

Beyond RPA in the relativistic
(quasi)particle-phonon coupling framework:
applications to isospin-transfer modes in nuclei

Caroline Robin, Elena Litvinova



WESTERN MICHIGAN UNIVERSITY

**Workshop “Theory and applications
of RPA-and-beyond methods in physics and chemistry”
May 4, 2017, Paris, France.**

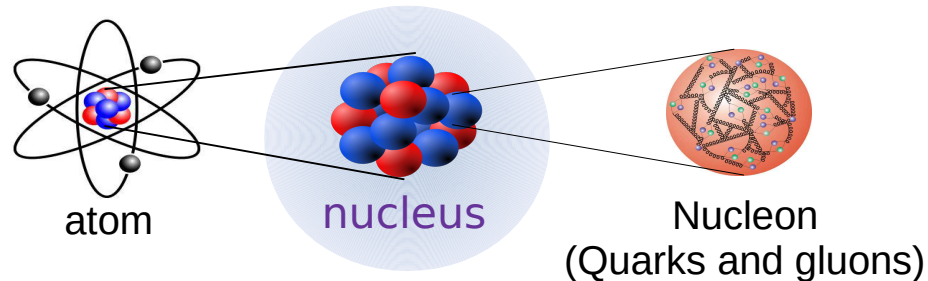
Outline

- ✦ **Introduction**
Relativistic Nuclear Field Theory: connecting the scales of nuclear physics from Quantum Hadrodynamics to emergent collective phenomena
- ✦ **Response theory for isospin-transfer modes:**
Gamow-Teller transitions, beta-decay half-lives, the “quenching” problem and the need for higher-order correlations
- ✦ **Ground-state correlations in the time-blocking approximation**
- ✦ **Conclusion & perspectives**

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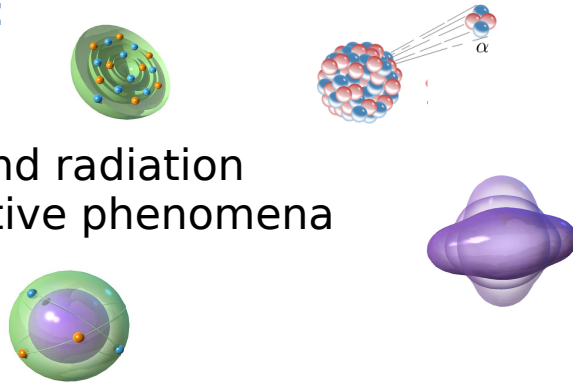
The atomic nucleus



At the frontiers between microscopic & macroscopic worlds

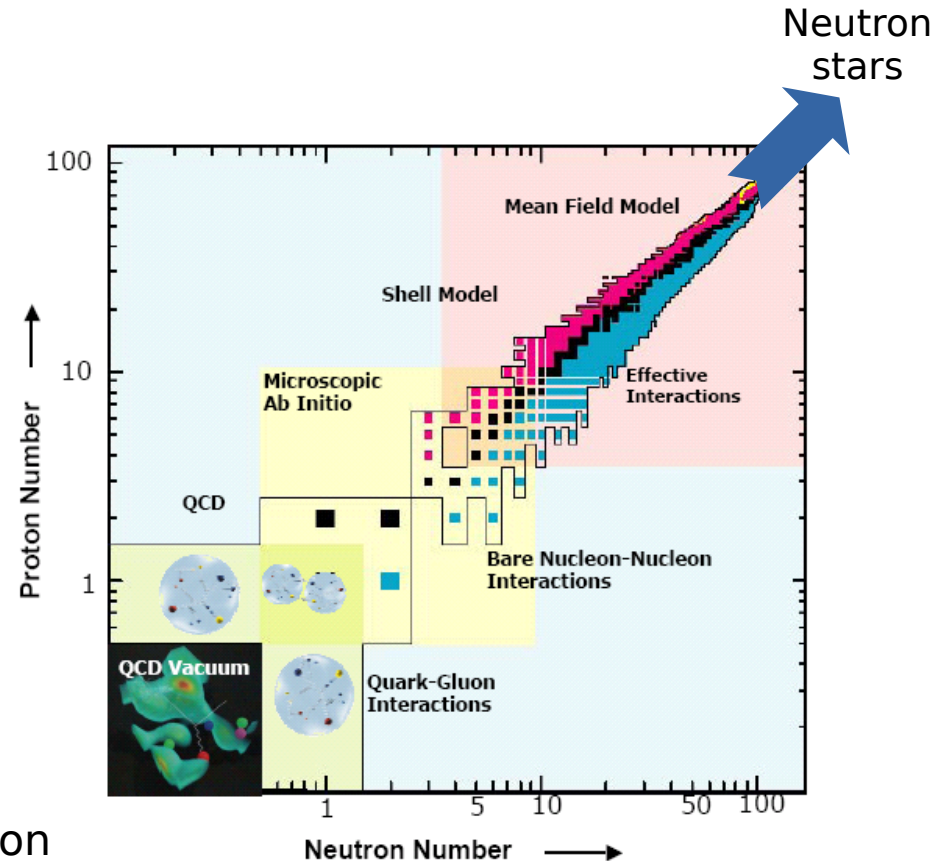
★ Exhibits generic properties of many-body systems:

- ▶ shell structure
- ▶ particle-decay and radiation
- ▶ emergent collective phenomena
- ▶ superfluidity



★ Also has specific features:

- ▶ Sensitive to 3 fundamental forces (strong, electromagnetic & weak)
- ▶ Two types of particles: neutrons & protons
→ new phenomena: neutron skin, proton-neutron pairing, isospin-transfer excitations...

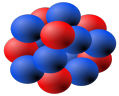


Relativistic Nuclear Field Theory: foundations



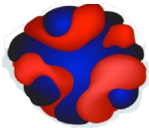
mesons

$m_{\pi, \sigma, \omega, \rho} \sim 140-800 \text{ MeV}$

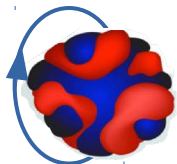


nucleons

$S_n \sim 10 \text{ MeV}$

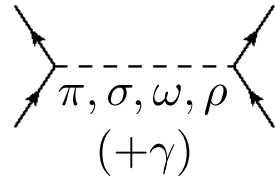


collective vibrations (phonons) \sim few MeV



nucleons & phonons

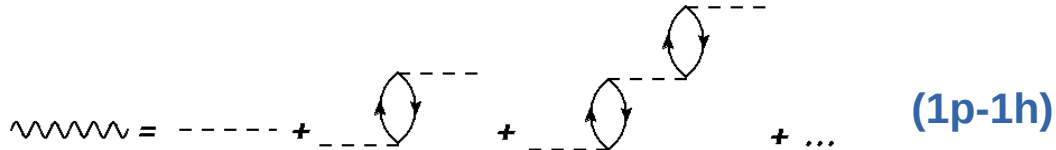
more correlations



Quantum Hadrodynamics
- Relativistic nucleons

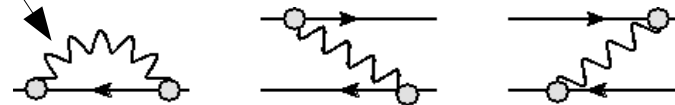


Relativistic mean-field
+ superfluidity



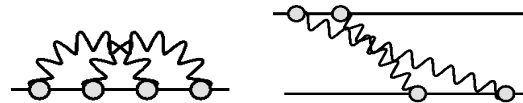
Relativistic Random Phase Approximation

phonon



(2p-2h)

Particle-Vibration coupling - Nuclear Field theory
- Time-Blocking



(3p-3h)

more correlations

self-consistent extensions of the Relativistic Mean-Field via Green function techniques

successive corrections in the single-particle motion and effective interaction

Include complex configurations of nucleons step by step to:

- ★ Keep the advantages of RPA methods applicability to many nuclei (up to heavy/superheavy)
- ★ Ultimately achieve a highly-precise description of nuclear phenomena

Outline

✦ Introduction

Relativistic Nuclear Field Theory: connecting the scales of nuclear physics from Quantum Hadrodynamics to emergent collective phenomena

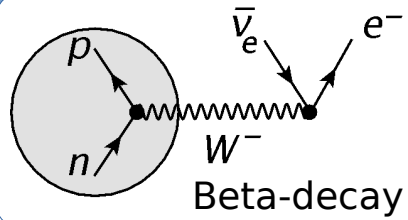
✦ **Response theory for isospin-transfer modes:**

Gamow-Teller transitions, beta-decay half-lives, the “quenching” problem and the need for higher-order correlations

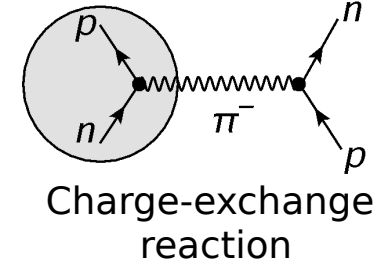
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✦ **Conclusion & perspectives**

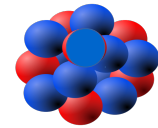
Isospin-transfer modes in nuclei



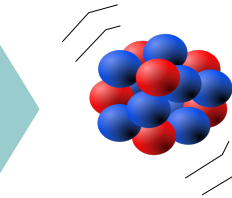
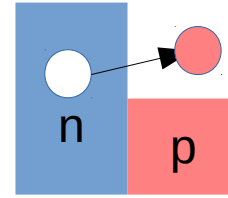
Response to an external field involving a change of the isospin projection:



Weak external field $F(t)$ with $\Delta T_z = \pm 1$

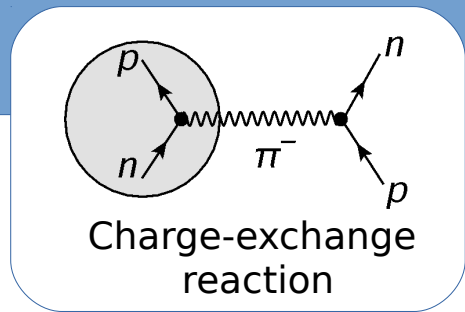
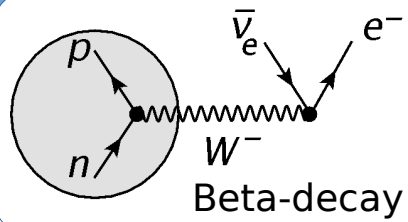


(Z, N)



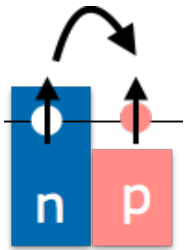
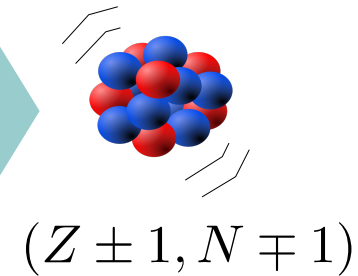
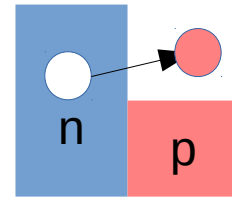
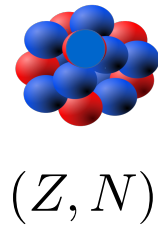
$(Z \pm 1, N \mp 1)$

Isospin-transfer modes in nuclei

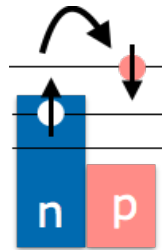


Response to an external field involving a change of the isospin projection:

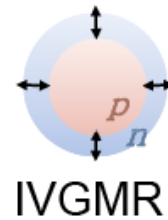
Weak external field $F(t)$ with $\Delta T_z = \pm 1$



$$F_F = \sum_n \tau_{\pm}^{(n)}$$



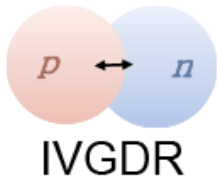
$$F_{GT} = \sum_n \sigma_{(n)}^i \tau_{\pm}^{(n)}$$



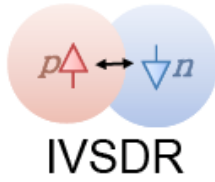
$$F_M = \sum_n r_{(n)}^2 \tau_{\pm}^{(n)}$$



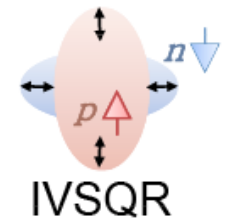
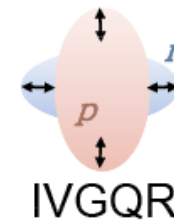
$$F_{SM} = \sum_n r_{(n)}^2 \sigma_{(n)}^i \tau_{\pm}^{(n)}$$



$$F_D = \sum_n r_{(n)} Y_1^{(n)} \tau_{\pm}^{(n)}$$



$$F_{SD}^{\lambda} = \sum_n r_{(n)} [\sigma_{(n)}^i \otimes Y_1^{(n)}]_{\lambda} \tau_{\pm}^{(n)}$$



...

Isospin-transfer modes in nuclei

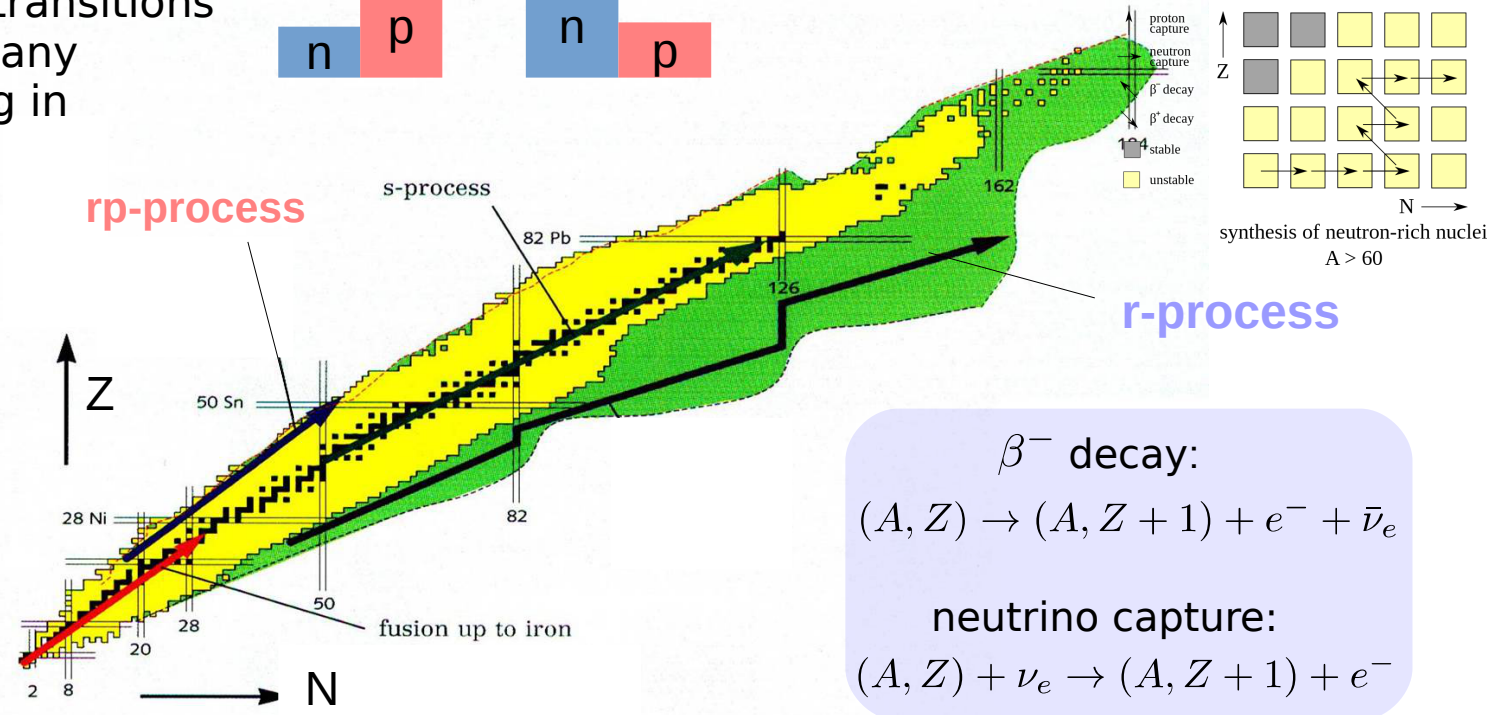
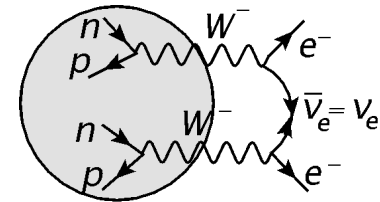
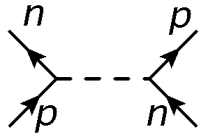
★ The study of nuclear isospin-transfer excitations has many applications in

→ **Nuclear physics:** constraints on the (S,T) channels of the nuclear interaction...

→ **Particle physics:** nature of neutrinos ($0\nu\beta\beta$ decay), ...

→ **Astrophysics:**

Fermi and Gamow-Teller transitions determine the rates of many weak processes occurring in stellar environments...



β^+ decay:
 $(A, Z) \rightarrow (A, Z - 1) + e^+ + \nu_e$

electron capture:
 $(A, Z) + e^- \rightarrow (A, Z - 1) + \nu_e$

β^- decay:
 $(A, Z) \rightarrow (A, Z + 1) + e^- + \bar{\nu}_e$

neutrino capture:
 $(A, Z) + \nu_e \rightarrow (A, Z + 1) + e^-$

Astrophysical modeling requires properties of nuclei far from stability not yet reached experimentally

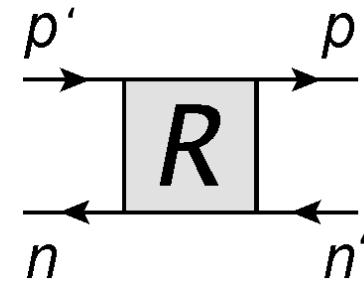
→ **need precise, consistent and predictive information from theory for many nuclei**



Response theory for isospin-transfer modes

- ★ Theoretically, all the information about the excited states is contained in the **proton-neutron response function**
= propagator of 2 correlated proton and neutron (in the particle-hole channel)

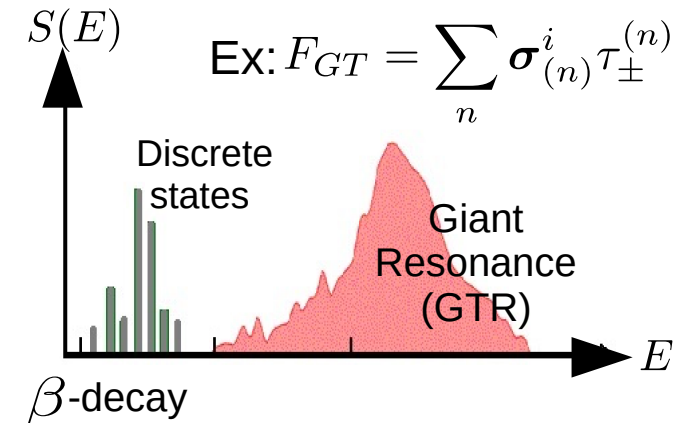
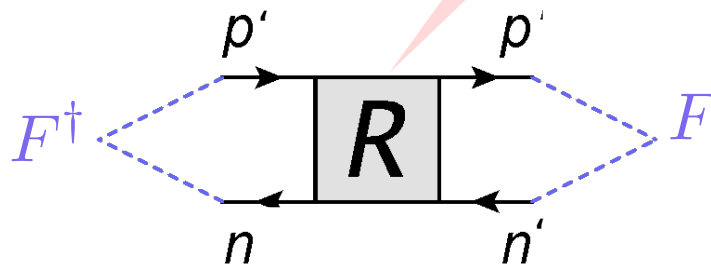
$$R_{pn,n'p'}^{ph}(t-t') = \langle 0 | \mathcal{T} (\psi_p(t) \bar{\psi}_{n'}(t) \psi_n(t') \bar{\psi}_{p'}(t')) | 0 \rangle$$



→ For instance, the strength distribution is:

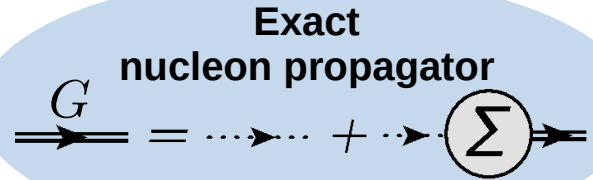
$$S(E) = \sum_f |\langle \Psi_f | \hat{F} | \Psi_i \rangle|^2 \delta(E - E_f + E_i)$$

$$= -\frac{1}{\pi} \lim_{\Delta \rightarrow 0^+} \text{Im} \langle \Psi_i | \hat{F}^\dagger R(E + i\Delta) \hat{F} | \Psi_i \rangle$$

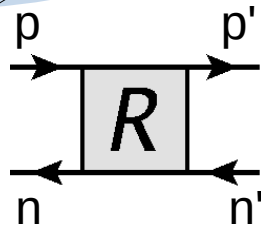


→ the response of the mother nucleus (N,Z) gives information about the states of the daughter (N+1,Z-1) or (N-1,Z+1) nucleus

Response theory for isospin-transfer modes

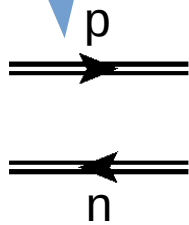


self-energy

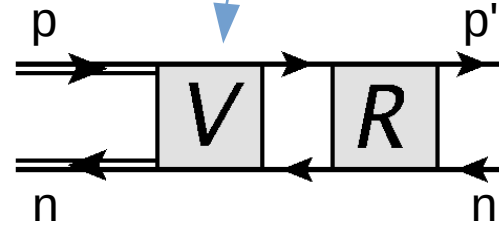


Bethe-Salpeter equation for the response:

=



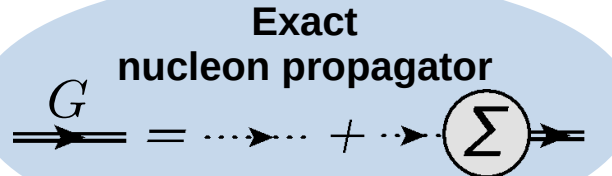
+



$$V = i \frac{\delta \Sigma}{\delta G}$$

Effective in-medium interaction

Response theory for isospin-transfer modes

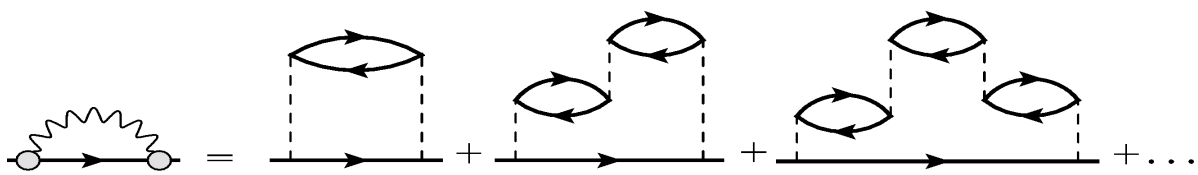
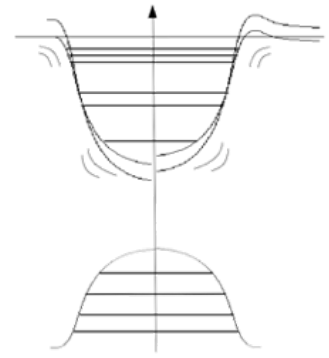
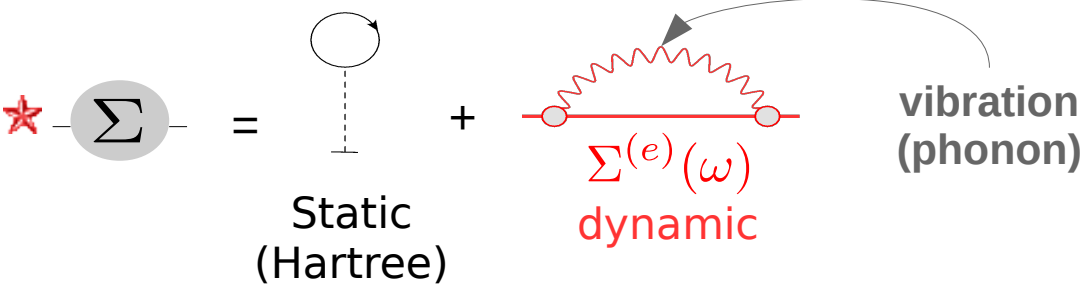
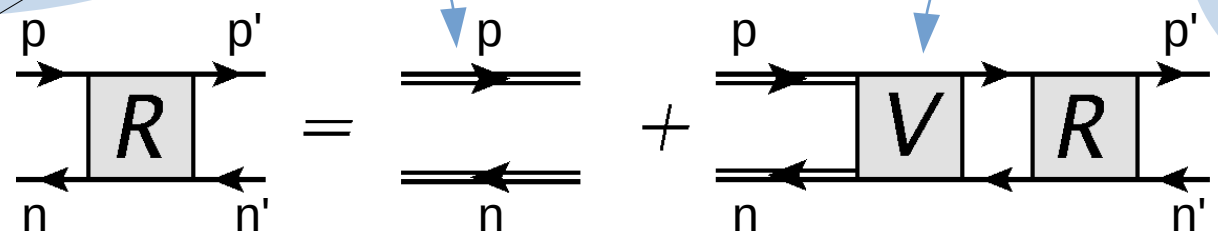


Bethe-Salpeter equation for the response:

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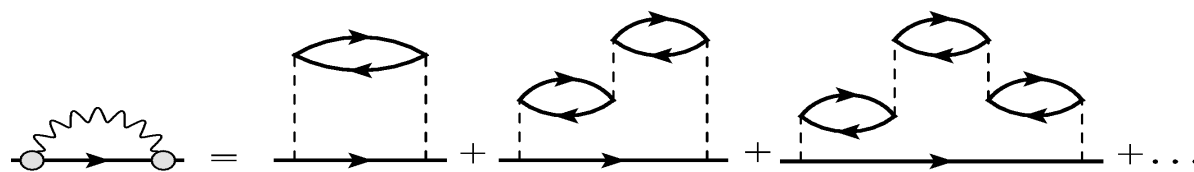
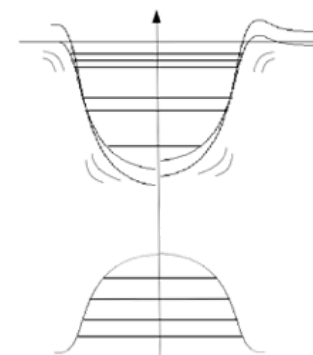
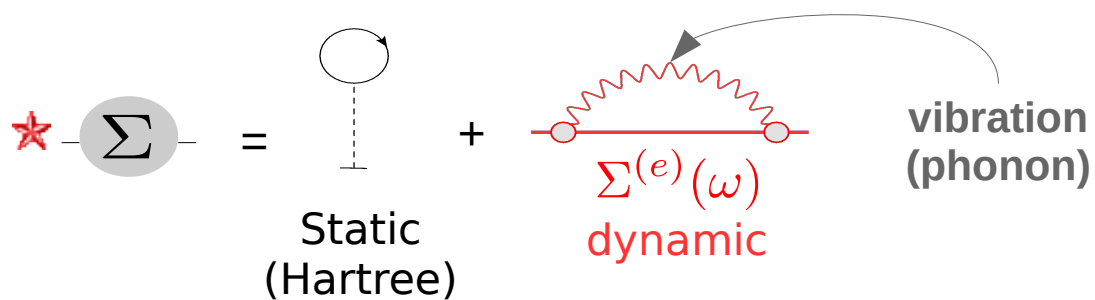
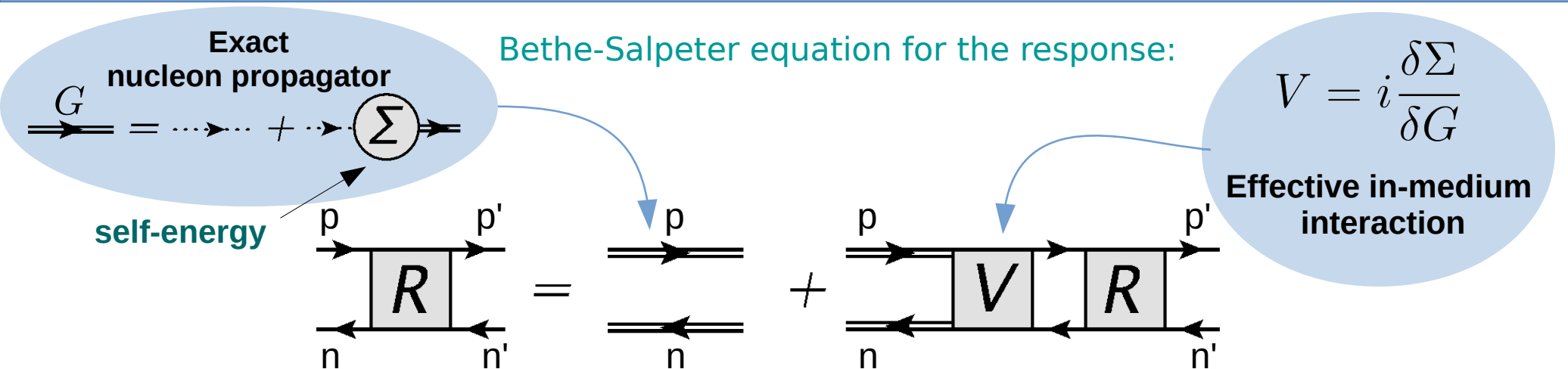
Effective in-medium interaction

self-energy

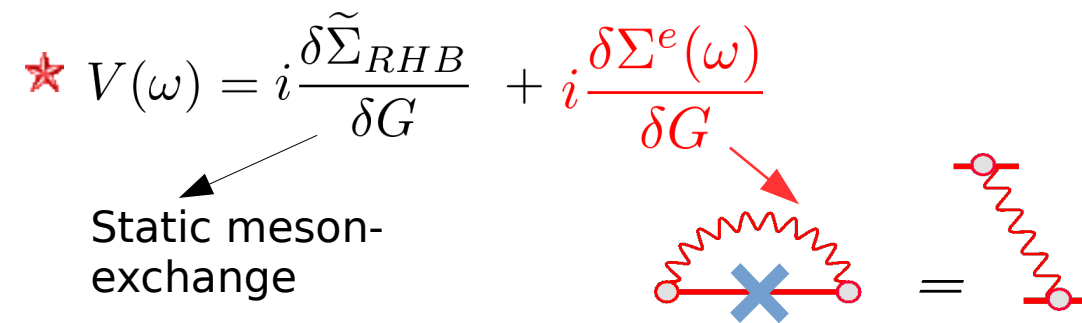


→ New-order parameter = PVC vertex

Response theory for isospin-transfer modes

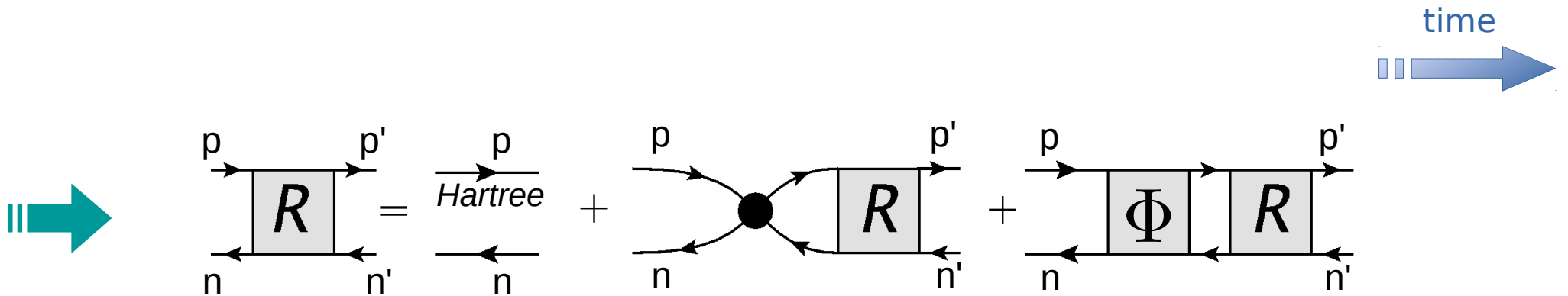


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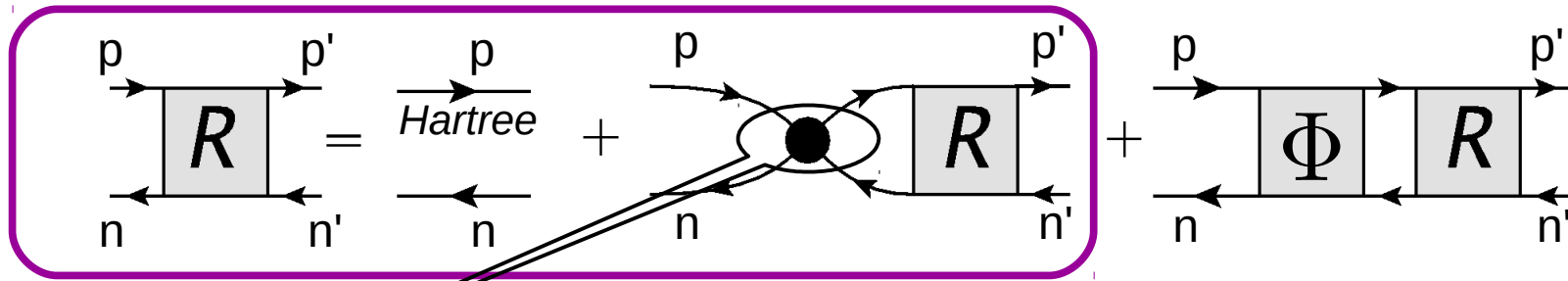
Response theory for isospin-transfer modes

In the Time-Blocking Approximation:



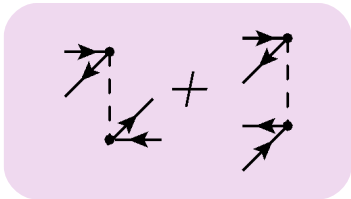
Response theory for isospin-transfer modes

In the Time-Blocking Approximation:



pn-RRPA

accounts for 1p1h configurations
(on correlated ground state)

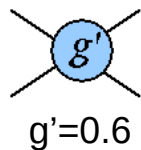


Isovector static
meson exchange

$$\tilde{V} = V_{\pi} + V_{\rho} + V_{\delta\pi}$$

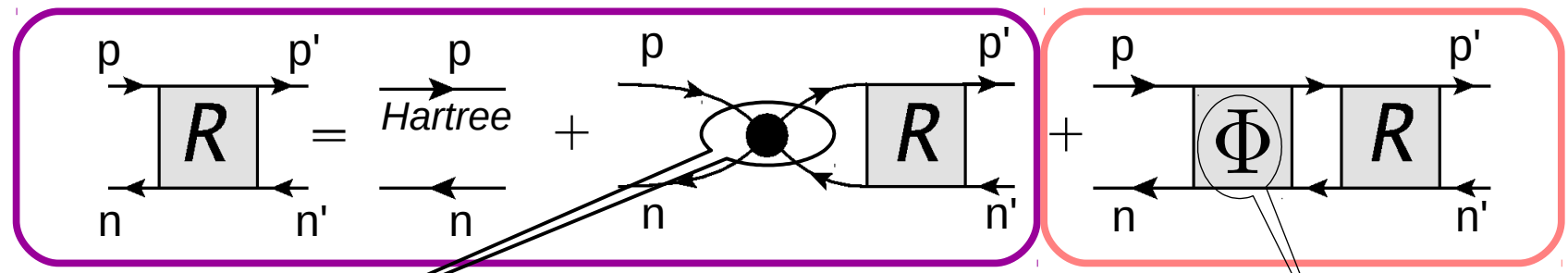
With free-space
coupling
constant

Landau-Migdal
contact term



Response theory for isospin-transfer modes

In the Time-Blocking Approximation:

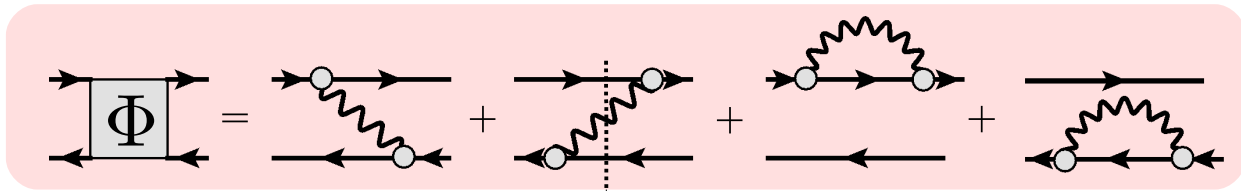


pn-RRPA

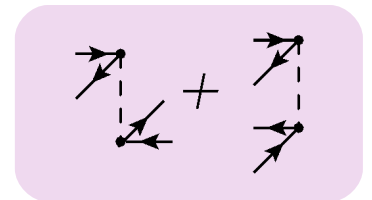
accounts for 1p1h configurations
(on correlated ground state)

+PVC

energy-dependent interaction:



accounts for
1p1h \otimes 1phonon = 2p2h
configurations

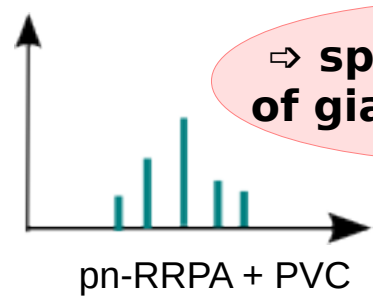
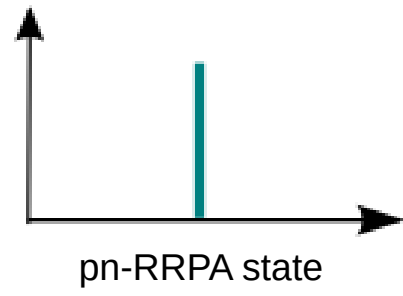
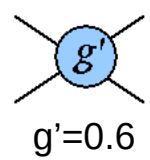


Isovector static
meson exchange

$$\tilde{V} = V_{\pi} + V_{\rho} + V_{\delta\pi}$$

With free-space
coupling
constant

Landau-Migdal
contact term



\Rightarrow **spreading width
of giant resonances**

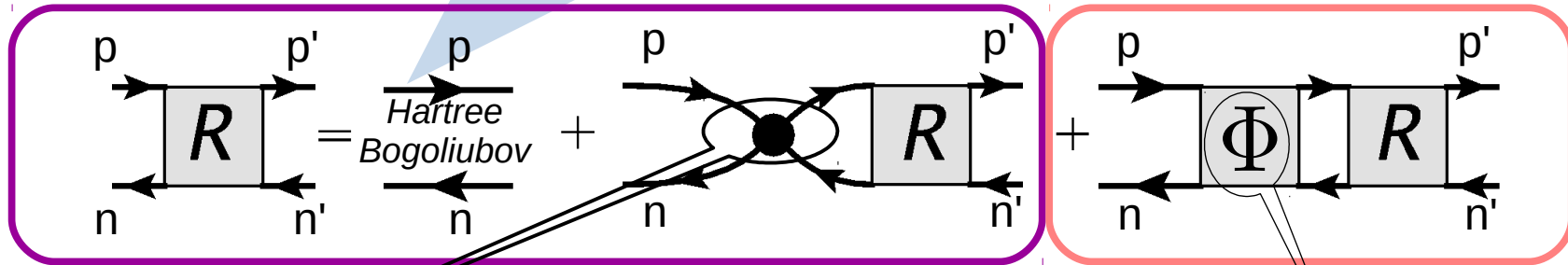
Response theory for isospin-transfer modes

In open-shell nuclei:

$$\text{Bogoliubov Quasiparticle} = \begin{bmatrix} \rightarrow & \rightarrow \\ \leftarrow & \leftarrow \end{bmatrix}$$

→ spinors of dimensions 16
(spin, isospin, relativity, pairing)

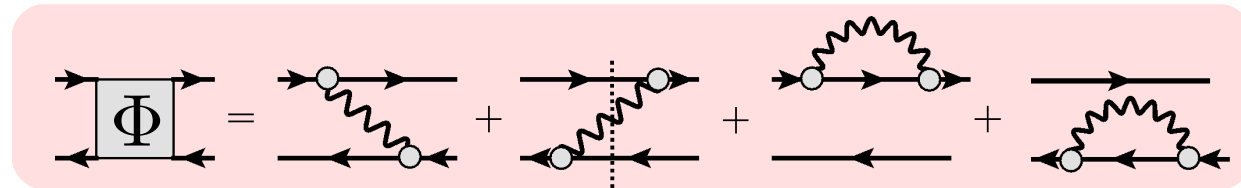
Gorkov propagator



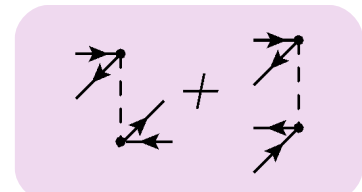
pn-RQRPA accounts for 2qp configurations
(on correlated ground state)

+QVC

energy-dependent interaction:



accounts for
2qp ⊗ 1phonon = 4qp
configurations



Isvector static
meson exchange

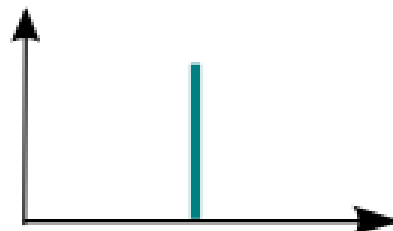
$$\tilde{V} = V_{\pi} + V_{\rho} + V_{\delta\pi}$$

With free-space
coupling
constant

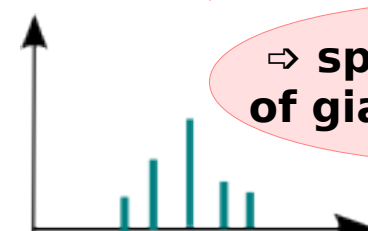
Landau-Migdal
contact term



$g'=0.6$



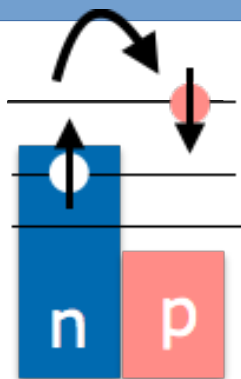
pn-RQRPA state



pn-RQRPA + QVC

⇒ **spreading width
of giant resonances**

Gamow-Teller transitions in Nickel isotopes (Ni → Cu)



$$F_{GT^-} = \sum_n \begin{pmatrix} \sigma_{(n)}^i & 0 \\ 0 & \sigma_{(n)}^i \end{pmatrix} \tau_{-}^{(n)}$$

$$\Delta T_z = -1$$

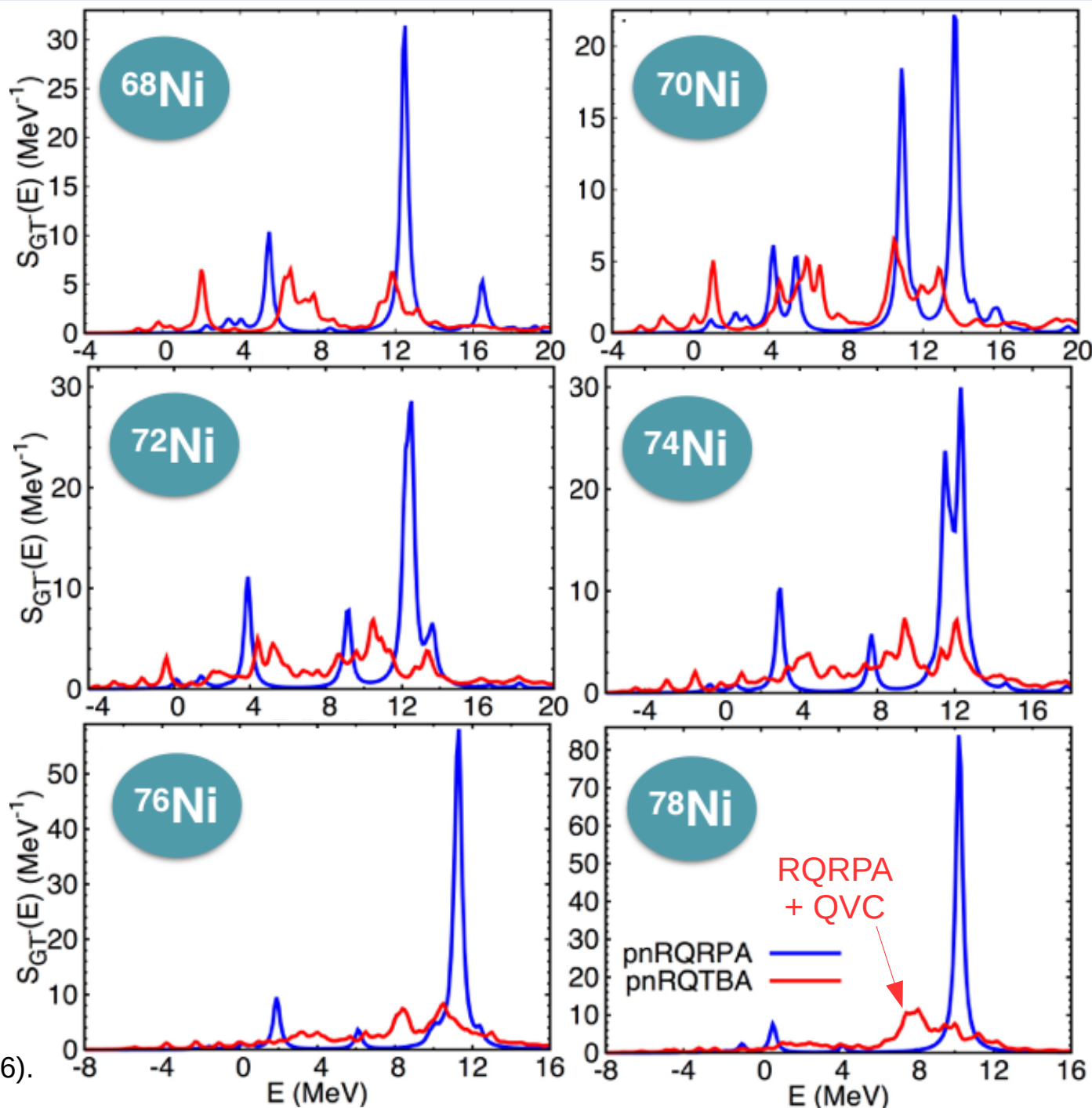
$$\Delta S = 1$$

$$\Delta L = 0$$

QVC brings fragmentation of the strength and distribution over a larger energy range

(Smearing $\Delta = 200$ keV)

C. R. and E. Litvinova EPJA 52, 205 (2016).



Gamow-Teller transitions



Two major issues concerning the theoretical description of the GT strength:

- Details of the low-lying strength and prediction of beta-decay half-lives
- “Quenching problem” of the overall strength

Gamow-Teller transitions

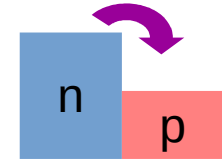
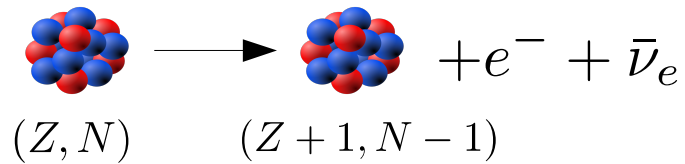


Two major issues concerning the theoretical description of the GT strength:

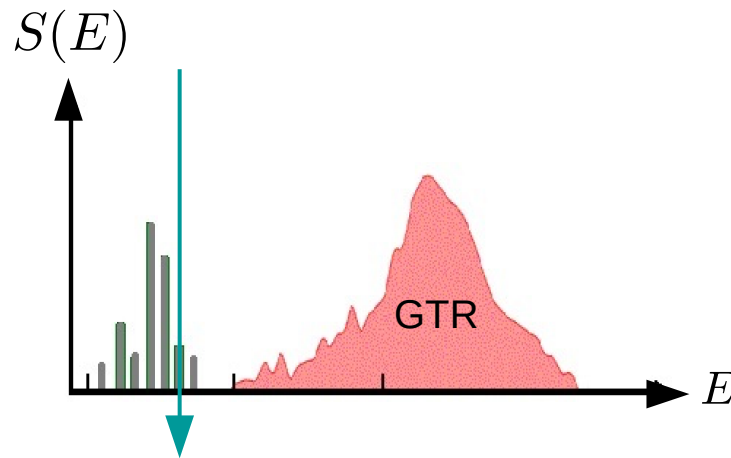
- Details of the low-lying strength and prediction of beta-decay half-lives
- “Quenching problem” of the overall strength

Low-energy GT strength and beta-decay half-lives

● β^- -decay:



It is mostly determined by the low-lying GT strength:



$$\text{Maximal energy release} = Q_\beta = M_{\text{at}}(Z, n) - M_{\text{at}}(Z+1, N-1)$$

→ beta-decay half-lives:
$$\frac{1}{T_{1/2}} = \frac{g_a^2}{D} \int_0^{Q_\beta} f(Z, Q_\beta - E) S(E) dE$$

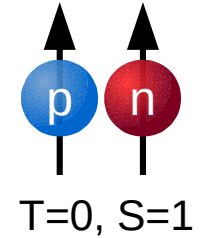
Leptonic phase-space factor

Low-energy GT strength and beta-decay half-lives

★ Problem with QRPA description: the beta-decay half-lives are systematically overestimated.

→ issue overcome by considering $T=0$ pn-pairing

But this type of pairing is not well understood
(no deuteron condensate → $T=0$ pairing is dynamic (?)...)
And not well constrained ...



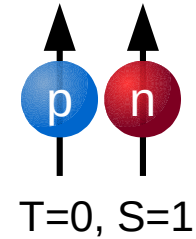
→ often treated phenomenologically with an additional static pn residual interaction in the particle-particle channel.

Low-energy GT strength and beta-decay half-lives

★ Problem with QRPA description: the beta-decay half-lives are systematically overestimated.

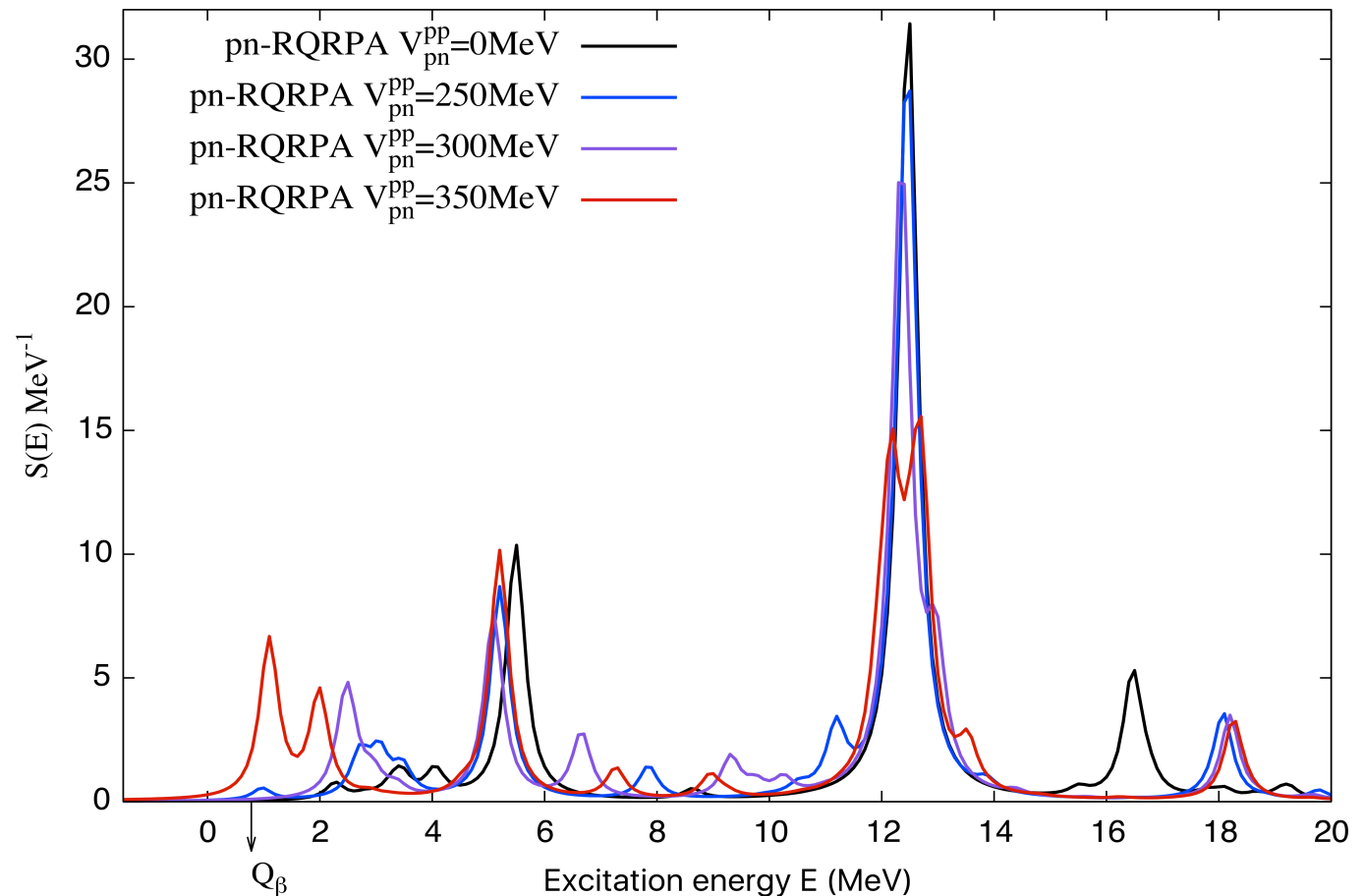
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→ often treated phenomenologically with an additional static pn residual interaction in the particle-particle channel.

→ Example in ^{68}Ni :



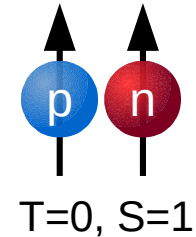
⇒ Lack of predictive power

Low-energy GT strength and beta-decay half-lives

★ Problem with QRPA description: the beta-decay half-lives are systematically overestimated.

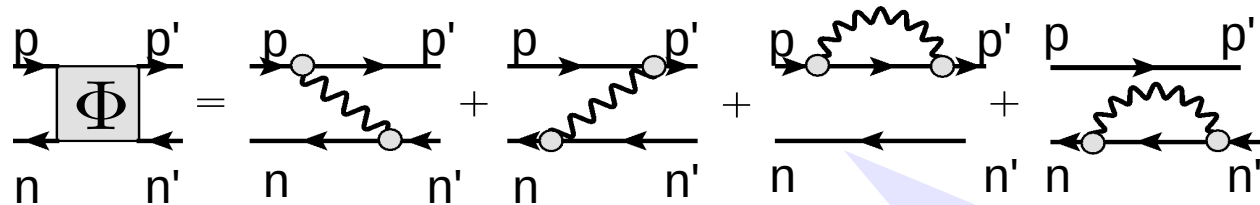
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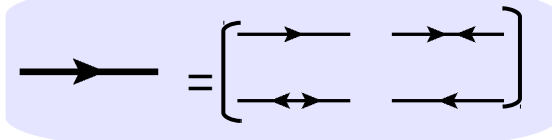


→ often treated phenomenologically with an additional static pn residual interaction in the particle-particle channel.

⇒ Goal: evaluate the effect of QVC on the half-lives and provide a possible microscopic mechanism for pn-pairing:



Quasiparticle = superposition of particles and holes:

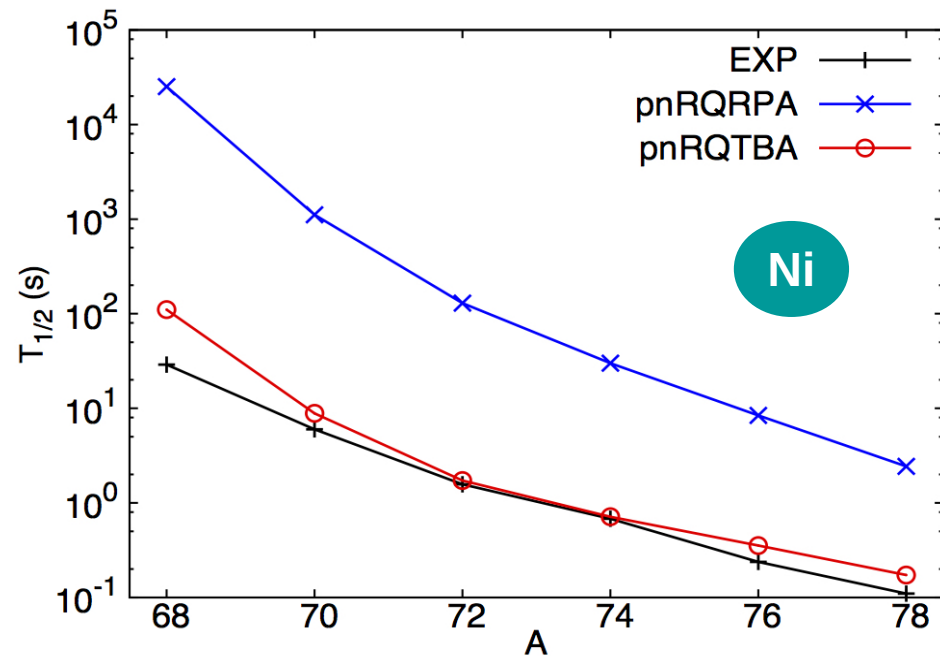


- QVC generates a pn effective interaction in the particle-hole and particle-particle channels.
- QVC can provide an underlying mechanism for dynamical proton-neutron pairing

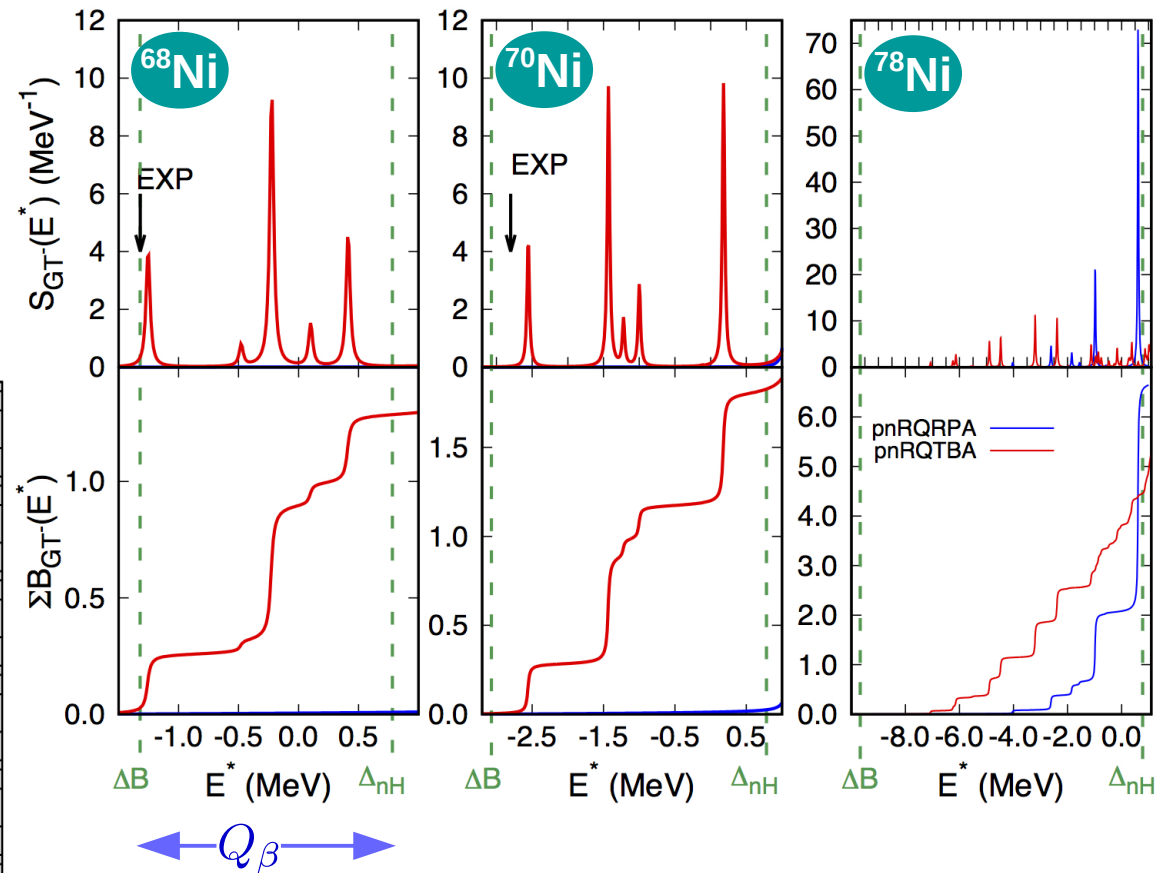
Low-energy GT strength and beta-decay half-lives

★ Half-lives and low-energy strength:

With $g_a = 1$



→ big improvement due to QVC!



- ^{68}Ni and ^{70}Ni : appearance of strength in the Q_{β} window due to QVC → finite lifetime
- ^{78}Ni : more strength with RQRPA but located at higher energies → smaller lifetime with QVC due to phase space factor

exp data from nndc.bnl.gov

C.R. and E. Litvinova EPJA 52, 205 (2016).

Gamow-Teller transitions



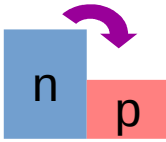
Two major issues concerning the theoretical description of the GT strength:

- Details of the low-lying strength and prediction of beta-decay half-lives
- “Quenching problem” of the overall strength

Gamow-Teller transitions and the “quenching” problem

● “Quenching problem”:

The observed GT strength (~up to the GR region) in nuclei is ~30-40% less than the model independent Ikeda sum rule: $S_- - S_+ = 3(N-Z)$

$$S_- = \sum B(GT^-)$$


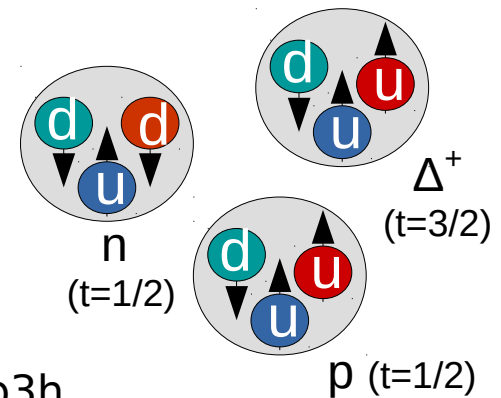
$$S_+ = \sum B(GT^+)$$


⇒ some strength is pushed at high energies → possible mechanisms?

★ Coupling of 1p1h to Δ baryon (believed to be small)

★ Coupling of 1p1h to higher-order configurations such as 2p2h, 3p3h...
(Believed to be the most important)

⇒ important to introduce complex configurations in large model spaces

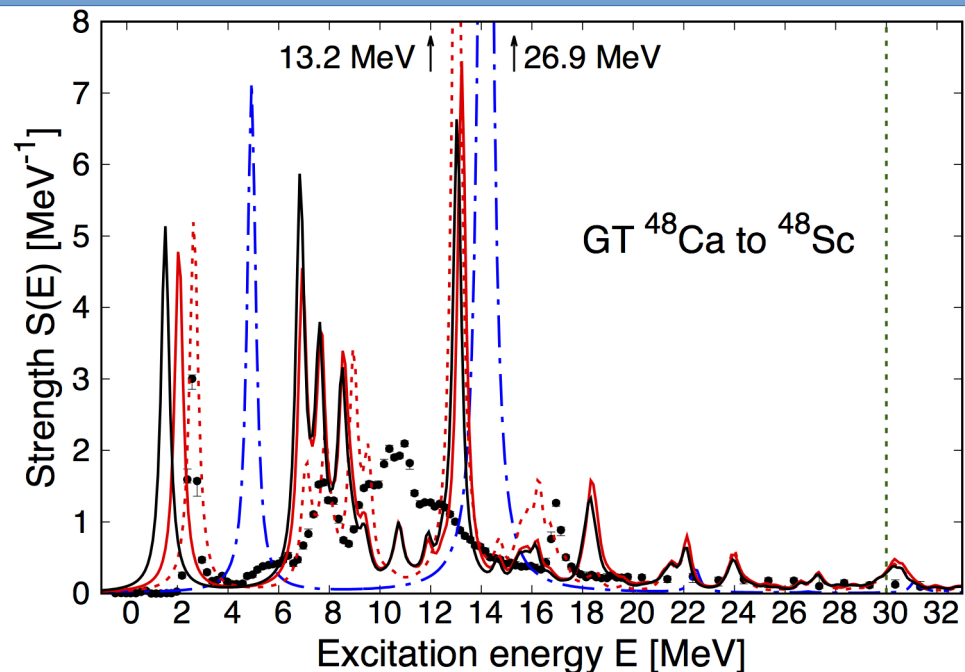
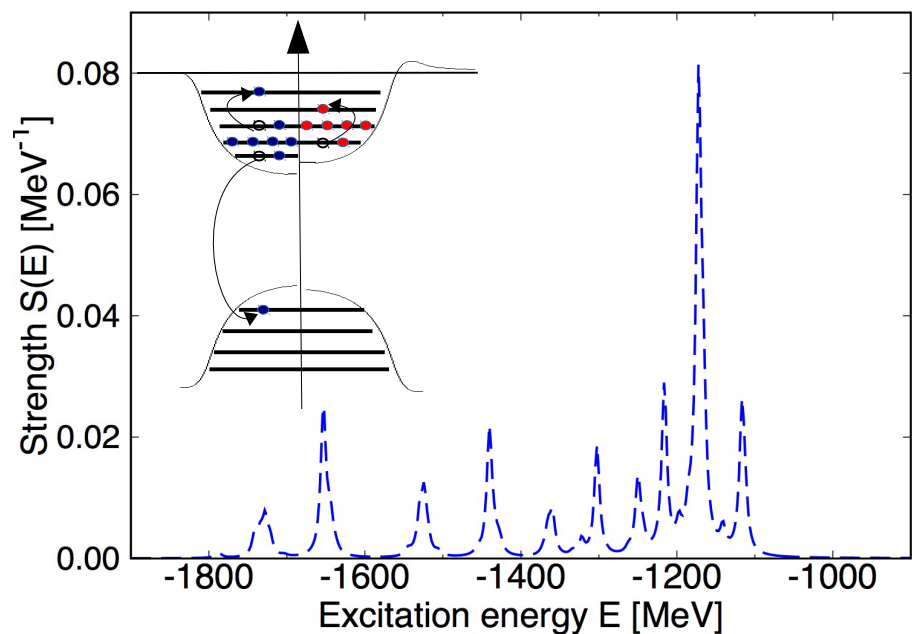


At present with RNFT+TBA:

✓ 2(q)p-2(q)h configurations

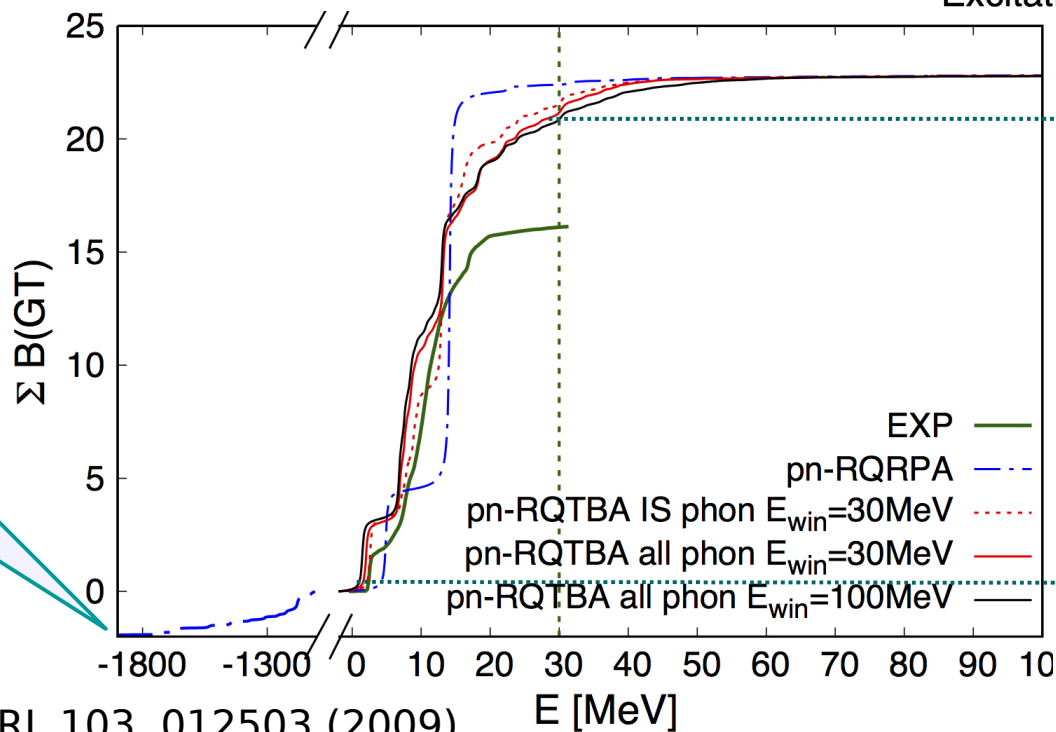
✓ in an energy window from 30 MeV up to ~100 MeV in light or doubly magic nuclei

Gamow-Teller transitions and the “quenching” problem



+ transitions from the Fermi sea to the Dirac sea (~8%)

[N. Paar et al., PRC 69, 054303]

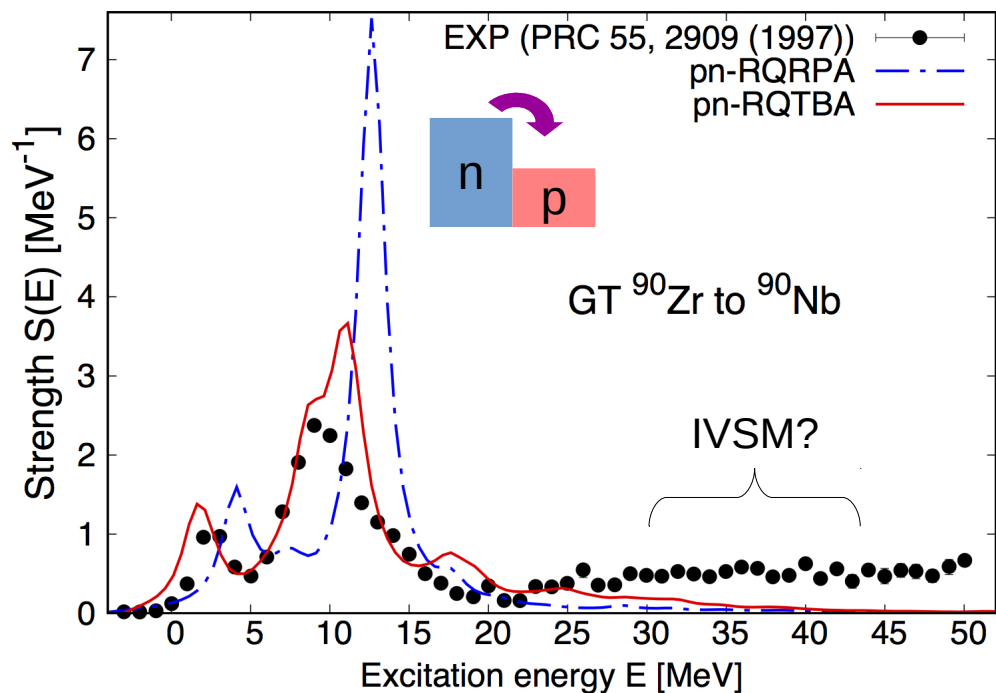


Up to 30 MeV: ~91% (vs 98% in RQRPA) of the total GT_ strength

→ RQRPA strength naturally “quenched” due to complex configurations

But not enough... (exp: 71%)

Gamow-Teller transitions and the “quenching” problem



GT strength only:

0-50 MeV:

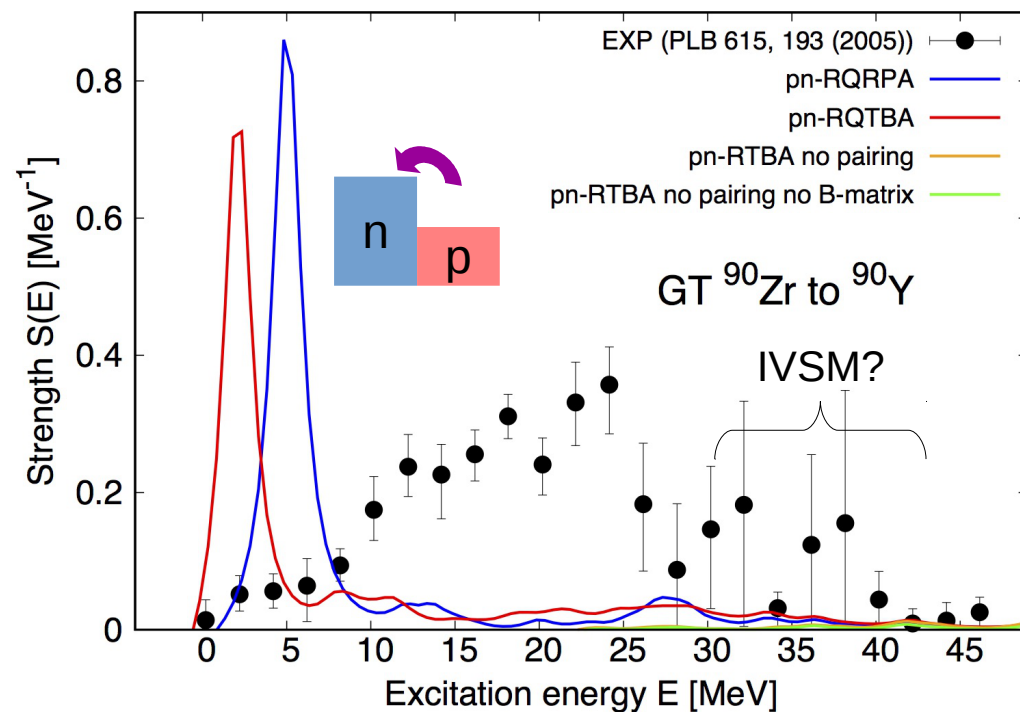
$$S_{-}^{EXP} \sim 29.3$$

$$S_{-}^{RQTBA} \sim 30.35$$

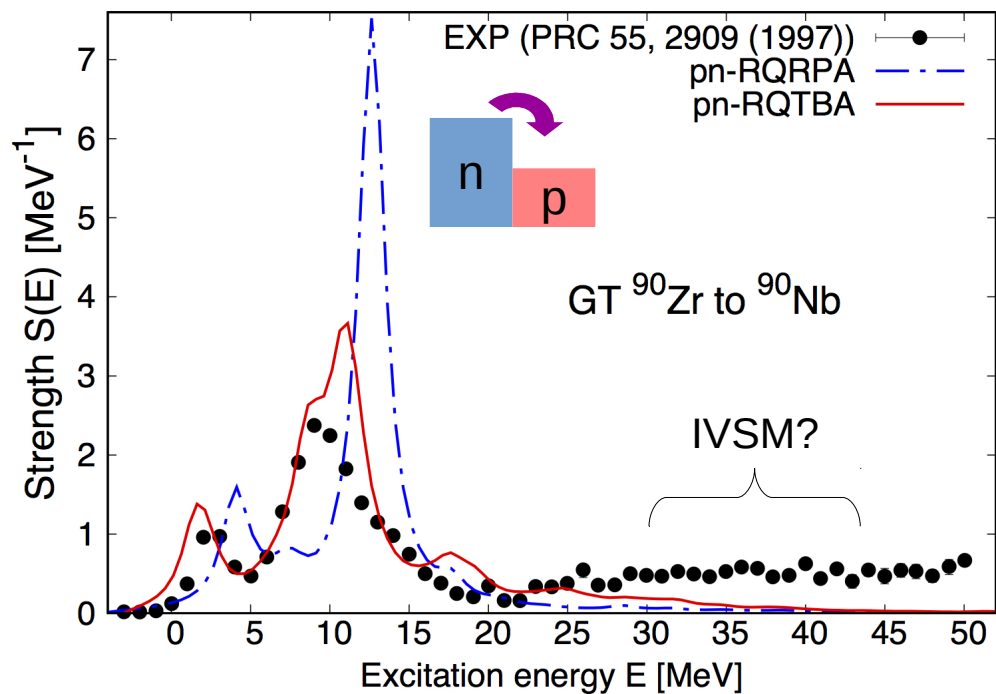
0-32 MeV:

$$S_{+}^{EXP} \sim 2.9$$

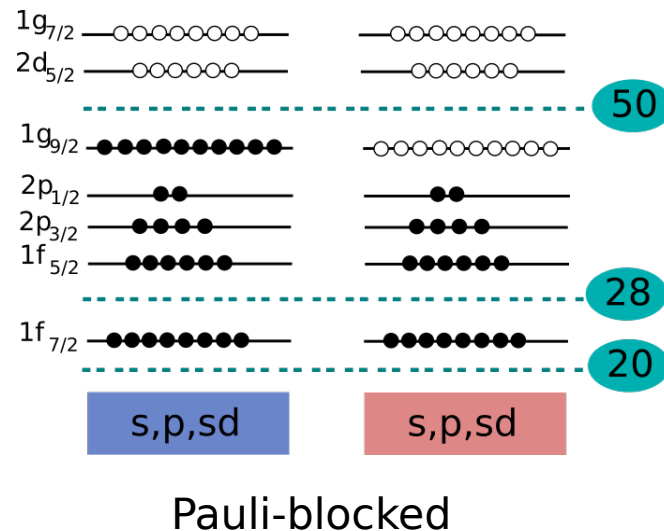
$$S_{+}^{RQTBA} \sim 2.54$$



Gamow-Teller transitions and the “quenching” problem



Schematic mean-field - no pairing:



GT strength only:

0-50 MeV:

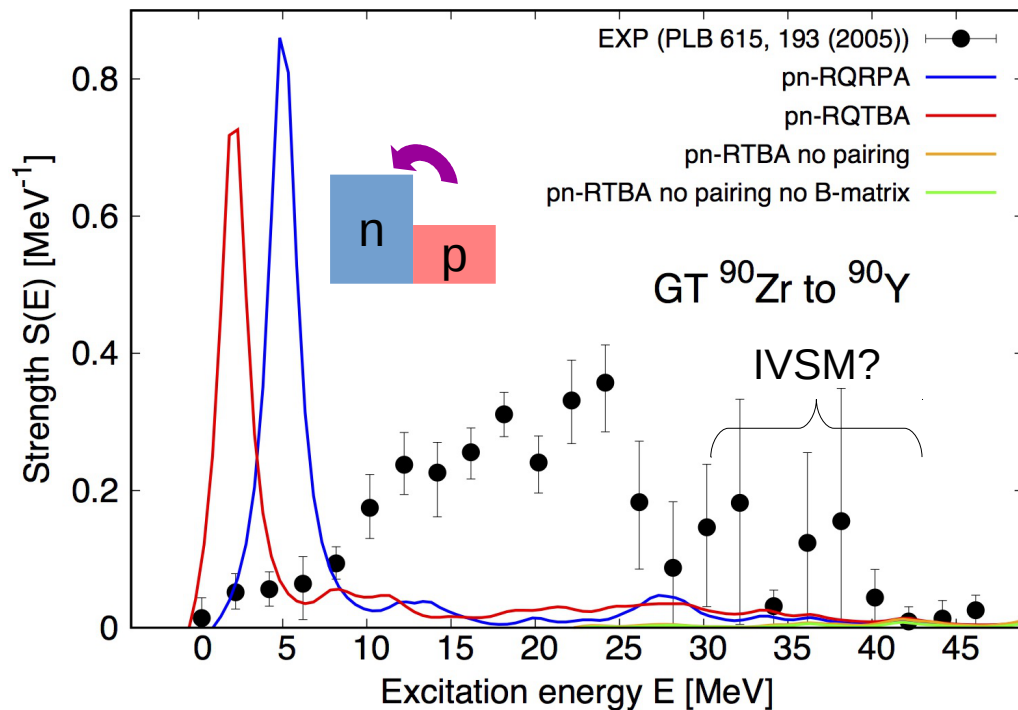
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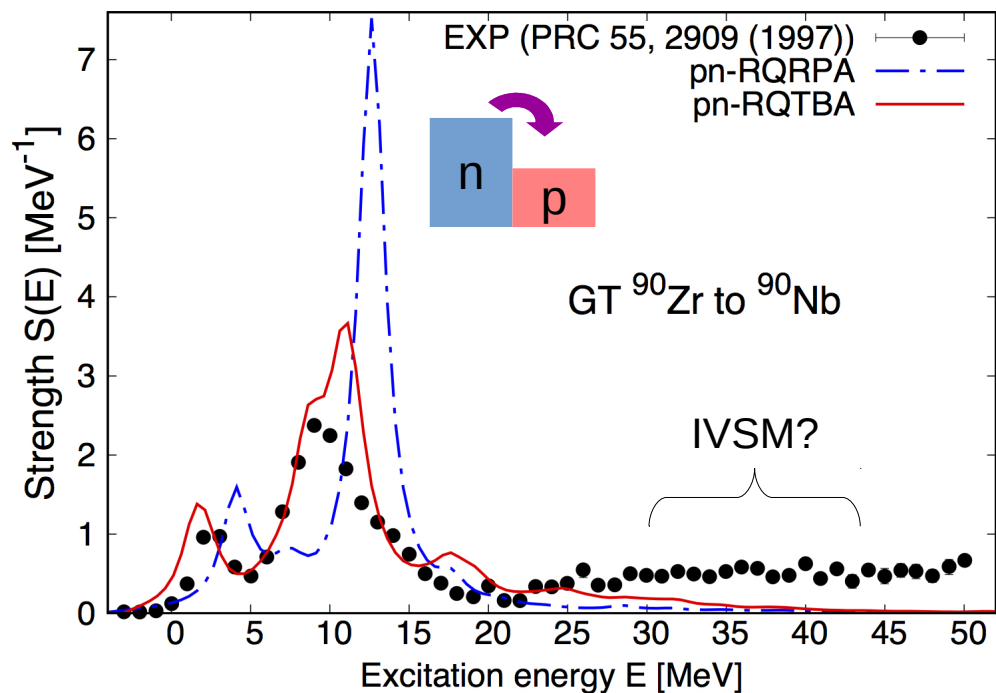
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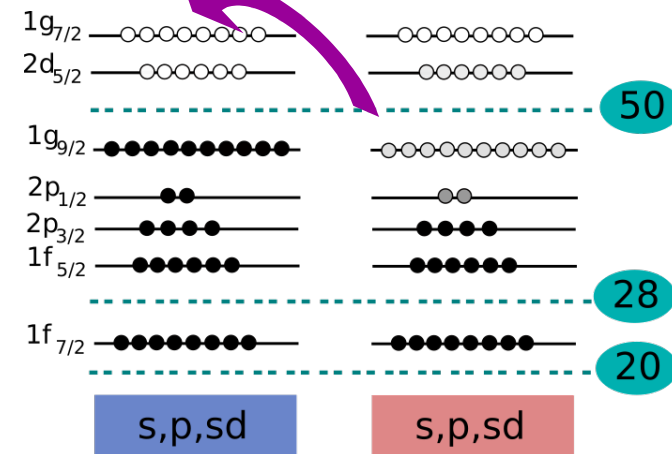
$$S_{+}^{RQTBA} \sim 2.54$$



Gamow-Teller transitions and the “quenching” problem



Schematic mean-field with pairing:



GT strength in β^+ channel caused by ground-state correlations (pairing here). But need further fragmentation \rightarrow GSC induced by QVC?

GT strength only:

0-50 MeV:

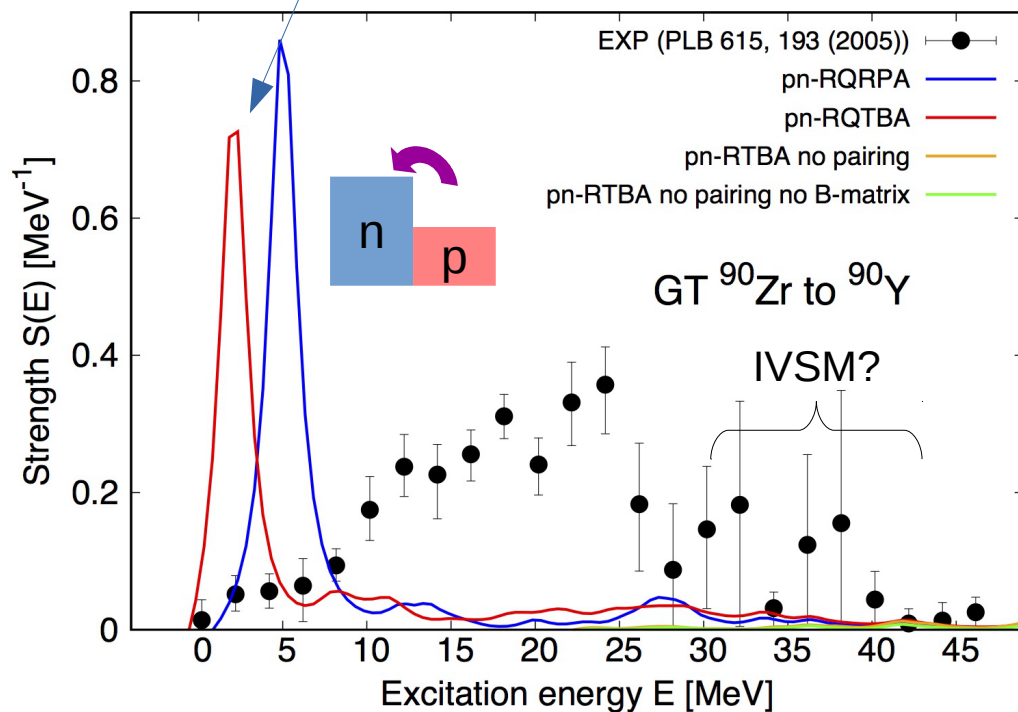
$$S_{-}^{EXP} \sim 29.3$$

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0-32 MeV:

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Outline

✦ **Introduction**

Relativistic Nuclear Field Theory: connecting the scales of nuclear physics from Quantum Hadrodynamics to emergent collective phenomena

✦ **Response theory for isospin-transfer modes:**

Gamow-Teller transitions, beta-decay half-lives, the “quenching” problem and the need for higher-order correlations

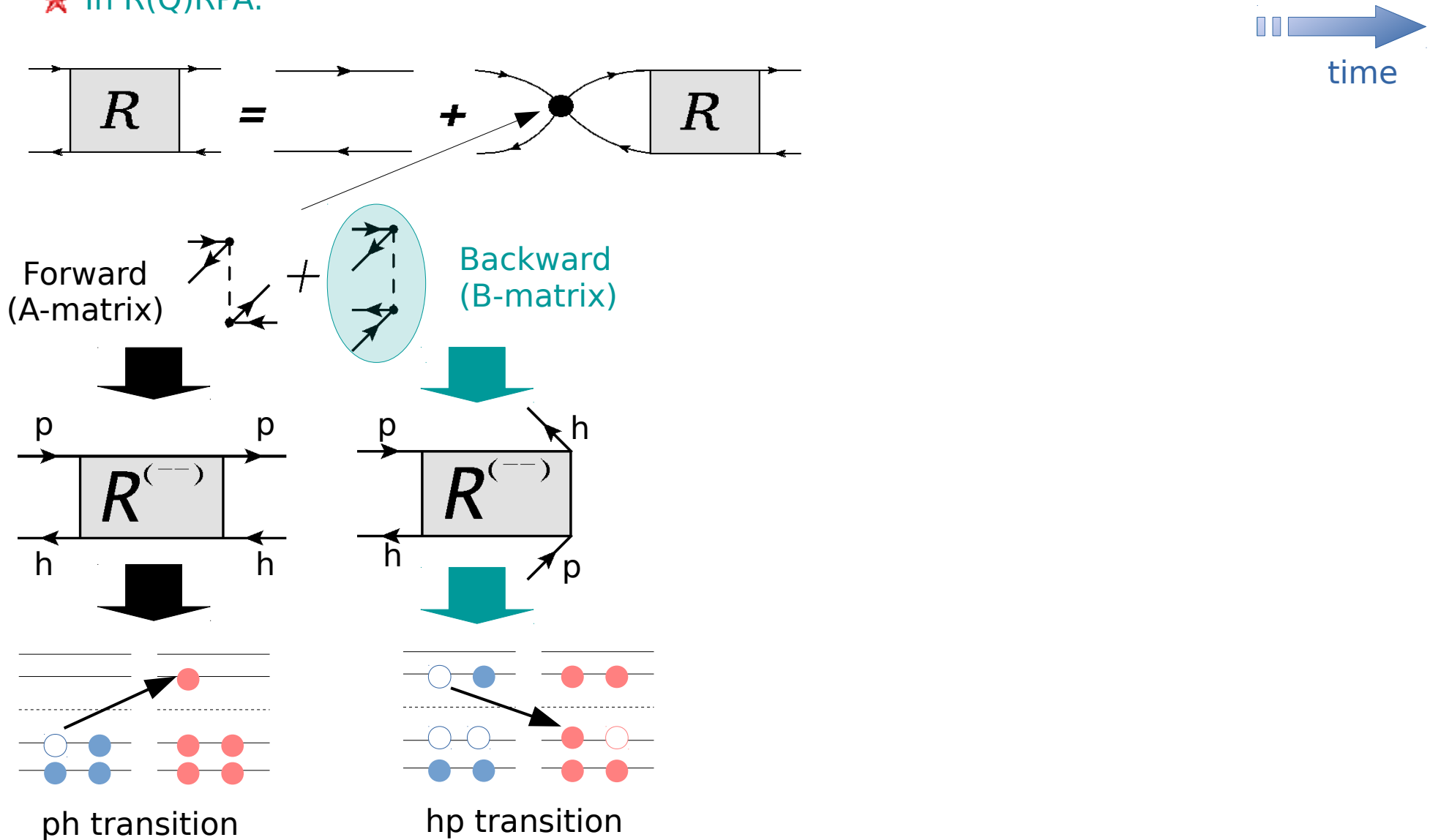
✦ **Ground-state correlations in the time-blocking approximation**

✦ **Conclusion & perspectives**

Ground-state correlations in RNFT

Ground-state correlations (GSC) in the Green's functions formalism are generated by the so-called "backward-going diagrams":

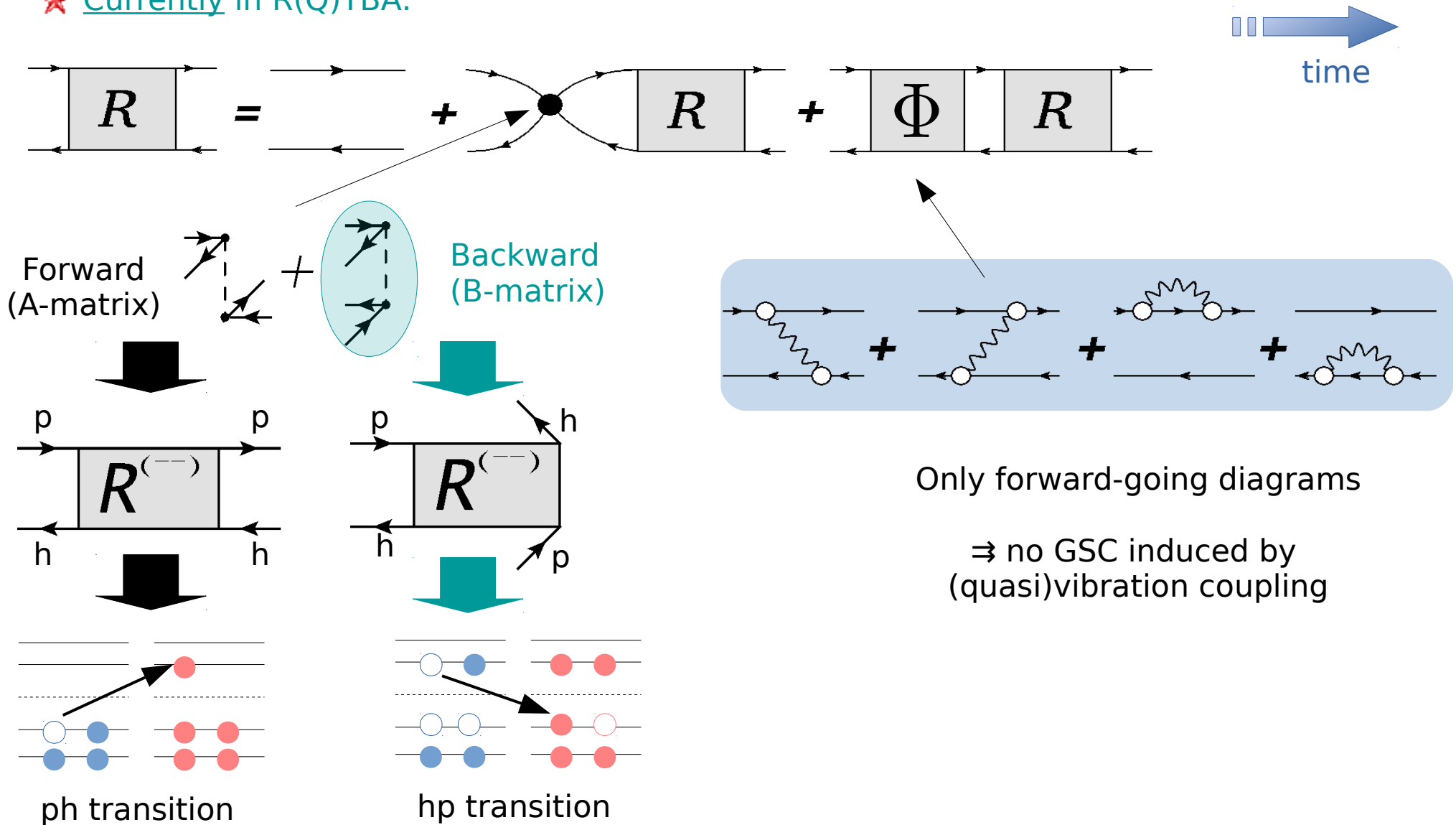
★ In R(Q)RPA:



Ground-state correlations in RNFT

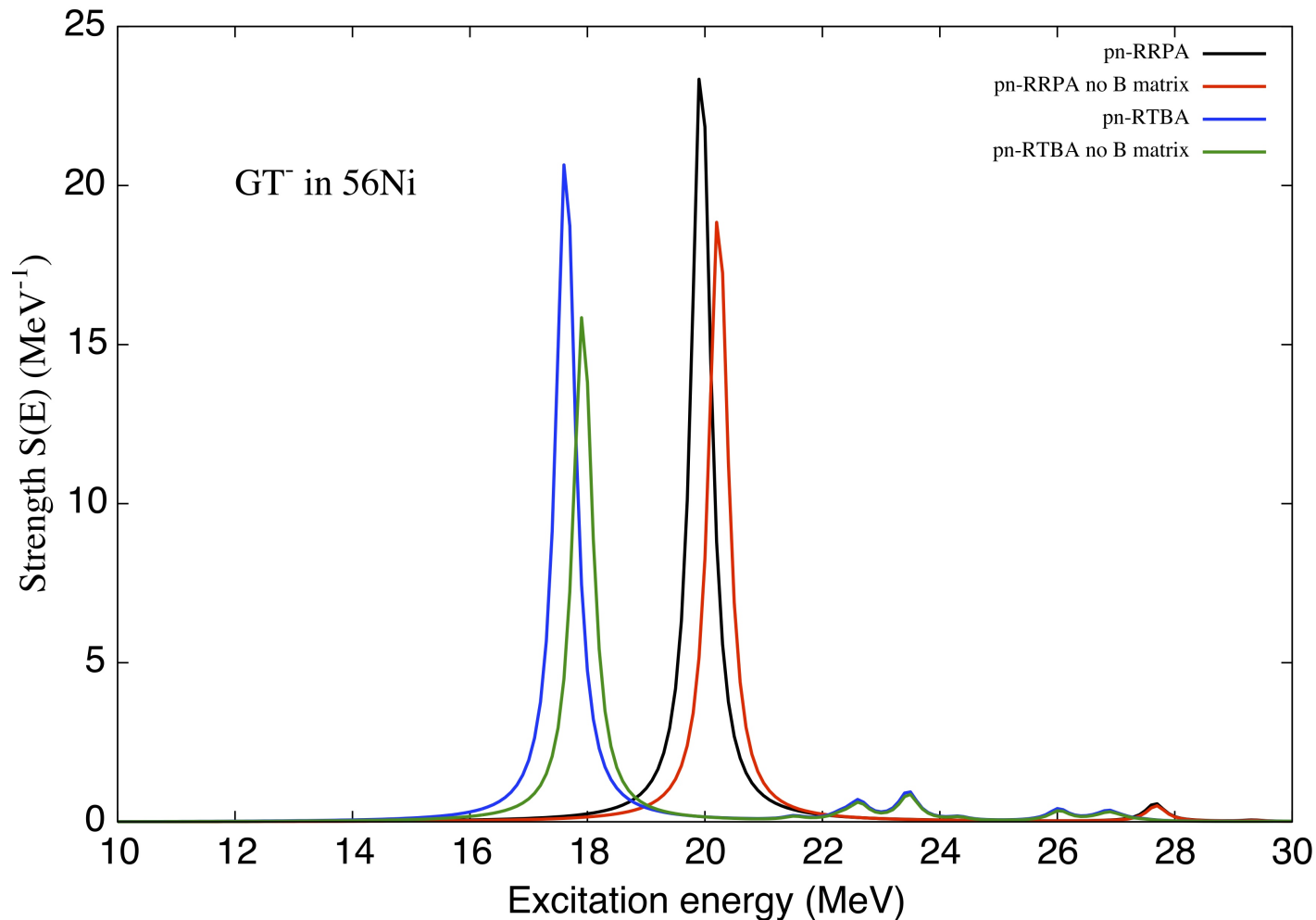
Ground-state correlations (GSC) in the Green's functions formalism are generated by the so-called "backward-going diagrams":

★ Currently in R(Q)TBA:



Ground-state correlations in RNFT

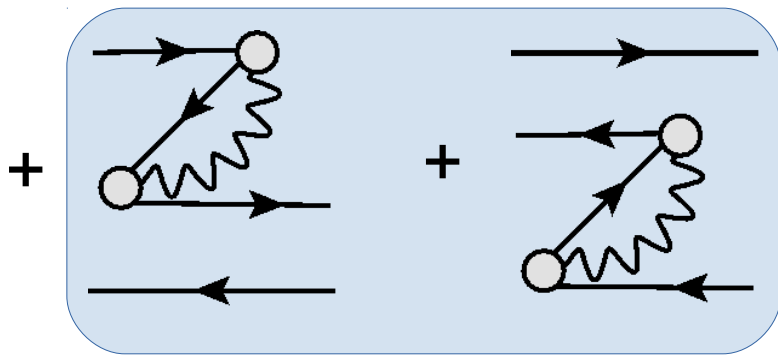
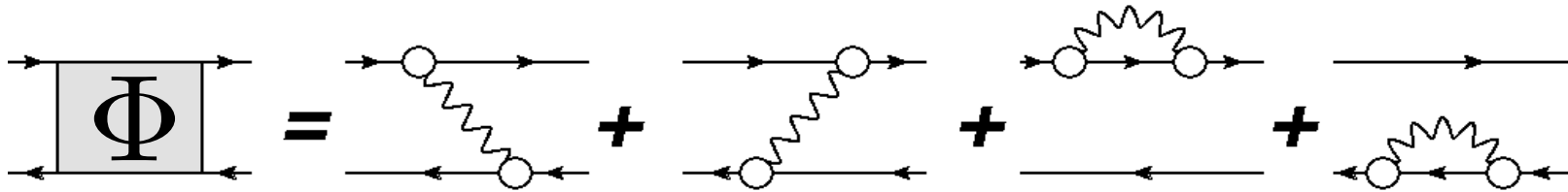
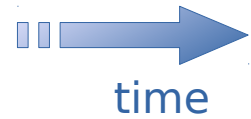
- ★ The B-matrix usually has a minor effect on isospin-transfer modes.
Example: Role of the B-matrix on the Gamow-Teller strength in ^{56}Ni :



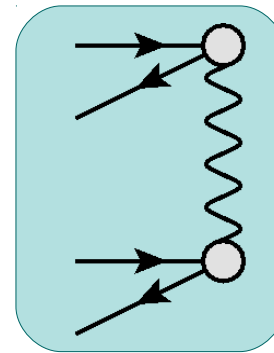
→ small effect although it is known from Shell-Model calculations that the ground-state wave function of ^{56}Ni is importantly fragmented ($\sim 65\%$ of $0p-0h$ configuration).

Ground-state correlations in RNFT

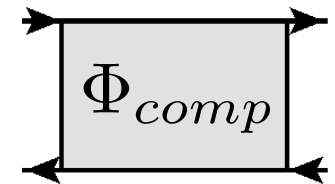
★ When GSC induced by QVC are included in the TBA, the component $R^{(--)}$ of the response are modified by the following diagrams:



Add to the A-matrix
-
Dynamic but do not
introduce new poles



Adds to the B-matrix
-
Static

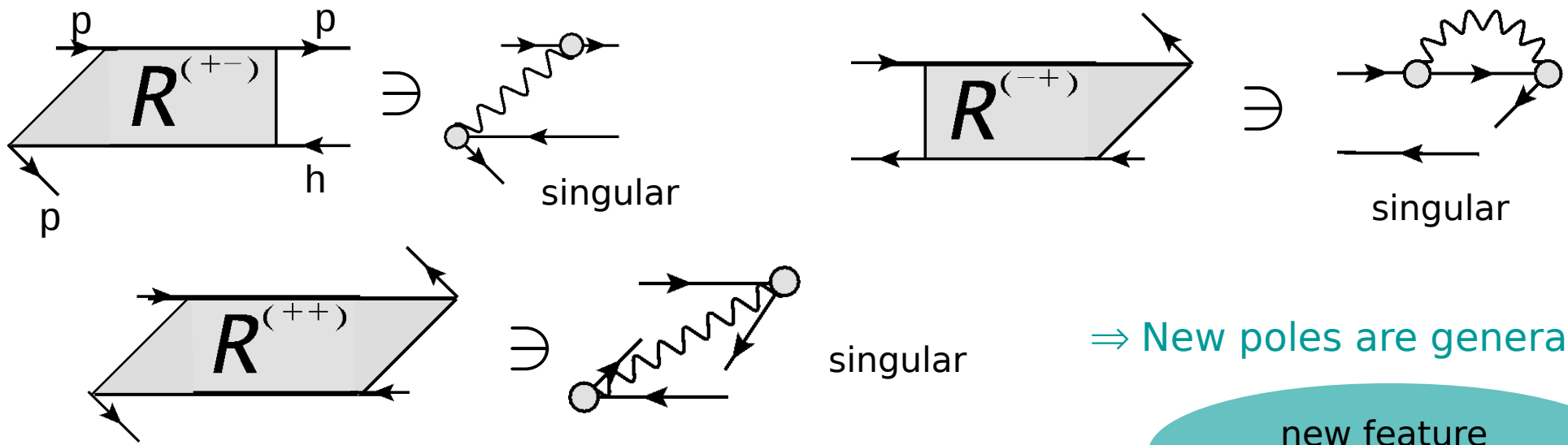


To compensate for
double-counting
of double self-energy
insertions

No new states → these diagrams only shift the previous $R(Q)$ TBA poles

Ground-state correlations in RNFT

★ Additionally, new components of the response appear:



⇒ New poles are generated

new feature compared to (Q)RPA

★ These components are related to R^{--} through:

$$R(\omega) = \left(1 + Q^{+-}(\omega)\right) R^{--}(\omega) \left(1 + Q^{-+}(\omega)\right) + P^{++}(\omega)$$

→ the dimensions of the problem remain the same!

★ They induce new types of transitions:



→ These effects should be very important for (p,n) strength in n-rich nuclei & (n,p) strength in p-rich nuclei

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Response theory for isospin-transfer modes:

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Ground-state correlations in the time-blocking approximation

Conclusion & perspectives

Conclusion, perspectives

→ Conclusions:

- ★ The RNFT is a powerful framework for the microscopic description of mid-mass to heavy nuclei, which allows the account for complex configurations of nucleons in a large model space.
- ★ It has been quite successful in the description of neutral excitations (E. Litvinova's talk).
- ★ It appears promising in the spin-isospin channel (description of both the low-energy strength and overall distribution to higher excitation energy).
- ★ However, in its present formulation (time-blocking approximation) it is often not sufficient.

→ Perspectives:

- ★ Inclusion of higher-order configurations (E. Litvinova's talk) and ground-state correlations (ongoing)
- ★ Application to double-charge exchange and double-beta decay ($2\nu\beta\beta$ and $0\nu\beta\beta$)
- ★ Together with RNFT in the neutral channel, this framework provides a high-quality and consistent description of both phases of the r-process nucleosynthesis, (n,γ) and β -decay \Rightarrow implementation in astrophysical modeling
- ★ Long-term goals: inclusion of the Fock term, inclusion of two-body currents and Delta resonance, start from bare interaction.

Thank you!

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