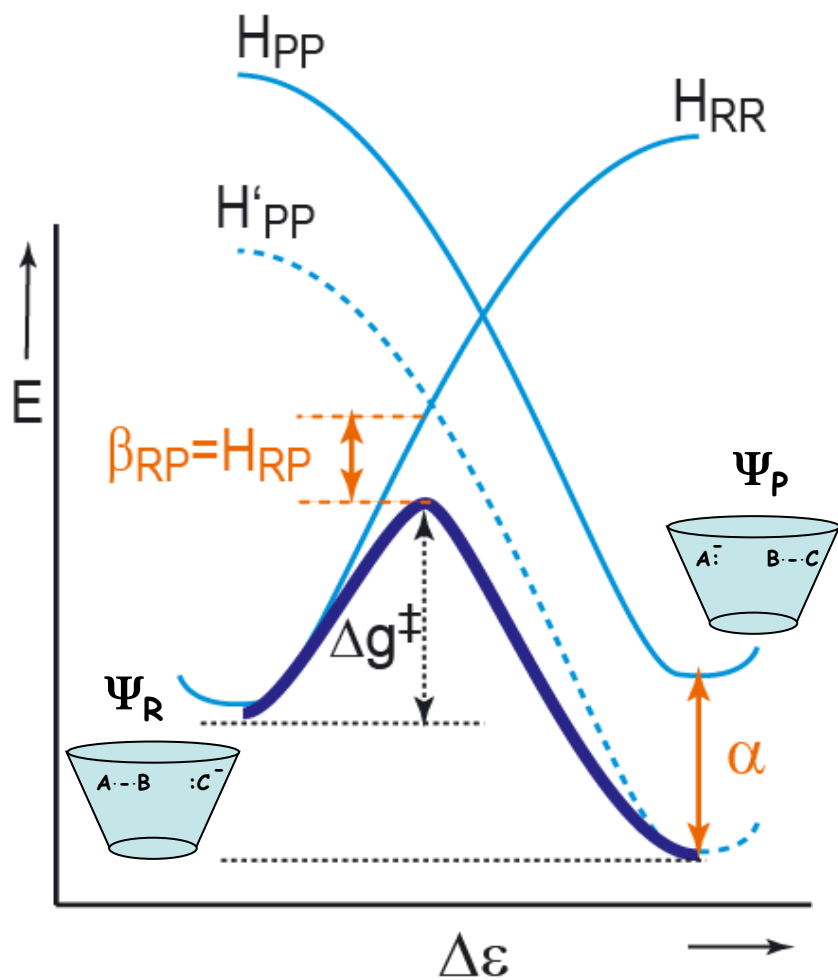
Use same parameters for different environments!

Solution Reaction:

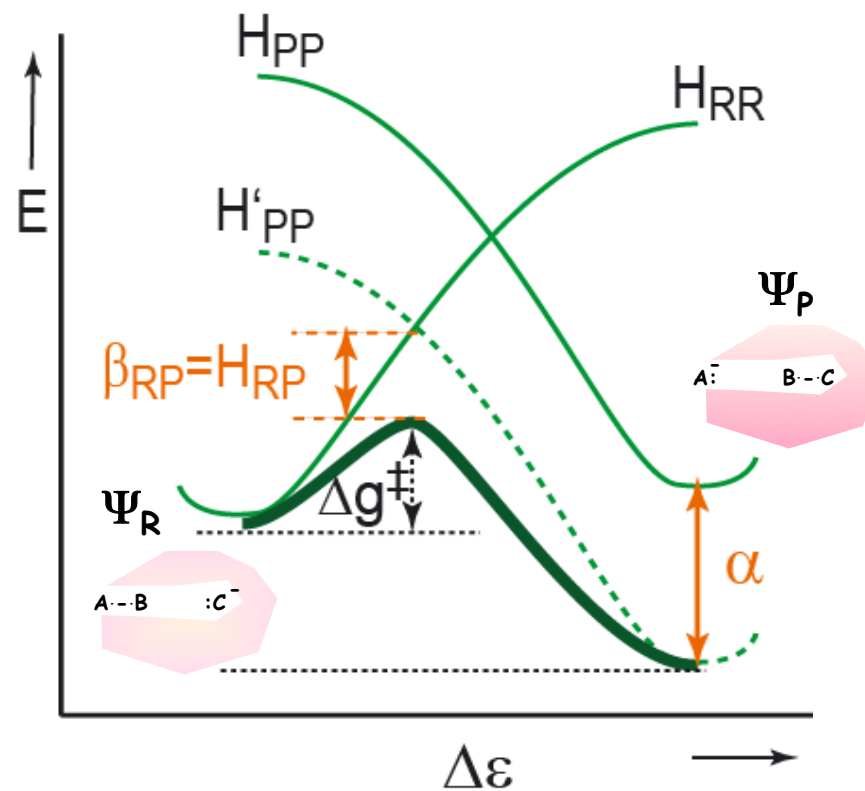


Two classical states which include the environment

Water

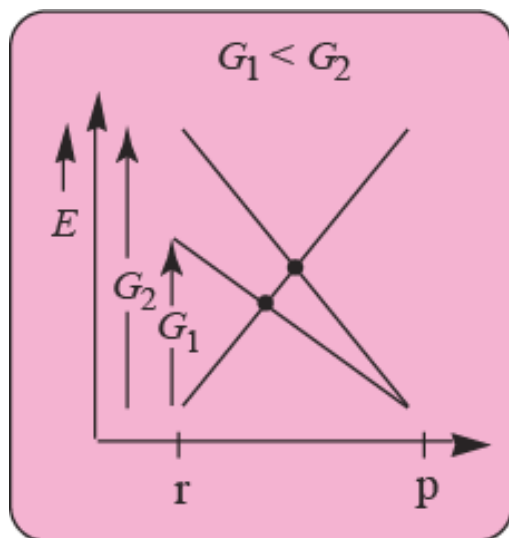


Protein

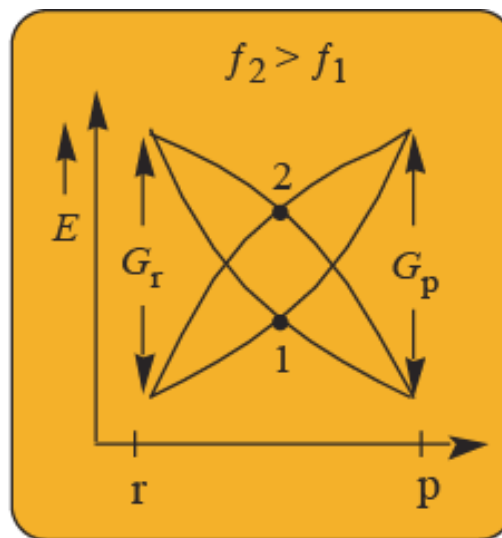


VB State Correlation Diagram (VBSCD)

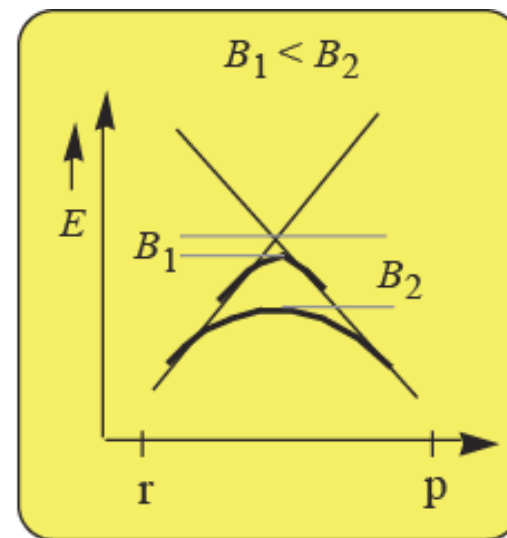
Factors governing reactivity:



$$G = I_{X:-} - A_{R-X}$$



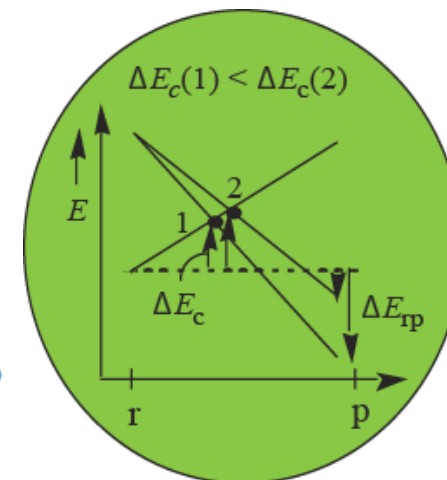
f : delocalization



B : Stereochemistry

$$\Delta E^\ddagger = fG - B$$

$$\Delta E^\ddagger = f_{av}G_r + F(\Delta E_{rp}) - B$$



Ionic contribution

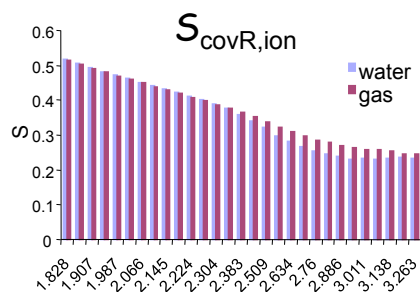
| | Reactants | TS |
|----------|-----------|------|
| Gas | 0.36 | 0.53 |
| Solution | 0.34 | 0.61 |
| Protein | 0.38 | 0.59 |

The protein increased the contribution of the ionic structure in the reactants, increasing delocalization in the reactants and thus reducing the barrier compared to the solution.

Ionic (Reactant's Covalent) contribution

| | Reactants | TS |
|----------|-------------|-------------|
| Gas | 0.36 (0.60) | 0.53 (0.28) |
| Solution | 0.34 (0.65) | 0.61 (0.23) |
| Protein | 0.38 (0.60) | 0.59 (0.26) |

Examination of approximations regarding S_{ij} and β_{ij}

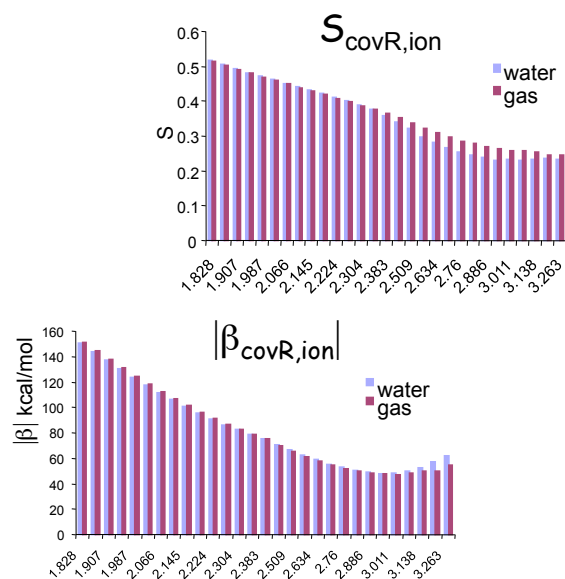


TS geometry (2.38Å)

| | Gas | VB/MM | DE-VB/MM |
|-----------------|----------------|--------------------|----------|
| | <i>overlap</i> | | |
| $S_{covR,covP}$ | 0.124 | <i>Same as gas</i> | 0.118 |
| $S_{covR,ion}$ | 0.376 | | 0.359 |
| $S_{covP,ion}$ | 0.349 | | 0.359 |



Examination of approximations regarding S_{ij} and β_{ij}



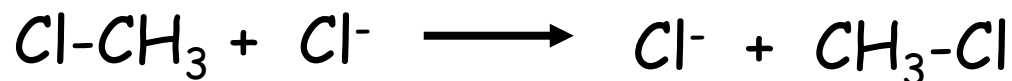
TS geometry (2.38Å)

| | Gas | VB/MM | DE-VB/MM |
|----------------------------|-------|-------------|----------|
| overlap | | | |
| $S_{\text{covR,covP}}$ | 0.124 | Same as gas | 0.118 |
| $S_{\text{covR,ion}}$ | 0.376 | | 0.359 |
| $S_{\text{covP,ion}}$ | 0.349 | | 0.359 |
| Reduced Resonance Integral | | | |
| $\beta_{\text{covR,covP}}$ | -45.9 | Same as gas | -45.1 |
| $\beta_{\text{covR,ion}}$ | -75.4 | | -75.6 |
| $\beta_{\text{covP,ion}}$ | -75.4 | | -75.4 |

- Changes in overlap and reduced resonance are negligible

The approximations in VB/MM seem reasonable

Examination of Wavefunction



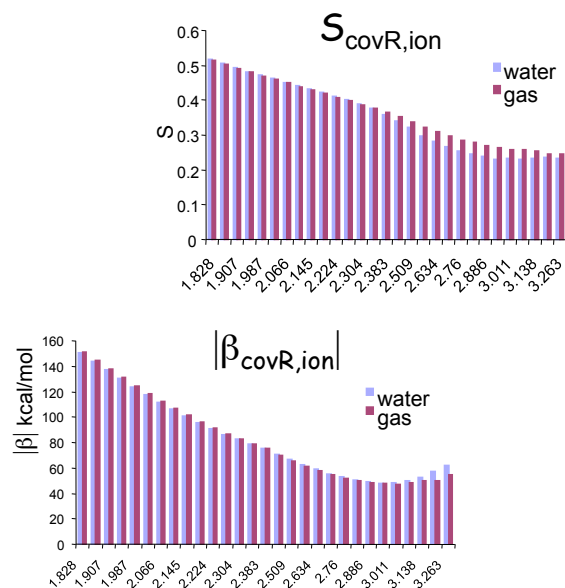
TS geometry (2.38Å)

| | Gas | VB/MM | DE-VB/MM |
|-------------------|-------|-------|----------|
| weights | | | |
| w_{covR} | 0.268 | 0.216 | 0.217 |
| w_{covP} | 0.268 | 0.219 | 0.222 |
| w_{ion} | 0.462 | 0.565 | 0.560 |

Changes in the weights are similar for the two methods

VB/MM seems sufficient to account for most of the wavefunction polarization

Examination of approximations regarding S_{ij} and β_{ij}



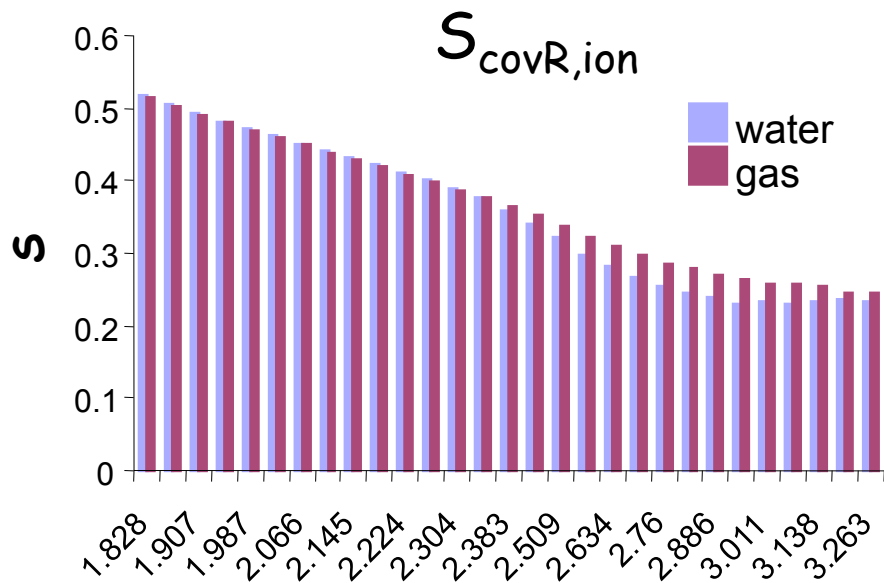
TS geometry (2.38Å)

| | Gas | VB/MM | DE-VB/MM |
|-----------------------------------|-------|--------------------|----------|
| <i>overlap</i> | | | |
| $S_{\text{covR,covP}}$ | 0.124 | <i>Same as gas</i> | 0.118 |
| $S_{\text{covR,ion}}$ | 0.376 | | 0.359 |
| $S_{\text{covP,ion}}$ | 0.349 | | 0.359 |
| <i>Reduced Resonance Integral</i> | | | |
| $\beta_{\text{covR,covP}}$ | -45.9 | <i>Same as gas</i> | -45.1 |
| $\beta_{\text{covR,ion}}$ | -75.4 | | -75.6 |
| $\beta_{\text{covP,ion}}$ | -75.4 | | -75.4 |
| <i>weights</i> | | | |
| φ_{covR} | 0.268 | 0.216 | 0.217 |
| φ_{covP} | 0.268 | 0.219 | 0.222 |
| φ_{ion} | 0.462 | 0.565 | 0.560 |

- Changes in overlap and reduced resonance are negligible
- The trends in the weights is kept

The approximations in VB/MM seem reasonable

Examination of Approximations - overlap

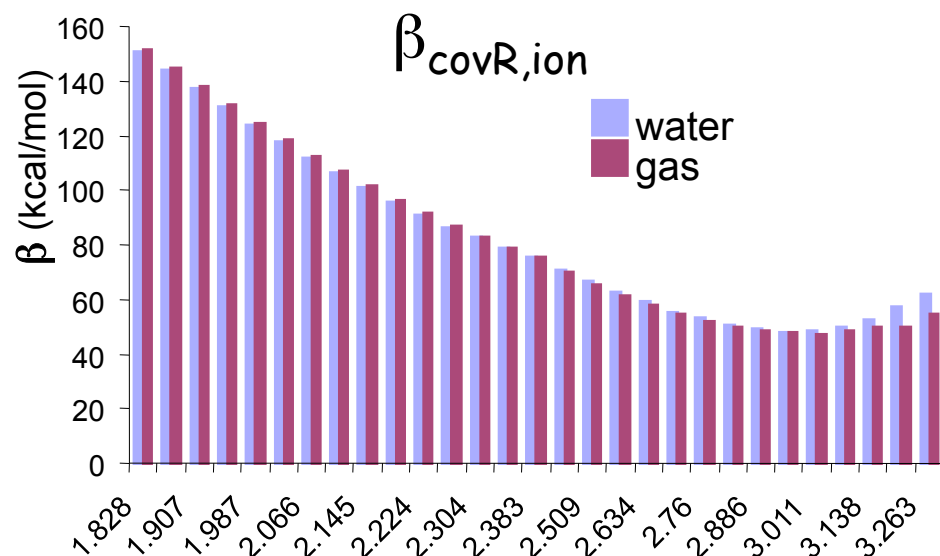
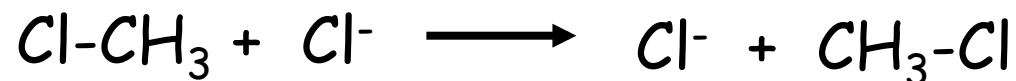


Changes in overlap are negligible

TS geometry (2.38Å)

| | Gas | VB/MM | DE-VB/MM |
|------------------------|--------|--------------------|----------|
| overlap | | | |
| $S_{\text{covR,covP}}$ | 0.124 | <i>Same as gas</i> | 0.118 |
| $S_{\text{covR,ion}}$ | -0.376 | | -0.359 |
| $S_{\text{covP,ion}}$ | -0.349 | | -0.359 |

Examination of Approximations - reduced resonance



Changes in reduced resonance are negligible

TS geometry (2.38 Å)

| | Gas | VB/MM | DE-VB/MM |
|-----------------------------------|-------|--------------------|----------|
| Reduced Resonance Integral | | | |
| $\beta_{\text{covR,covP}}$ | -45.9 | <i>Same as gas</i> | -45.1 |
| $\beta_{\text{covR,ion}}$ | 75.4 | | 75.6 |
| $\beta_{\text{covP,ion}}$ | 75.4 | | 75.4 |

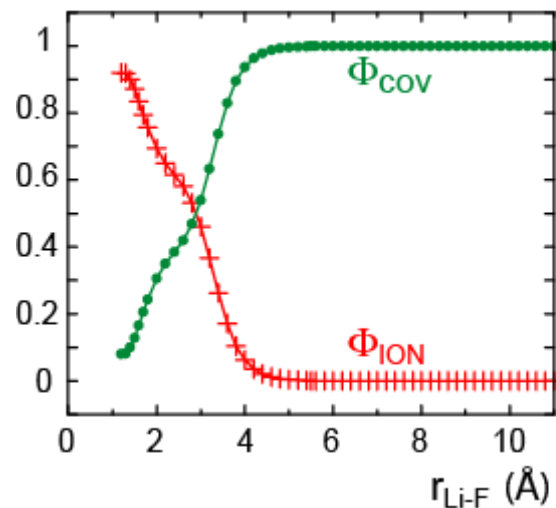
Results: Li-F

Ionic Bond

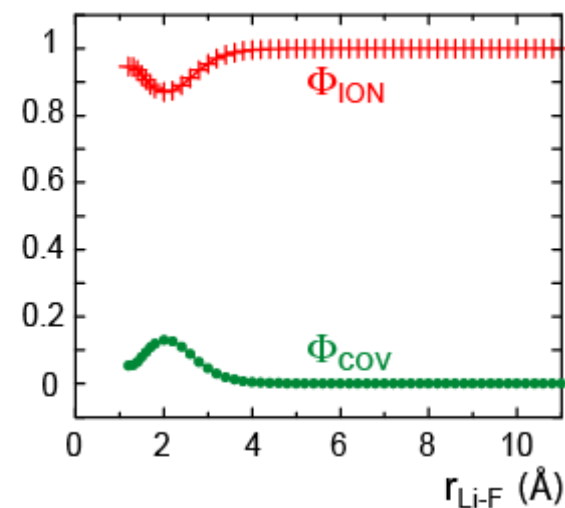


Weights:

Gas Phase



Solution

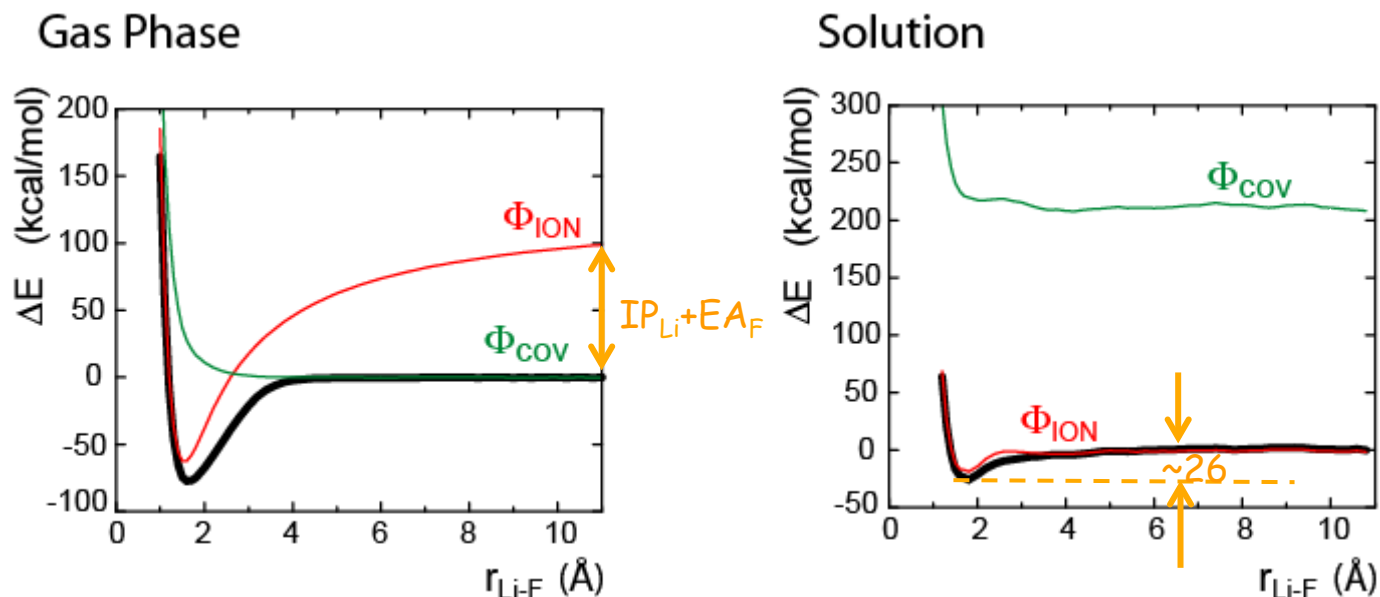


(6-31G* basis set
1S electrons frozen)

Results: Li-F

(6-31G* basis set
15 electrons frozen)

Energy Curves



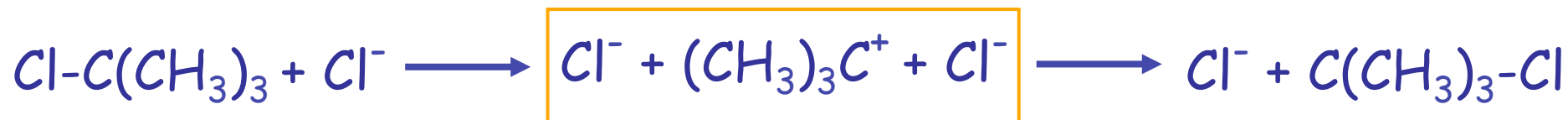
- ✚ Predicted dissociation of barrier ~ 26 kcal/mol instead of ~ 5 kcal/mol probably due to mal gas phase behavior (VBPCM - 55/30 kcal/mol)

exp $IP_{Li}+EA_F$ gives ~ 45 kcal/mol and not ~ 100 kcal/mol as calculated

- ✚ Bond length shifts from 1.6\AA to 1.8\AA in solution
- ✚ Adiabatic state stabilizes ~ 210 kcal/mol relative to the covalent state at long distance in agreement with ~ 220 kcal/mol solvation of the ions 58

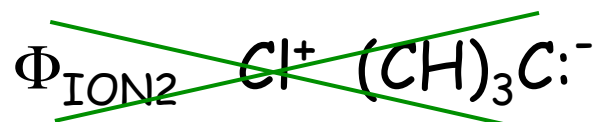
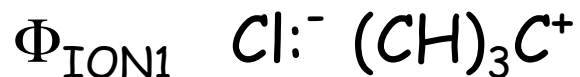
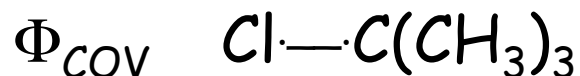
Tertiary-Butyl Chloride: *t*-BuCl

Polar Covalent Bond $\begin{cases} \text{Vacuum} \rightarrow \text{Radicals} \\ \text{Solution} \rightarrow \text{Ions} \end{cases}$



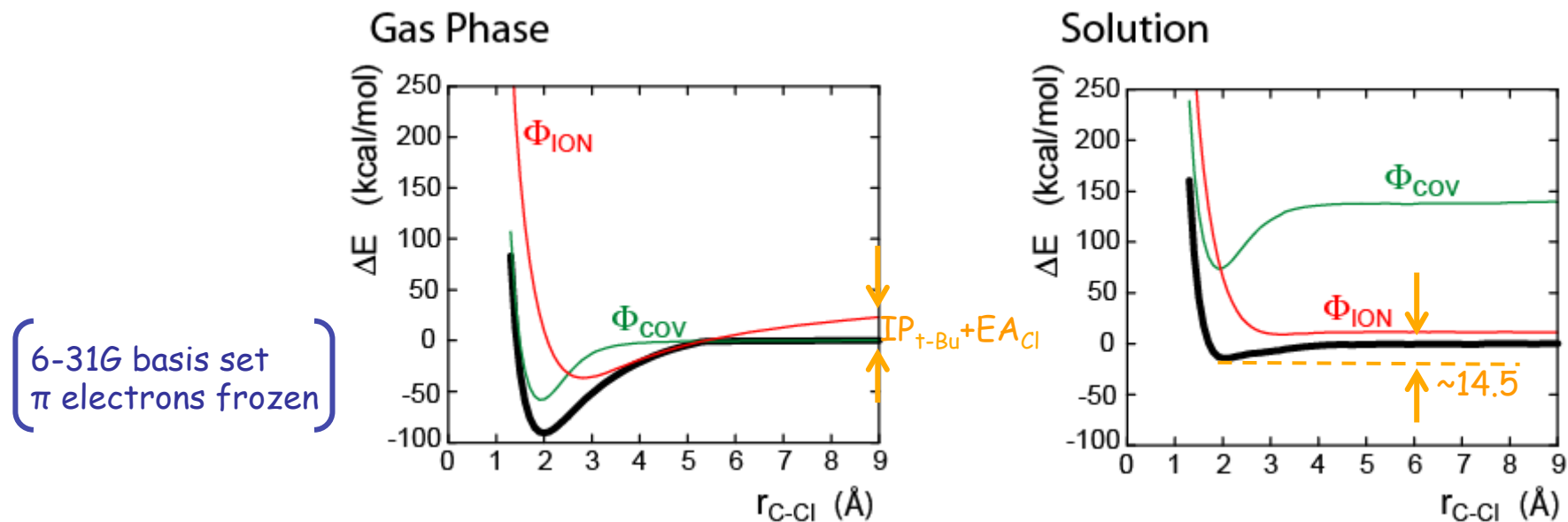
S_N1 mechanism in solution

Relevant VB Structures:

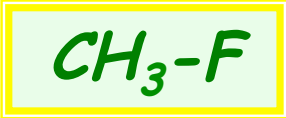


Results: *t*-BuCl

Energy Curves

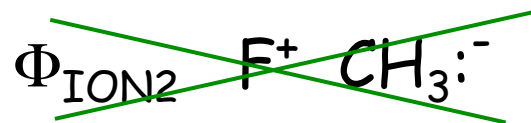


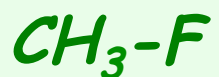
- ✚ Dissociation into: radicals - vacuum vs ions - solution
- ✚ Predicted dissociation barrier of ~ 14.5 kcal/mol instead of ~ 19.5 kcal/mol (VBPCM 27.8 kcal/mol)
- ✚ Absence of ion pair formation
again, probably due to mal gas phase behavior
($IP_{t-Bu} + EA_{Cl}$ gives ~ 84 kcal/mol and not ~ 56 kcal/mol as calculated)



Polar Covalent Bond $\xrightarrow[\text{Solution}]{\text{Vacuum}}$ Radicals

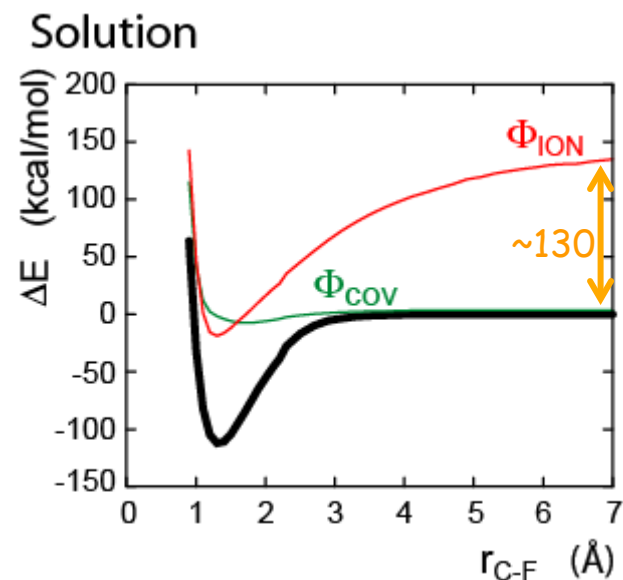
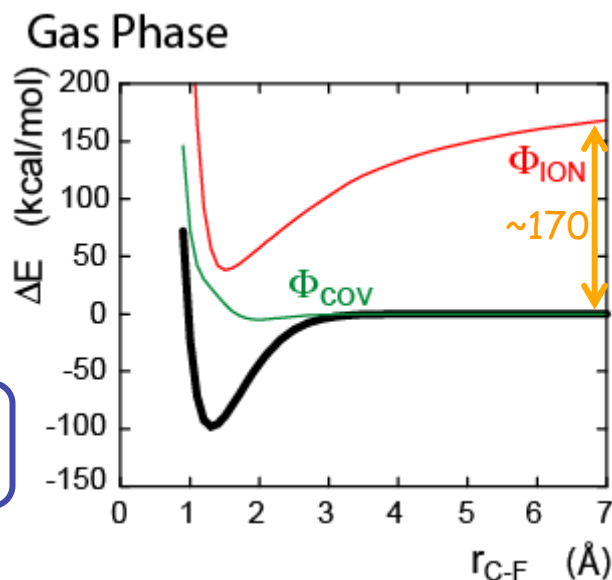
Relevant VB Structures:





Energy Curves

6-31G* basis set
Core electrons frozen



✚ Homolytic dissociation in both vacuum and solution

✚ Most of the bond energy comes from resonance

✚ Ionic stabilization of 50 kcal/mol - equilibrium
40 kcal/mol - long distance

✚ Expected small ionic-covalent gap in solution

$$(IP_{CH_3} + EA_F - \pi \sim 149 \text{ kcal/mol} = \text{Solvation}[CH_3^+] + \text{Solvation}[F^-])$$

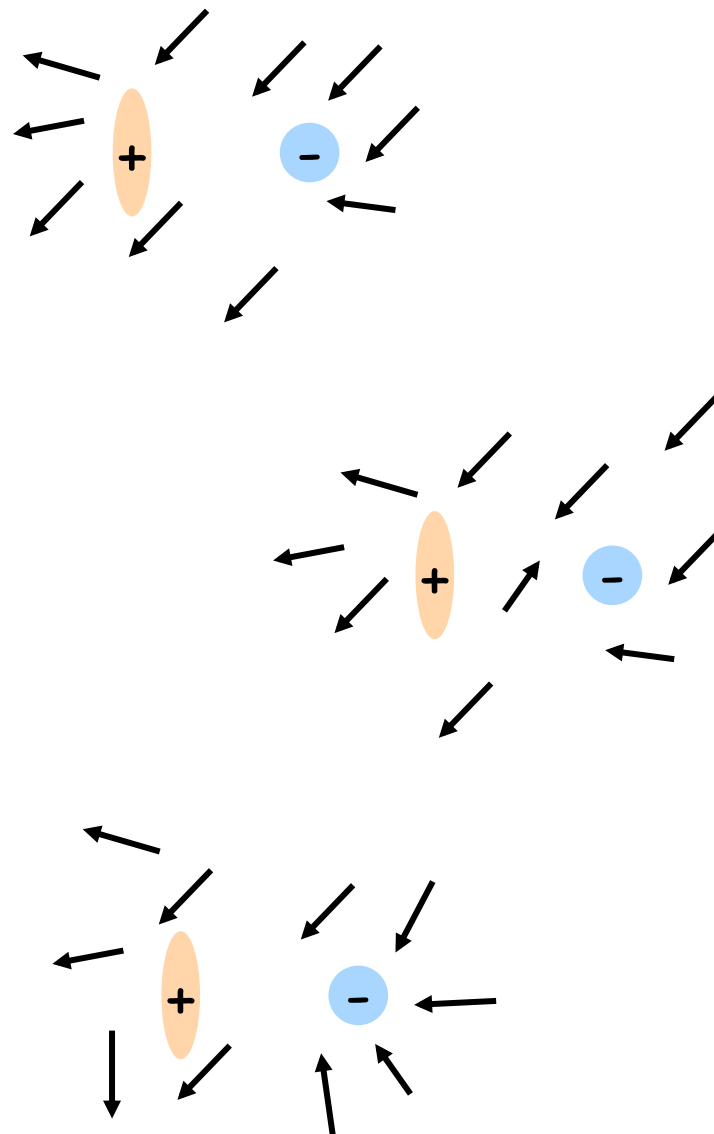
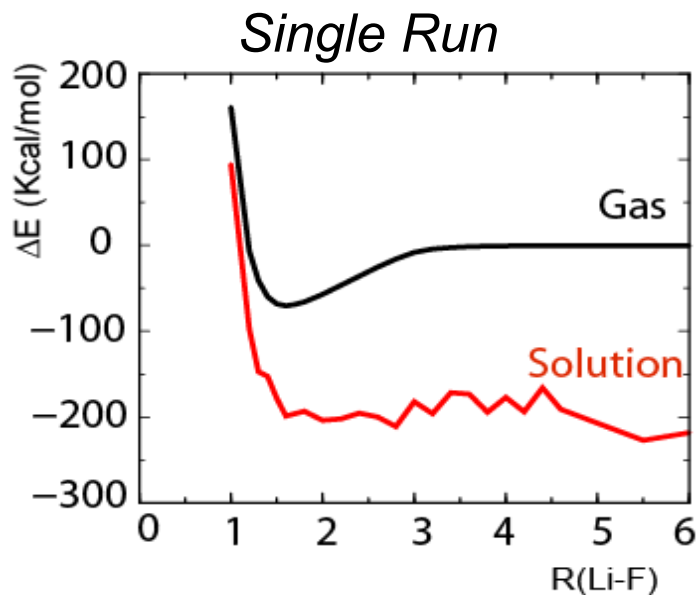
- Mal gas phase description - basis set

- Mean field description of the solution configurations.

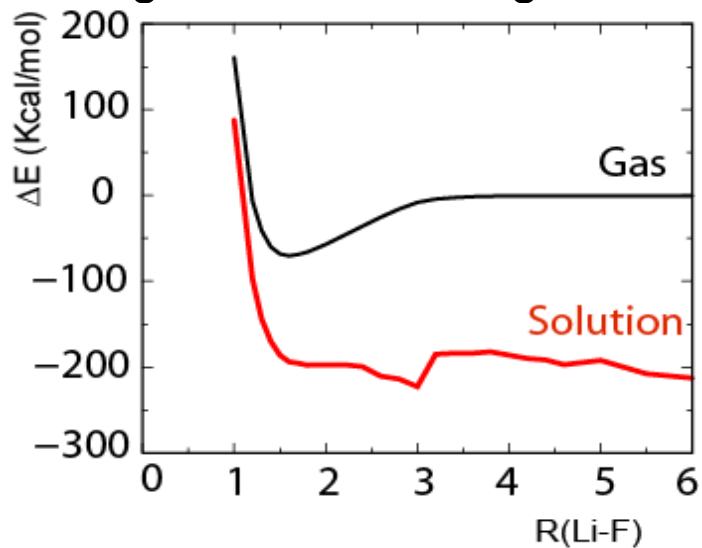
- Insufficient sampling

The importance of enough Sampling

Taken from calculations without the E_{MM}

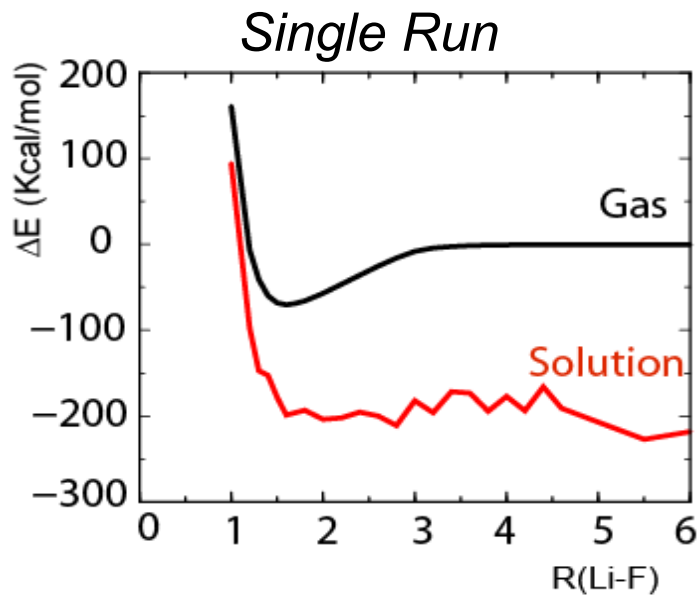
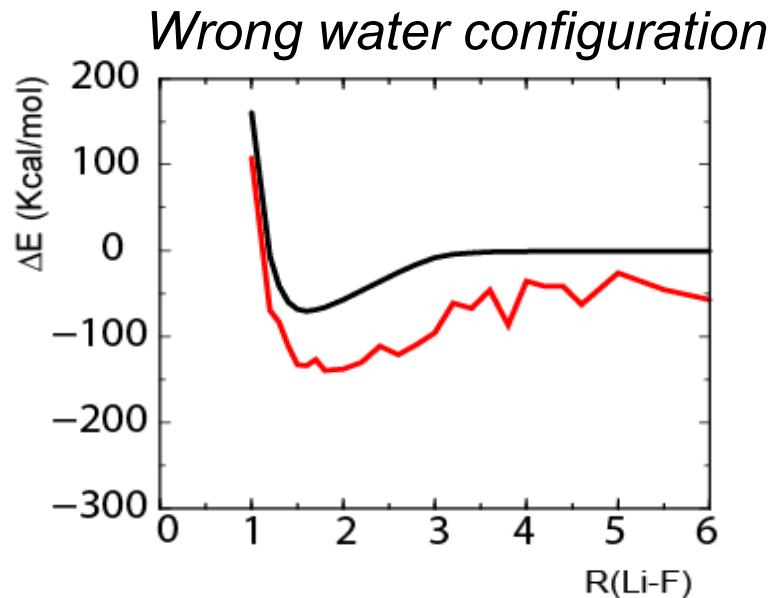
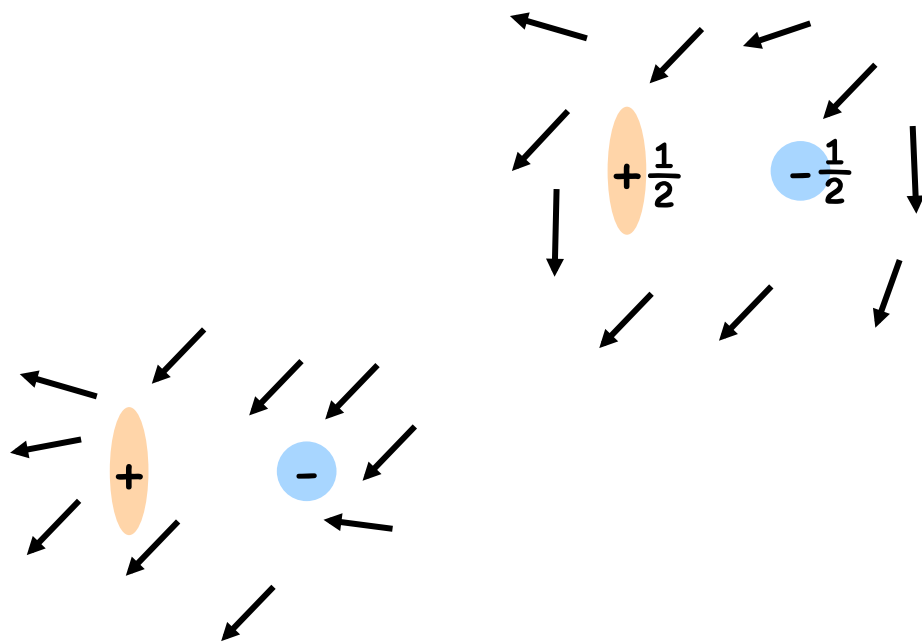


Average over 30 configurations



The importance of correct Sampling

Taken from calculations without the E_{MM}



$$\Psi \rightarrow \frac{1}{2} (\Phi_{\text{ION}} + \Phi_{\text{COV}})$$

Water relaxed with

$$\Psi \rightarrow \text{mainly } \Phi_{\text{ION}}$$

ab initio VB/MM

Finally ...

The *ab initio* VB calculations of the reactive fragments utilized the program **XMVB**:

Lingchun Song, Wei Wu, Yirong Mo, Qianer Zhang, **XMVB** - an *ab initio* Non-orthogonal Valence Bond Program, Center of Theoretical Chemistry, Department of Chemistry, and State Key Laboratory for Physical Chemistry of Solid Surfaces, Xiamen University, Xiamen Fujian 36005, China.

These values were incorporated into **MOLARIS** whose **MM** calculations were utilized

Microscopic and Semimicroscopic Calculations of Electrostatic Energies in Proteins by the **POLARIS** and **ENZYMIX** Programs, F. S. Lee, Z. T. Chu, and A. Warshel, *J. Comp. Chem.* 14, 161 (1993).

Solvation Energies (weighted)

Old values

| | | Reactants | TS | $\Delta_{(TS-R)}$ |
|---------|------|-----------|-----|-------------------|
| water | CovR | -54 | -17 | 37 |
| | Ion | -26 | -49 | -23 |
| | Tot | -80 | -73 | 7 |
| protein | CovR | -54 | -23 | 31 |
| | Ion | -37 | -61 | -24 |
| | Tot | -92 | -93 | -1 |

- The stabilization in the protein is consistently larger than in water
- Water stabilize CovR in the reactants geometry much more than in the TS - leading to the increased barrier

Solvation Energies (weighted)

Old values

| | | Reactants | TS | $\Delta_{(TS-R)}$ | $\Delta\Delta_{(P-W)}$ |
|---------|------|-----------|-----|-------------------|------------------------|
| water | CovR | -54 | -17 | 37 | |
| | Ion | -26 | -49 | -23 | |
| | Tot | -80 | -73 | 7 | |
| protein | CovR | -54 | -23 | 31 | -6 |
| | Ion | -37 | -61 | -24 | -1 |
| | Tot | -92 | -93 | -1 | -8 |

- The stabilization in the protein is consistently larger than in water
- Water stabilize CovR in the reactants geometry much more than in the TS - leading to the increased barrier
- This differential stabilization considerably decreases in the protein